Studying Color Transparency through Backward a Electroproduction of a Nuclear Target



Garth Huber University of Regina Wenliang Li

WILLIAM どMARY



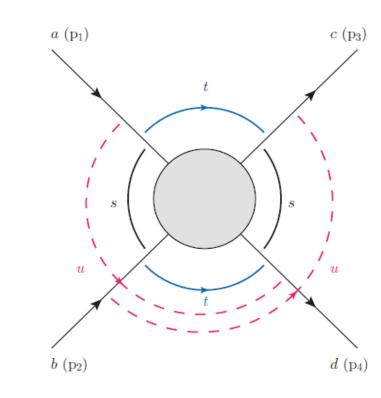
Supported by:



SAPIN-2021-000

Mandelstam variables (s,t,u-channels)





$$s = (p_1 + p_2)^2 = (p_3 + p_4)^2$$
$$t = (p_1 - p_3)^2 = (p_2 - p_4)^2$$
$$u = (p_1 - p_4)^2 = (p_2 - p_3)^2$$

s: invariant mass of the system

t: Four–momentum–transfer squared between target before and after interaction

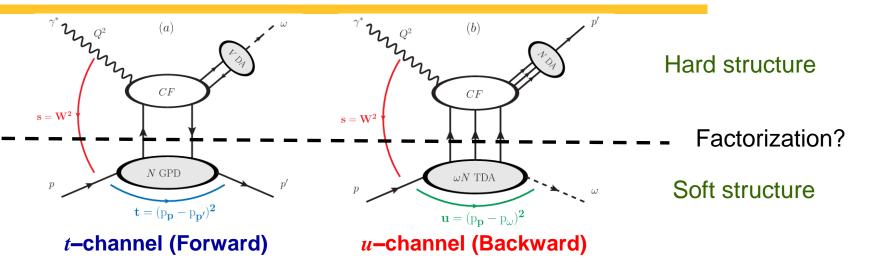
u: Four–momentum–transfer squared between virtual photon before interaction and target after interaction

t-channel: -*t* ~ 0, after interaction Target: stationary Meson: forward Measure of how forward could the meson go.

u-channel: -*u*~0, after interaction Target: forward Meson: stationary Measure of how backward could the meson go

GPD–Like Model: TDA and Factorization





Baryon to Meson Transition Distribution Amplitude (TDA)

- Extension of collinear factorization to backward angle regime.
 Further generalization of the concept of GPDs.
- Backward angle factorization first suggested by Frankfurt, Polykaov, Strikman, Zhalov, Zhalov [arXiv:hep-ph/0211263]
- TDAs describe the transition of nucleon to 3-quark state and final state meson [gray oval of plot b]
- A fundamental difference between GPDs and TDAs is that TDAs are defined as hadronic matrix elements of 3-quark operator, while GPDs involve quark-antiquark operator
- Can be accessed experimentally in backward angle meson electroproduction reactions

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Skewness in Backward Angle Regime



Forward angle kinematics, -t ~ -t_{min} and -u ~ -u_{max}, in the regime where handbag mechanism and GPD description may apply, Skewness is defined in usual manner:

 $\xi_t = \frac{p_1^+ - p_2^+}{p_1^+ + p_2^+} \text{ where } p_{1,2} \text{ refer to light cone + components}$ $\text{ in } \gamma^*(q) + p(p_1) \to \omega(p_\pi) + p'(p_2)$

Backward angle kinematics, $-u \sim -u_{min}$ and $-t \sim -t_{max}$, Skewness is defined with respect to *u*-channel momentum transfer in TDA formalism

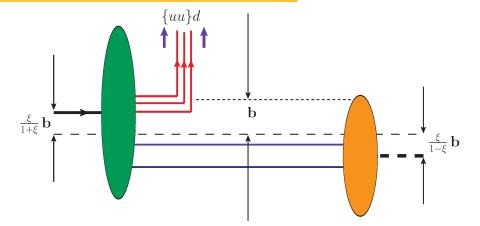
$$\xi_{u} = \frac{p_{1}^{+} - p_{\pi}^{+}}{p_{1}^{+} + p_{\pi}^{+}}$$

- GPDs depend on x, ξ_t and $t = (\Delta^t)^2 = (p_2 p_1)^2$ TDAs depend on x, ξ_u and $u = (\Delta^u)^2 = (p_\pi - p_1)^2$
- Impact parameter space interpretation of TDAs is similar to GPDs, except one has to Fourier transform with respect to $\Delta^{u}_{T} \approx (p_{\pi} - p_{I})_{T}$

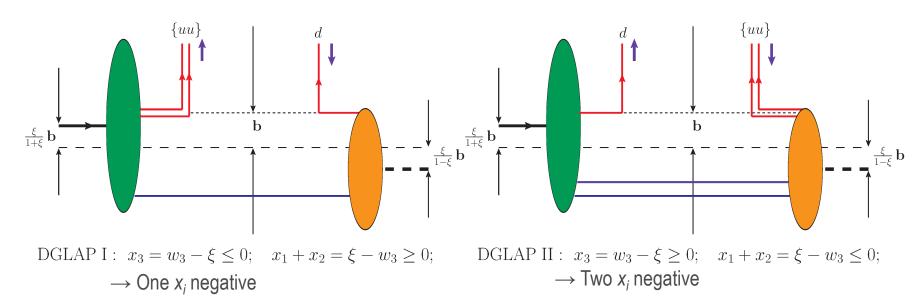
Impact parameter Interpretation of TDA



- After integrating over one momentum fraction x_i, the three exchanged quarks can be treated as an effective diquark+quark pair
- Impact picture then looks very much like that for GPDs



