## Studifng Color Transparency

 through Backward $\pi^{0}$ Elichtronrodudion oif a Nuclear Wrget

Color Transparency and Hadroilization Workshop

## Mandelstam variables (s,t,u-channels)

$s$ : invariant mass of the system

$t$ : Four-momentum-transfer squared between target before and after interaction
$u$ : Four-momentum-transfer squared between virtual photon before interaction and target after interaction
$t$-channel: $\boldsymbol{- t} \sim 0$, after interaction
Target: stationary
Meson: forward
Measure of how forward could the meson go.
$u$-channel: $\boldsymbol{- u \sim 0 \text { , after interaction }}$
Target: forward
Meson: stationary
Measure of how backward could the meson go

## GPD-Like Model: TDA and Factorization



## Baryon to Meson Transition Distribution Amplitude (TDA)

- Extension of collinear factorization to backward angle regime. Further generalization of the concept of GPDs.
- Backward angle factorization first suggested by Frankfurt, Polykaov, Strikman, Zhalov, Zhalov [arXiv:hep-ph/0211263]
- TDAs describe the transition of nucleon to 3-quark state and final state meson [gray oval of plot b]
- A fundamental difference between GPDs and TDAs is that TDAs are defined as hadronic matrix elements of 3-quark operator, while GPDs involve quark-antiquark operator
- Can be accessed experimentally in backward angle meson electroproduction reactions


## Skewness in Backward Angle Regime

- Forward angle kinematics, $-t \sim-t_{\min }$ and $-u \sim-u_{\max }$, in the regime where handbag mechanism and GPD description may apply, Skewness is defined in usual manner:

$$
\begin{aligned}
& \xi_{t}=\frac{p_{1}^{+}-p_{2}^{+}}{p_{1}^{+}+p_{2}^{+}} \text {where } p_{1,2} \text { refer to light cone }+ \text { components } \\
& \text { in } \gamma^{*}(q)+p\left(p_{1}\right) \rightarrow \omega\left(p_{\pi}\right)+p^{\prime}\left(p_{2}\right)
\end{aligned}
$$

- Backward angle kinematics, $-u \sim-u_{\min }$ and $-t \sim-t_{\max }$, Skewness is defined with respect to $u$-channel momentum transfer in TDA formalism

$$
\xi_{u}=\frac{p_{1}^{+}-p_{\pi}^{+}}{p_{1}^{+}+p_{\pi}^{+}}
$$

- GPDs depend on $x, \xi_{t}$ and $t=\left(\Delta^{t}\right)^{2}=\left(p_{2}-p_{l}\right)^{2}$

TDAs depend on $x, \xi_{u}$ and $u=\left(\Delta^{u}\right)^{2}=\left(p_{\pi}-p_{I}\right)^{2}$

- Impact parameter space interpretation of TDAs is similar to GPDs, except one has to Fourier transform with respect to $\Delta^{u}{ }_{\mathrm{T}} \approx\left(p_{\pi}-p_{1}\right)_{\mathrm{T}}$


## Impact parameter Interpretation of TDA

- After integrating over one momentum fraction $x_{i}$, the three exchanged quarks can be treated as an effective diquark+quark pair
- Impact picture then looks very much like that for GPDs


ERBL: $x_{3}=w_{3}-\xi \geq 0 ; \quad x_{1}+x_{2}=\xi-w_{3} \geq 0 ;$
$\rightarrow$ All 3 quark momentum fractions $x_{i}$ positive


## Backward Angle Collinear Factorization

- Kinematical regime for collinear factorization involving TDAs is similar to that involving GPDs:
- $x_{B}$ fixed
- $|u|$-momentum transfer small compared to $Q^{2}$ and $s$
- $Q^{2}$ and $s$ sufficiently large
- Early scaling for GPD physics occurs $2<Q^{2}<5 \mathrm{GeV}^{2}$
- Maybe something similar occurs for TDA physics...