ERBL : $x_3 = w_3 - \xi \ge 0$; $x_1 + x_2 = \xi - w_3 \ge 0$; \rightarrow All 3 quark momentum fractions x_i positive



Backward Angle Collinear Factorization



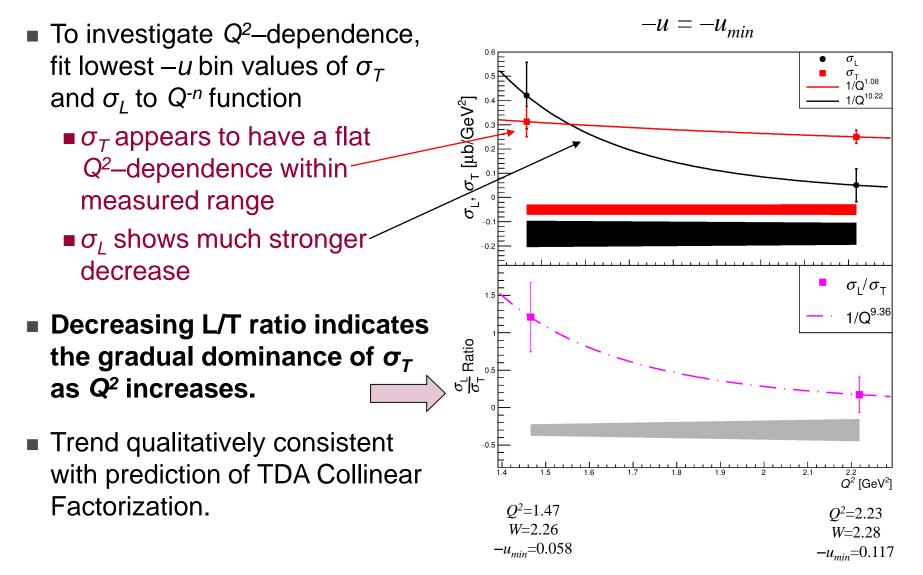
- Kinematical regime for collinear factorization involving TDAs is similar to that involving GPDs:
 - x_B fixed
 - /u/-momentum transfer small compared to Q^2 and s
 - Q^2 and s sufficiently large
- Early scaling for GPD physics occurs 2<Q²<5 GeV²
 - Maybe something similar occurs for TDA physics...

Two Key Predictions in Factorization Regime:

- Dominance of transverse polarization of virtual photon, resulting in suppression of longitudinal cross section by at least 1/Q²: σ_T » σ_L
- Characteristic $1/Q^8$ —scaling behavior of σ_T for fixed x_B