## Two Key Predictions in Factorization Regime:

- Dominance of transverse polarization of virtual photon, resulting in suppression of longitudinal cross section by at least $1 / Q^{2}: \sigma_{T}>\sigma_{L}$
- Characteristic $1 / Q^{8}$-scaling behavior of $\sigma_{T}$ for fixed $x_{B}$


## $p\left(e, e^{\prime} p\right) \omega Q^{2}-$ Dependence from Hall C

- To investigate $Q^{2}$-dependence,

$$
-u=-u_{\min }
$$ fit lowest $-u$ bin values of $\sigma_{T}$ and $\sigma_{L}$ to $Q^{-n}$ function - $\sigma_{T}$ appears to have a flat $Q^{2}$-dependence within measured range

- $\sigma_{L}$ shows much stronger decrease
- Decreasing L/T ratio indicates the gradual dominance of $\sigma_{T}$ as $Q^{2}$ increases.
- Trend qualitatively consistent with prediction of TDA Collinear Factorization.



## TDA model Comparison to Data



Hall C $\omega$ Electroproduction

Both data sets suggestive of early TDA scaling $Q^{2} \approx 2.5 \mathrm{GeV}^{2}$ !?


Hall B $\pi^{+}$Electroproduction
K. Park et al., PLB 780 (2017) 340

## Extension to Higher $Q^{2}$

- The 6 GeV JLab Halls B,C data are qualitatively consistent with the predictions of the backward-angle factorization / TDA formalism, but they are at a too low $Q^{2}$ to be in quantitative agreement.
- CLAS-6 $\pi^{+}$data, Hall C $\omega$ data
- Studies of the applicability of TDA formalism are being extended in the 12 GeV era, by measuring general scaling trend of separated $\mathrm{L} / \mathrm{T}$ cross sections for a variety of $u$-channel reactions
- 12 GeV data from Hall B
- Hall C $\rho, \omega, \varphi$ data (E12-09-011)
- Dedicated Hall C $\pi^{0}$ measurement (E12-20-007)


## Hall C 12 GeV data already acquired

$p\left(e, e^{\prime} p\right) X \quad$ Online Data Analysis

$$
Q^{2}=3.00 \quad W=2.32 \quad \theta_{p q}=+3.0^{\circ}-u=0.15 \quad \xi_{u}=0.15
$$



$K^{+} \mathrm{L} / \mathrm{T}$-experiment (E12-09-011)
Spokespersons: T. Horn, G.M. Huber, P. Markowitz

- Data acquired fall 2018-spring 2019
- Main purpose of experiment is to acquire $t$-channel L/T-separated $p\left(e, e^{\prime} K^{+}\right) \wedge$ data for reaction mechanism and $K^{+}$form factor studies
- Abundant $u$-channel $p\left(e, e^{\prime} p\right) X$ data acquired parasitically
- Will allow backward angle studies for several meson states over a wide kinematic range

| Setting | Low $\varepsilon$ data | High $\varepsilon$ data |
| :--- | :--- | :--- |
| $\mathrm{Q}^{2}=0.50$ |  |  |
| $\mathrm{~W}=2.40$ |  |  |
| $\mathrm{Q}^{2}=2.1$ |  |  |
| $\mathrm{~W}=2.95$ |  |  |
| $\mathrm{Q}^{2}=3.0$ |  |  |
| $\mathrm{~W}=2.32$ |  |  |
| $\mathrm{Q}^{2}=3.0$ |  |  |
| $\mathrm{~W}=3.14$ |  |  |
| $\mathrm{Q}^{2}=4.4$ |  |  |
| $\mathrm{~W}=2.74$ |  |  |
| $\mathrm{Q}^{2}=5.5$ |  |  |
| $\mathrm{~W}=3.02$ |  |  |

## Backward Exclusive $\pi^{0}$ Production



E12-20-007: $\boldsymbol{u \approx 0} \pi^{0}$ production in Hall C
Spokespersons: W.B. Li, G.M. Huber, J. Stevens
Purpose: test applicability of TDA formalism for $\pi^{0}$ production