$p(e,e'p)\omega Q^2$ –Dependence from Hall C

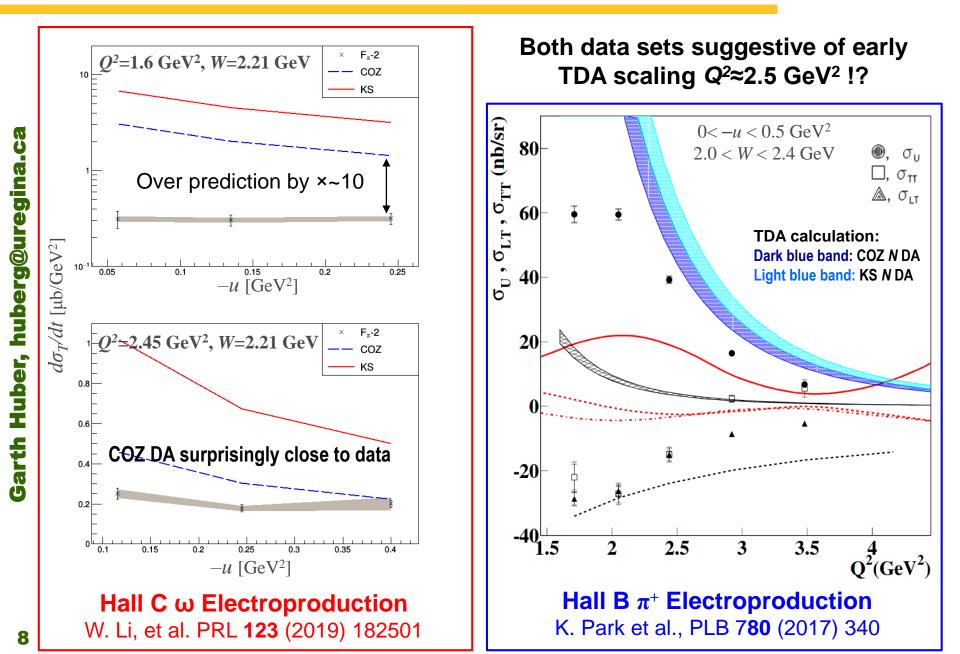




W. Li, et al. PRL **123** (2019) 182501

TDA model Comparison to Data



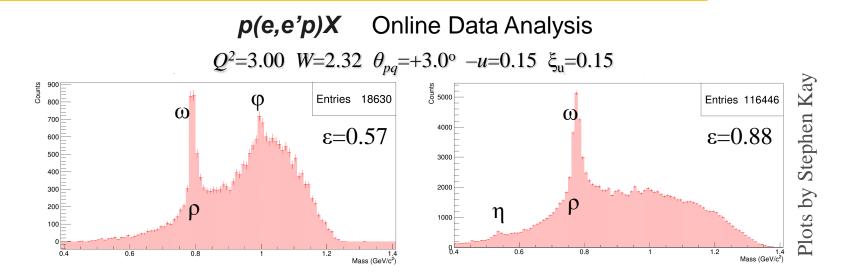


Extension to Higher Q²



- The 6 GeV JLab Halls B,C data are qualitatively consistent with the predictions of the backward-angle factorization / TDA formalism, but they are at a too low Q² to be in quantitative agreement.
 - CLAS–6 π^+ data, Hall C ω data
- Studies of the applicability of TDA formalism are being extended in the 12 GeV era, by measuring general scaling trend of separated L/T cross sections for a variety of *u*-channel reactions
 - 12 GeV data from Hall B
 - Hall C ρ, ω, φ data (E12-09-011)
 - Dedicated Hall C π^0 measurement (E12-20-007)

Hall C 12 GeV data already acquired



K⁺ L/T–experiment (E12–09–011)

Spokespersons: T. Horn, G.M. Huber, P. Markowitz

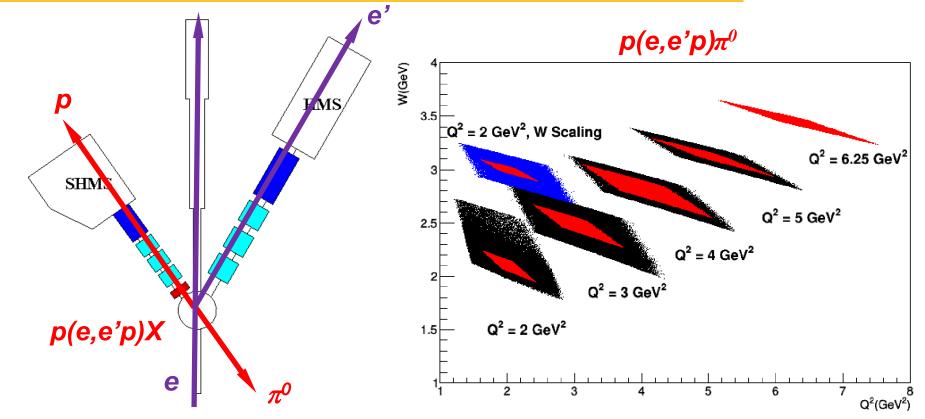
- Data acquired fall 2018–spring 2019
- Main purpose of experiment is to acquire t-channel L/T-separated p(e,e'K+)A data for reaction mechanism and K+ form factor studies
- Abundant u-channel p(e,e'p)X data acquired parasitically
 - Will allow backward angle studies for several meson states over a wide kinematic range

Setting	Low ε data	t <mark>a</mark> High ε data	
Q ² =0.50 W=2.40			
Q ² =2.1 W=2.95			
Q ² =3.0 W=2.32			
Q ² =3.0 W=3.14		*	
Q ² =4.4 W=2.74		-	
Q ² =5.5 W=3.02			

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Backward Exclusive π^0 Production





E12–20–007: $u \approx 0 \pi^0$ production in Hall C

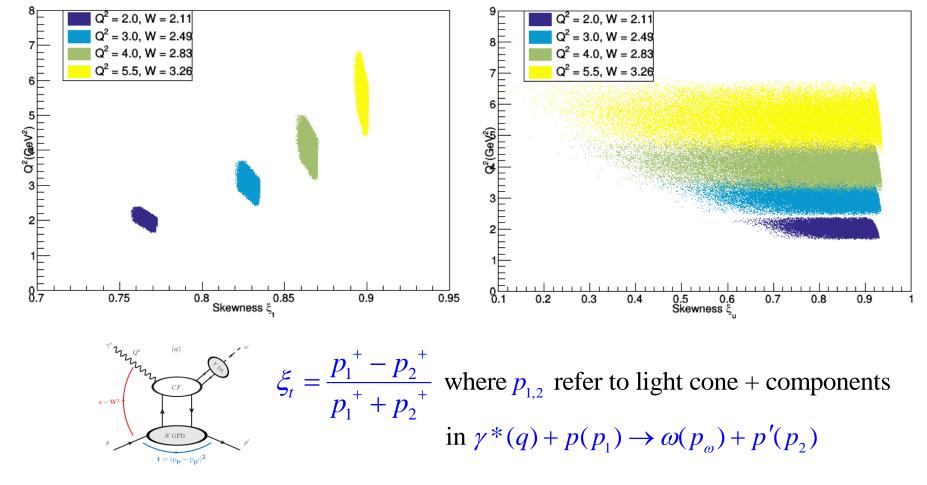
Spokespersons: W.B. Li, G.M. Huber, J. Stevens