- Is $\sigma_{T}$ dominant over $\sigma_{L}$ ?
- Does the $\sigma_{T}$ cross section at constant $x_{B}$ scale as $1 / Q^{8}$ ?
- Kinematics overlap forward angle $p\left(e, e^{\prime} \pi^{0}\right) p$ experiment with NPS+HMS


## $\mathbf{p}\left(\mathbf{e}, \mathrm{e}^{\prime} \mathbf{p}\right) \pi^{0}$ Skewness Range



$$
\xi_{u}=\frac{p_{1}^{+}-p_{\pi}^{+}}{p_{1}^{+}+p_{\pi}^{+}}
$$

HMS and SHMS acceptance cuts, and diamond cuts applied

## CT and Backward-angle Factorization

- CT has recently been shown to not apply in $\mathrm{C}\left(\mathrm{e}, \mathrm{e}\right.$ 'p) up to $\mathrm{Q}^{2}=14 \mathrm{GeV}^{2}$, in contrast to CT applying already in $\mathrm{A}\left(\mathrm{e}, \mathrm{e}^{\prime} \pi^{+}\right)$at $\mathrm{Q}^{2} \approx 5 \mathrm{GeV}^{2}$

- Color Transparency is a co-requisite of reaching the factorization regime, and is expected to be an equally valid requirement for both forward-angle and backward-angle factorizations


## Backward-angle A(e, $\left.\mathbf{e}^{\prime} p\right) \pi^{0}$

-Since JLab 6 GeV data are qualitatively consistent with early factorization in backward kinematics, backward-angle meson production events with a high momentum forward proton may provide an alternate means of probing Color Transparency

- Example is $\pi^{0}$ production, but technique extendable also to vector meson production. A short test could be attempted in E12-20-007

|  | $\mathrm{A}(\mathrm{e}, \mathrm{e}$ 'p $) \pi^{0}$ Kinematics $\mathrm{E}_{\text {beam }}=10.6 \mathrm{~W}=2 \mathrm{GeV}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\underset{\left(\mathrm{GeV}^{2}\right)}{\boldsymbol{Q}^{2}}$ | $\begin{gathered} \boldsymbol{e}^{\prime}(\mathrm{GeV} / \mathrm{c}, \\ \mathrm{deg}) \end{gathered}$ | $\begin{gathered} \boldsymbol{p}(\mathrm{GeV} / \mathrm{c}, \\ \mathrm{deg}) \end{gathered}$ | $\begin{gathered} \pi^{0}(\mathrm{GeV} / \mathrm{c}, \\ \mathrm{deg}) \end{gathered}$ | $\begin{gathered} \boldsymbol{t} \\ \left(\mathrm{GeV}^{2}\right) \end{gathered}$ | $\underset{\left(\mathrm{GeV}^{2}\right)}{\boldsymbol{u}}$ |
|  | 3 | $\begin{aligned} & \hline 7.3 @ \\ & 11.3^{\circ} \end{aligned}$ | $\begin{gathered} \hline 3.9-3.6 @ \\ 23^{\circ}-30^{\circ} \end{gathered}$ | $\begin{aligned} & \hline 0.2-0.5 \text { @ } \\ & 2020-95^{\circ} \end{aligned}$ | $\begin{gathered} -5.7 \text { to } \\ -5.2 \end{gathered}$ | $\begin{gathered} +0.5 \text { to } \\ -0.1 \end{gathered}$ |
|  | 6 | $\begin{aligned} & \hline 5.7 @ \\ & 18.1^{\circ} \end{aligned}$ | $\begin{gathered} \hline 5.6-5.2 @ \\ 190-24^{\circ} \end{gathered}$ | $\begin{gathered} \hline 0.1-0.5 @ \\ 1966^{\circ}-79^{\circ} \end{gathered}$ | $\begin{gathered} \hline-8.8 \text { to }- \\ 8.2 \end{gathered}$ | $\begin{gathered} \hline+0.6 \text { to } \\ 0.0 \end{gathered}$ |
|  | 10 | $\begin{aligned} & 3.6 @ \\ & 29.7^{\circ} \end{aligned}$ | $\begin{array}{c\|} \hline 7.7-7.3 @ \\ 13^{\circ}-16^{\circ} \end{array}$ | $\begin{gathered} \hline 0.0-0.5 @ \\ 1930-61^{\circ} \end{gathered}$ | $\begin{gathered} -12.8 \text { to } \\ -12.1 \end{gathered}$ | $\begin{gathered} \text { +0.6 to } \\ -0.1 \end{gathered}$ |
|  | 14 | $\begin{aligned} & \hline 1.5 @ \\ & 56.7^{\circ} \end{aligned}$ | $\begin{aligned} & \hline 9.9-9.5 @ \\ & 70-90 \end{aligned}$ | $\begin{gathered} \hline 0.1-0.5 @ \\ 187^{\circ}-50^{\circ} \end{gathered}$ | $\begin{gathered} -16.8 \text { to } \\ -16.2 \end{gathered}$ | $\begin{gathered} \hline+0.6 \text { to } \\ -0.1 \end{gathered}$ |