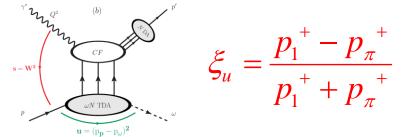
Purpose: test applicability of TDA formalism for π^0 production

- Is σ_T dominant over σ_L ?
- Does the σ_T cross section at constant x_B scale as $1/Q^8$?
- Kinematics overlap forward angle $p(e, e'\pi^0)p$ experiment with NPS+HMS

$p(e,e'p)\pi^0$ Skewness Range







HMS and SHMS acceptance cuts, and diamond cuts applied

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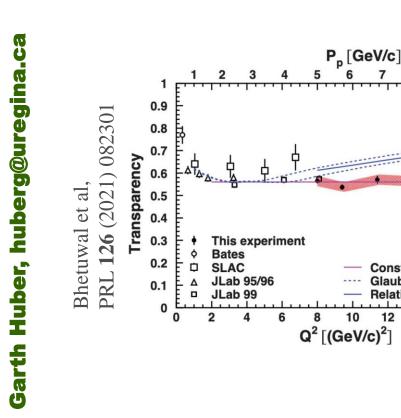
CT and Backward-angle Factorization

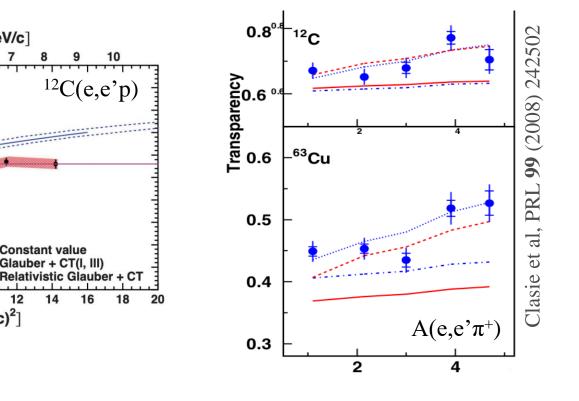
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• CT has recently been shown to not apply in $C(e,e^{p})$ up to $Q^{2}=14$ GeV², in contrast to CT applying already in A(e,e' π^+) at Q² \approx 5 GeV²



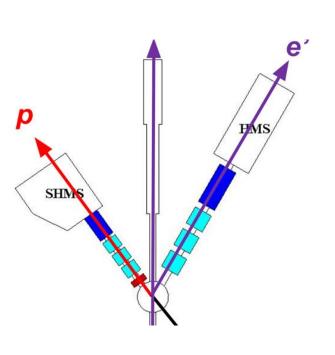


Color Transparency is a co-requisite of reaching the factorization regime, and is expected to be an equally valid requirement for both forward-angle and backward-angle factorizations

Backward-angle A(e,e'p) π^0



- Since JLab 6 GeV data are qualitatively consistent with early factorization in backward kinematics, backward-angle meson production events with a high momentum forward proton may provide an alternate means of probing Color Transparency
- Example is π^0 production, but technique extendable also to vector meson production. A short test could be attempted in E12-20-007



A(e,e'p) π^0 Kinematics E _{beam} =10.6 W=2 GeV						
Q ² (GeV ²)	<i>e</i> ' (GeV/c, deg)	p (GeV/c, deg)	$oldsymbol{\pi^0}$ (GeV/c, deg)	<i>t</i> (GeV²)	u (GeV²)	
3	7.3 @	3.9-3.6 @	0.2-0.5 @	-5.7 to	+0.5 to	
	11.3º	23º-30º	202º-95º	-5.2	-0.1	
6	5.7 @	5.6-5.2 @	0.1-0.5 @	-8.8 to -	+0.6 to	
	18.1º	19º-24º	196º-79º	8.2	0.0	
10	3.6 @	7.7-7.3 @	0.0-0.5 @	-12.8 to	+0.6 to	
	29.7º	13º-16º	193º-61º	-12.1	-0.1	
14	1.5 @	9.9-9.5 @	0.1-0.5 @	-16.8 to	+0.6 to	
	56.7º	7º-9º	187º-50º	-16.2	-0.1	

Theoretical considerations



- Halls B,C 6 GeV data hint at applicability of backward-angle factorization mechanism as early as Q²=2.5 GeV²
- If this interpretation is correct, it can be confirmed by *u*-channel CT measurements such as A(e,e'p)π⁰
- Considerations:
 - CT will not appear in the same way for backward π^0 as for the other experiments. This is because the π^0 does not originate from a point-like quark configuration, it is attached to the TDA which has no small transverse distance inside
 - Even if factorization applies, the π⁰ will be subject to strong interactions in the nucleus, such as absorption, or formation of a 2π state
 - One should not insist on detecting the final meson. Rather, it would be sufficient to require 120<m_{missing}<500 MeV. It is important to detect the high-momentum forward-going nucleon.
- More work would clearly be needed for model calculations of CT ratios for this new type of experiment. It gives rise to the intriguing idea of "Half Color Transparency".[Bernard Pire]