## Theoretical considerations

- Halls B,C 6 GeV data hint at applicability of backward-angle factorization mechanism as early as $\mathrm{Q}^{2}=2.5 \mathrm{GeV}^{2}$
- If this interpretation is correct, it can be confirmed by $u$-channel CT measurements such as $A\left(e, e^{\prime} p\right) \pi^{0}$
- Considerations:
- CT will not appear in the same way for backward $\pi^{0}$ as for the other experiments. This is because the $\pi^{0}$ does not originate from a pointlike quark configuration, it is attached to the TDA which has no small transverse distance inside
■ Even if factorization applies, the $\pi^{0}$ will be subject to strong interactions in the nucleus, such as absorption, or formation of a $2 \pi$ state
- One should not insist on detecting the final meson. Rather, it would be sufficient to require $120<\mathrm{m}_{\text {missing }}<500 \mathrm{MeV}$. It is important to detect the high-momentum forward-going nucleon.
- More work would clearly be needed for model calculations of CT ratios for this new type of experiment. It gives rise to the intriguing idea of "Half Color Transparency". [Bernard Pire]


## Summary

- New experimental technique pioneered at JLab Hall C has opened up a unique kinematic regime for study:
- Extreme backward angle ( $u \approx 0$ ) scattering
- Detect forward-going proton in parallel kinematics
- Leaves "recoil" meson nearly-at-rest in target
- Possible access to Transition Distribution Amplitudes
- Universal perturbative objects in u-channel, analogous to GPDs
- Access to 3-quark plus sea component $\psi_{(3 q+q \bar{q})}$ of nucleon
- The approach of backward angle factorization regime can be studied via $u$-channel CT measurements, such as $\mathrm{A}\left(\mathrm{e}, \mathrm{e}^{\prime} \mathrm{p}\right) \pi^{0}$, across a variety of nuclei

부밍운 University

## TDA Formalism (e.g. $u$-channel $\pi^{0}$ )

- Fourier transform of the $\pi N$ transition matrix element

$$
\begin{aligned}
& 4 \stackrel{\downarrow}{\mathcal{F}}\left\langle\pi_{\alpha}\left(p_{\pi}\right)\right| \widehat{O}_{\rho \tau \chi}\left(\lambda_{1} n, \lambda_{2} n, \lambda_{3} n\right)\left|N_{\iota}\left(p_{1}\right)\right\rangle \\
= & \delta\left(x_{1}+x_{2}+x_{3}-2 \xi_{u}\right) \sum_{\text {s.f. }}\left(f_{a}\right)_{\iota}^{\alpha \beta \gamma} s_{\rho \tau, \chi} H_{s . f .}^{\pi N}\left(x_{1}, x_{2}, x_{3}, \xi_{u}, \Delta^{2} ; \mu_{F}^{2}\right)
\end{aligned}
$$

- $\pi N$ TDA invariant amplitudes (eight TDAs at leading twist)

$$
H_{s . f .}^{\pi N}=\left\{V_{1,2}^{\pi N}, A_{1,2}^{\pi N}, T_{1,2,3,4}^{\pi N}\right\}
$$

- Factorizing out the $u$-dependence:
meson to nucleon transition form factor

$$
H^{\pi N}\left(x, \xi_{u}, \Delta^{2}\right)=H^{\pi N}\left(x_{i}, \xi_{u}\right) \times G\left(\Delta^{2}\right)
$$

$$
\Delta^{2}=u
$$

J.P. Lansberg, B. Pire, K. Semenov-Tian-Shansky, L. Szymanowski, Phys. Rev. D 85 (2011) 054201

## $\pi^{0} p$ TDAs as functions of $q$-diquark coordinates

University
of Regina

$$
w=\xi_{u}-x_{3} ; v=\frac{x_{1}-x_{2}}{2}
$$






Axiäl-Vector


## Partonic Interpretation of TDA

Main reactions of interest to date:

- Backward angle exclusive $\pi^{0}, \pi^{+}, \rho, \omega, \varphi$ production
- Backward angle DVCS


Interpretation of $\pi N$ TDAs in light-cone quark model
a) Quark sea contrib to baryon wf (ERBL region)
b) Minimal Fock states of baryon \& meson (DGLAP-1) region
c) Quark sea contribution to meson wf (DGLAP-2)

$\pi^{0} p$ TDAs (CZ): Vector


Axial-Vector


Tensor

Model based on spectral representation w/ CZ sol for DA as input (function of quark-diquark coord)

## TDAs Formalism - 1

$$
T_{\alpha}
$$

$$
T_{\alpha}^{\prime}
$$


computed as functions of quark-diquark coordinates

## TDA Meson Production Cross Section

## ■ Unpolarized exclusive $\pi^{0}$ production cross section:

$$
\begin{aligned}
& \text { 皆 } \quad \frac{d^{2} \sigma_{T}}{d \Omega_{\pi}}=\left|\mathcal{C}^{2}\right| \frac{1}{Q^{6}} \frac{\Lambda\left(s, m^{2}, M^{2}\right)}{128 \pi^{2} s\left(s-M^{2}\right)} \frac{1+\xi}{\xi}\left(|\mathcal{I}|^{2}-\frac{\Delta_{T}^{2}}{M^{2}}\left|\mathcal{I}^{\prime}\right|^{2}\right) \\
& \mathcal{I}=\int\left(2 \sum_{\alpha=1}^{7} T_{\alpha}+\sum_{\alpha=8}^{14} T_{\alpha}\right) \quad \mathcal{I}^{\prime}=\int\left(2 \sum_{\alpha=1}^{7} T_{\alpha}^{\prime}+\sum_{\alpha=8}^{14} T_{\alpha}^{\prime}\right)
\end{aligned}
$$

J. P. Lansberg, B. Pire, K. Semenov-Tian-Shansky, L. Szymananovski, Phys. Rev. D 85 (2011) 054021

## TDA Model Predictions for JLab E12-19-006

$\mathbf{F} \boldsymbol{\pi}$ - $\mathbf{1 2}$ experiment (E12-19-006) L/T separations up to $Q^{2}=8.5 \mathrm{GeV}^{2}$ Spokespersons: D. Gaskell, G.M. Huber, T. Horn

- L/T-Separations over wide kinematic range will allow $\sigma_{T}$ " $\sigma_{\mathrm{L}}$ and $1 / Q^{8}$ scaling predictions to be checked with greater authority
- u-channel $\varphi$-electroproduction particularly interesting
- Sensitive to Strangeness content of nucleon
- Combined analysis of $\rho$, $\omega$ production allows one to disentangle isotopic structure of $V N$ TDAs in non-strange sector




At $Q^{2}=6.0 \mathrm{GeV}^{2}$, $\omega$ predicted to remain dominant (unlike $t$-channel), $\varphi$ to drop rapidly with $-u$.