Summary



- New experimental technique pioneered at JLab Hall C has opened up a unique kinematic regime for study:
 - Extreme backward angle (*u*≈0) scattering
 - Detect forward–going proton in parallel kinematics
 - Leaves "recoil" meson nearly-at-rest in target
- Possible access to Transition Distribution Amplitudes
 - Universal perturbative objects in u-channel, analogous to GPDs
 - Access to 3–quark plus sea component $\Psi_{(3q+q\bar{q})}$ of nucleon
- The approach of backward angle factorization regime can be studied via *u*-channel CT measurements, such as A(e,e'p)π⁰, across a variety of nuclei



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TDA Formalism (e.g. u-channel π^0)



• Fourier transform of the πN transition matrix element $4\mathcal{F}\langle \pi_{\alpha}(p_{\pi})|\hat{O}_{\rho\tau\chi}(\lambda_{1}n,\lambda_{2}n,\lambda_{3}n)|N_{\iota}(p_{1})\rangle$ Factorization scale $=\delta(x_{1}+x_{2}+x_{3}-2\xi_{u})\sum_{s.f.}(f_{a})_{\iota}^{\alpha\beta\gamma}s_{\rho\tau,\chi}H_{s.f.}^{\pi N}(x_{1},x_{2},x_{3},\xi_{u},\Delta^{2};\mu_{F}^{2})$

• πN TDA invariant amplitudes (eight TDAs at leading twist)

$$H_{s.f.}^{\pi N} = \{V_{1,2}^{\pi N}, A_{1,2}^{\pi N}, T_{1,2,3,4}^{\pi N}\}$$

Factorizing out the *u*-dependence:

meson to nucleon transition form factor

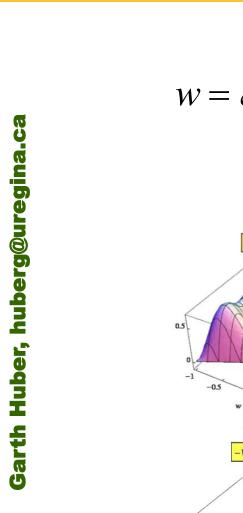
$$H^{\pi N}(x,\xi_u,\Delta^2) = H^{\pi N}(x_i,\xi_u) \times G(\Delta^2)$$

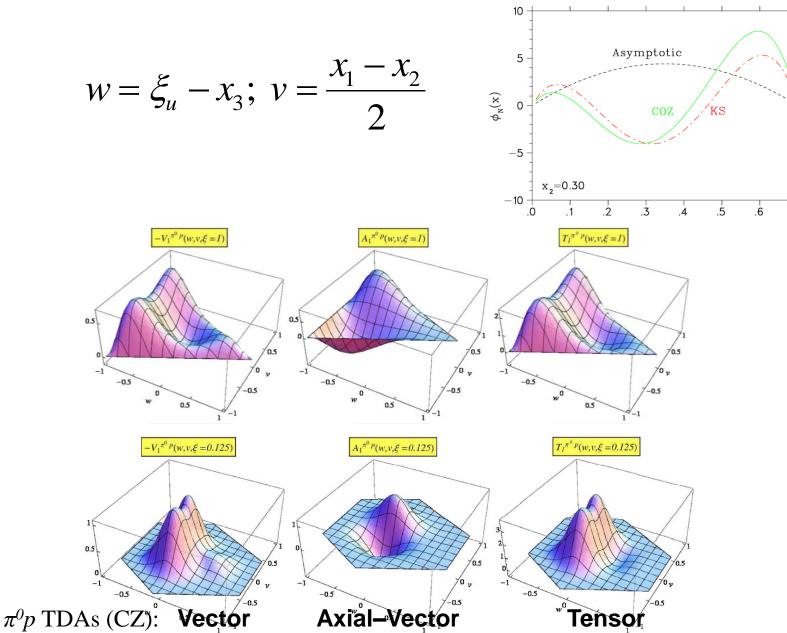
J.P. Lansberg, B. Pire, K. Semenov–Tian–Shansky, L. Szymanowski, Phys. Rev. D 85 (2011) 054201

π^{0} p TDAs as functions of q-diquark coordinates



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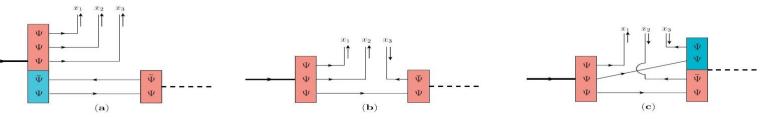
Partonic Interpretation of TDA



J.P. Lansberg et al., PRD **85** (2012) 054201

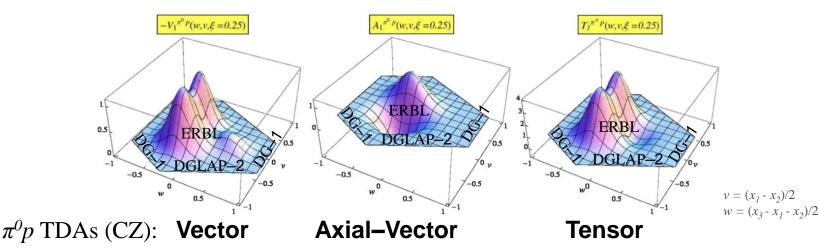
Main reactions of interest to date:

- **Backward angle exclusive** π^0 , π^+ , ρ , ω , φ production
- Backward angle DVCS



Interpretation of πN TDAs in light–cone quark model

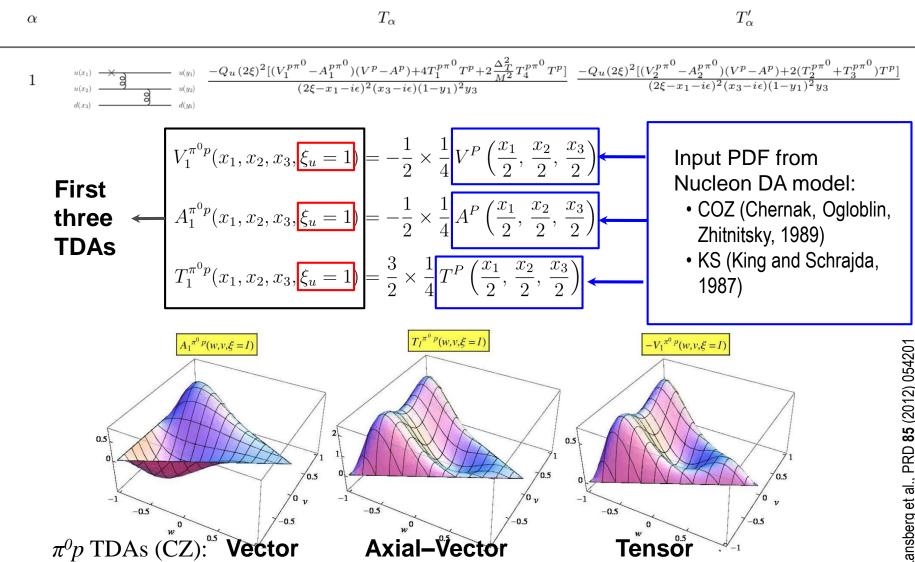
- a) Quark sea contrib to baryon wf (ERBL region)
- b) Minimal Fock states of baryon & meson (DGLAP-1) region
- c) Quark sea contribution to meson wf (DGLAP-2)



Model based on spectral representation w/ CZ sol for DA as input (function of quark-diquark coord)

TDAs Formalism – 1





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TDA Meson Production Cross Section



• Unpolarized exclusive π^0 production cross section:

$$\frac{d^{2}\sigma_{T}}{d\Omega_{\pi}} = |\mathcal{C}^{2}| \frac{1}{Q^{6}} \frac{\Lambda(s, m^{2}, M^{2})}{128 \pi^{2} s(s - M^{2})} \frac{1 + \xi}{\xi} (|\mathcal{I}|^{2} - \frac{\Delta_{T}^{2}}{M^{2}} |\mathcal{I}'|^{2})$$

$$\mathcal{I} = \int \left(2\sum_{\alpha=1}^{7} T_{\alpha} + \sum_{\alpha=8}^{14} T_{\alpha} \right) \qquad \mathcal{I}' = \int \left(2\sum_{\alpha=1}^{7} T_{\alpha}' + \sum_{\alpha=8}^{14} T_{\alpha}' \right)$$

$$\frac{\alpha}{1 - \frac{\omega(s)}{\frac{-\varkappa}{4s}} \frac{-\frac{\omega}{4s}}{\frac{3}{s}} \frac{\omega(s)}{s(s)}} \frac{-\frac{Q_{u}(2\xi)^{2}[(V_{1}^{p\pi^{0}} - A_{1}^{p\pi^{0}})(V^{p} - A^{p}] + 4T_{1}^{p\pi^{0}}T^{p} + 2\frac{\Delta_{T}^{2}}{M^{2}} T_{1}^{\mu^{\alpha}} T_{1}} \frac{-Q_{u}(2\xi)^{2}[(V_{2}^{p\pi^{0}} - A_{2}^{p\pi^{0}})(V^{p} - A^{p}] + 4T_{1}^{p\pi^{0}}T^{p}} \frac{-Q_{u}(2\xi)^{2}[(V_{2}^{p\pi^{0}} - A_{2}^{p\pi^{0}})(V^{p} - A^{p}] + 2T_{1}^{p\pi^{0}}T^{p}} \frac{-Q_{u}(2\xi)^{2}[(V_{2}^{p\pi^{0}} - A_{2}^{p\pi^{0}})(V^{p} - A^{p}) + 2T_{1}^{p\pi^{0}}T^{p}} \frac{-Q_{u}(2\xi)^{2}[(V_{2}^{p\pi^{0}} - A_{2}^{p$$

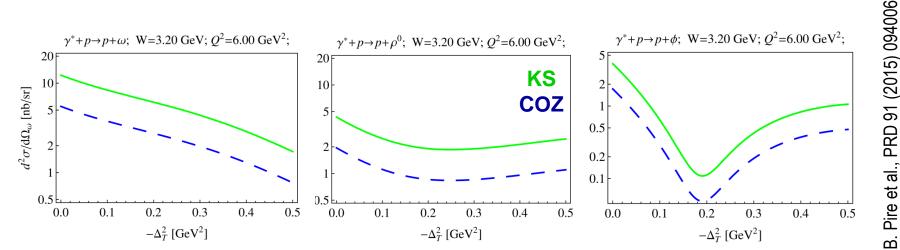
J. P. Lansberg, B. Pire, K. Semenov-Tian-Shansky, L. Szymananovski, Phys. Rev. D 85 (2011) 054021