## SIMC: Q²_W overlap at high, low $\varepsilon, ~_{\varepsilon}$



$\boldsymbol{p}(\boldsymbol{e}, \boldsymbol{e} \boldsymbol{p}) \boldsymbol{\pi}^{\boldsymbol{0}}$ : HMS and SHMS acceptance cuts applied



## $\pi^{0}$ Channel Expected to be Clean

- In comparison to backwardangle $\omega$ electroproduction, there is little physics background in $\pi^{0}$ production.
- Bethe-Heitler process has no backward-angle peak, and will be negligible.
- VCS should dominate backward-angle $\gamma$ production, but is expected to be much smaller than $\pi^{0}$ production.

$\mathrm{BH}+\mathrm{VCS}$ simulations based on code by P. Guichon and M. Vanderhaeghen.
- BH calculation is exact.
- VCS calculation makes use of ad-hoc ansatz based on $u$-channel $\omega$ data.
$Q^{2}=3.0 \mathrm{GeV}^{2}, W=2.49 \mathrm{GeV}, \phi=0$


SHMS+HMS Q ${ }^{2}=3.0$ Simulation


## SIMC: Missing Mass squared

Missing mass ${ }^{2}$


Missing mass ${ }^{2}$


HMS and SHMS acceptance cuts, and diamond cuts applied


Missing mass ${ }^{2}$


## Central Kinematics are $\mathrm{x}_{\text {Bjorken }}=0.36$



HMS and SHMS acceptance cuts, and diamond cuts applied

## $p\left(e, e^{\prime} p\right) \pi^{0} Q^{2}$-dependence projections

Ex University of Regina


# Missing Mass Background Removal 



## Background Extraction and Check











## Reconstructed Missing Energy

 Worse Example
## Yield Ratio and Model Cross-Section



## Unseparated Cross Sections

* U University of Regina

$$
2 \pi \frac{d^{2} \sigma}{d t d \phi}=\varepsilon \frac{d \sigma_{L}}{d t}+\frac{d \sigma_{T}}{d t}+\sqrt{2 \varepsilon(\varepsilon+1)} \frac{d \sigma_{L T}}{d t} \cos \phi+\varepsilon \frac{d \sigma_{T T}}{d t} \cos 2 \phi
$$




## Regge Trajectory Model by J-M Laget

"
of Regina


33

## Hadronic Model: Regge Model by JM Laget



Soft structure $\rightarrow$ Hard $\rightarrow$ Soft transition!

## Extension to Higher $\mathbf{Q}^{2}$

1. Determine if the backward angle peak observed in exclusive $\omega$ electroproduction occurs also in other channels, over a broad kinematic range.
2. Measure the $u$-dependence of L/T-separated cross sections, to determine the relevance of Regge-rescattering and TDA mechanisms in JLab kinematics.
3. Assuming the backward angle peak is present, as expected, measure the $\sigma_{T} / \sigma_{L}$ ratio over a wide $Q^{2}$ range for $\mathrm{W}>2 \mathrm{GeV}$.

- Where does $\sigma_{T} » \sigma_{L}$, as predicted by TDA formalism?

4. Determine the $Q^{2}-$ dependence of $\sigma_{T}$ at fixed $x_{B}$.

- Where does $\sigma_{T} \sim 1 / Q^{8}$ as predicted by TDA formalism?


## Questions to be addressed

- Halls B,C 6 GeV data hint at applicability of backward-angle factorization mechanism as early as $\mathrm{Q}^{2}=2.5 \mathrm{GeV}^{2}$
- If this interpretation is correct, it can be confirmed by $u$-channel CT measurements such as $A\left(e, e^{\prime} p\right) \pi^{0}$
- The observation of CT in $A\left(e, e^{\prime} p\right) \pi^{0}$ by Q2=14 GeV2, when it is absent in A(e,e'p), would be a considerable achievement
- Other Considerations:
- In the quasi-elastic process, the observed fast nucleon is part of the nuclear target. In the TDA picture, the fast proton comes from the partons of the original proton target.
- It is not obvious that the fast proton from the $u$-channel interaction is the same as the original construct of the "original" valence quarks, thus would it really inherit all of the properties from the original proton?
- Is the proton from the fast proton quasi-elastic process the same as the fast $u$-channel fast proton, and could this proton experience color transparency?