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TDA Model Predictions for JLab E12–19–006

F π –**12 experiment (E12–19–006)** L/T separations up to Q^2 =8.5 GeV² Spokespersons: D. Gaskell, G.M. Huber, T. Horn

- L/T–Separations over wide kinematic range will allow $\sigma_T \gg \sigma_L$ and $1/Q^8$ scaling predictions to be checked with greater authority
- u-channel φ -electroproduction particularly interesting
 - Sensitive to Strangeness content of nucleon
- Combined analysis of ρ , ω production allows one to disentangle isotopic structure of *VN* TDAs in non–strange sector



At Q²=6.0 GeV², ω predicted to remain dominant (unlike *t*-channel), φ to drop rapidly with -u.

SIMC: Q²–W overlap at high, low ε

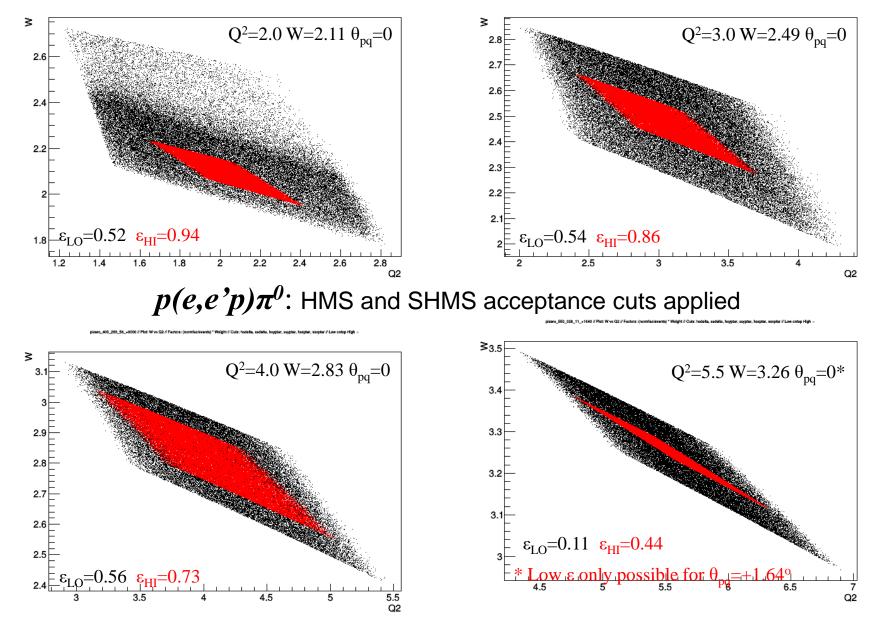


izaro_200_211_52_+0000 // Piot: W vs Q2 // Factors: (normfac/events) * Weight // Cuits: Insdeita, sadaita, huyptar, ssyptar, hospiar, sseptar // Low ontop High =

arth Hu

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pizero_300_249_54_+0000 // Piot: W vs Q2 // Factors: (normfac/events) * Weight // Cuts: hadeita, sadeita, hoyptar, sosptar, hosptar, sosptar // Low ontop High //



π^0 Channel Expected to be Clean

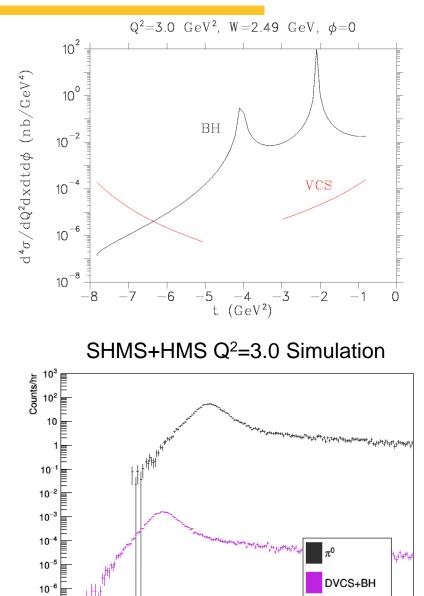
- In comparison to backwardangle ω electroproduction, there is little physics background in π^0 production.
- **Bethe–Heitler process** has no backward-angle peak, and will be negligible.
 - VCS should dominate backward–angle γ production, but is expected to be much smaller than π^0 production.

- BH+VCS simulations based on code by P. Guichon and M. Vanderhaeghen.
- BH calculation is exact.
- VCS calculation makes use of ad-hoc ansatz based on *u*-channel ω data.

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0.02

0.04

0.06

0.08

Mm² GeV²

10⁻⁷ _____

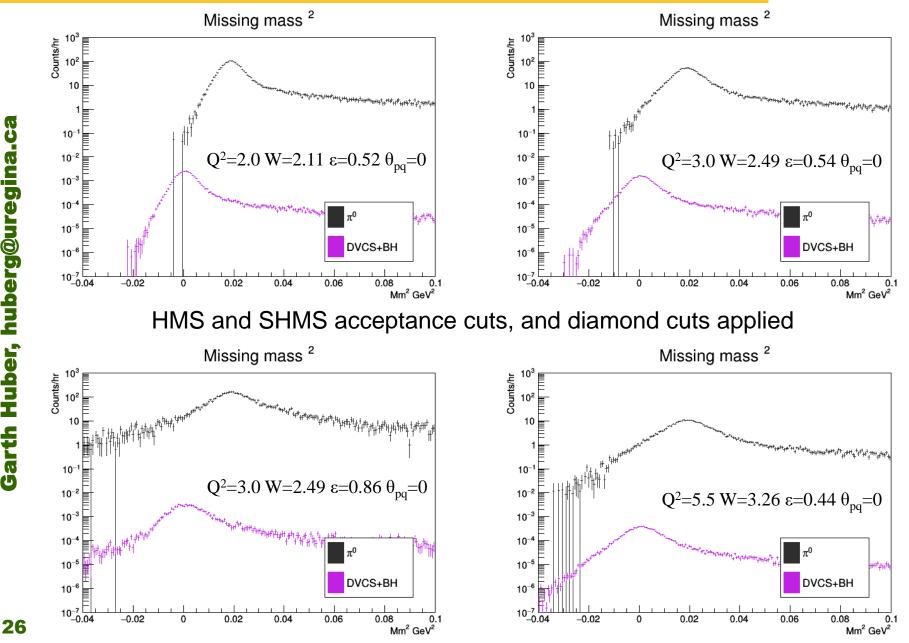
-0.02

0



SIMC: Missing Mass squared

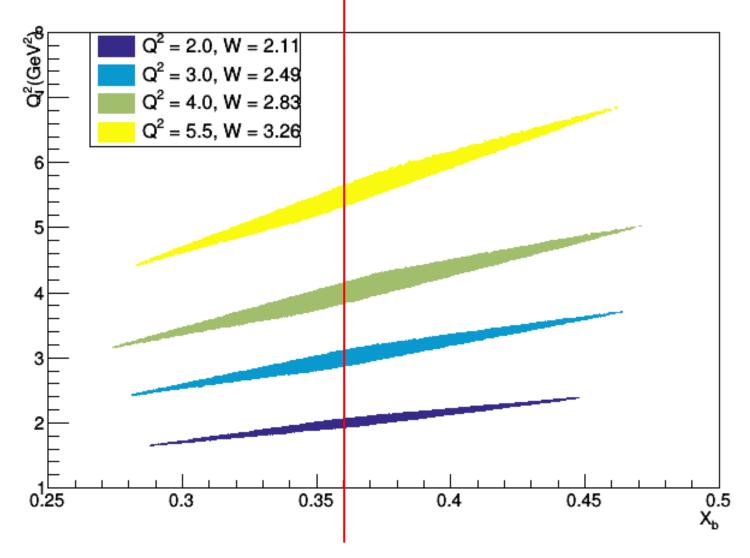




Central Kinematics are x_{Bjorken}=0.36

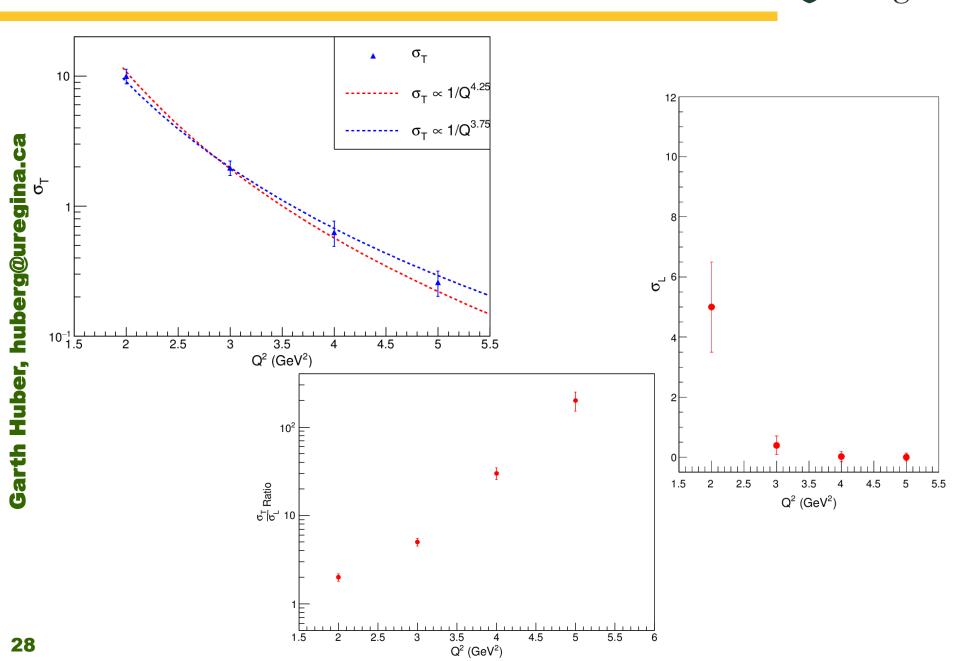


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HMS and SHMS acceptance cuts, and diamond cuts applied

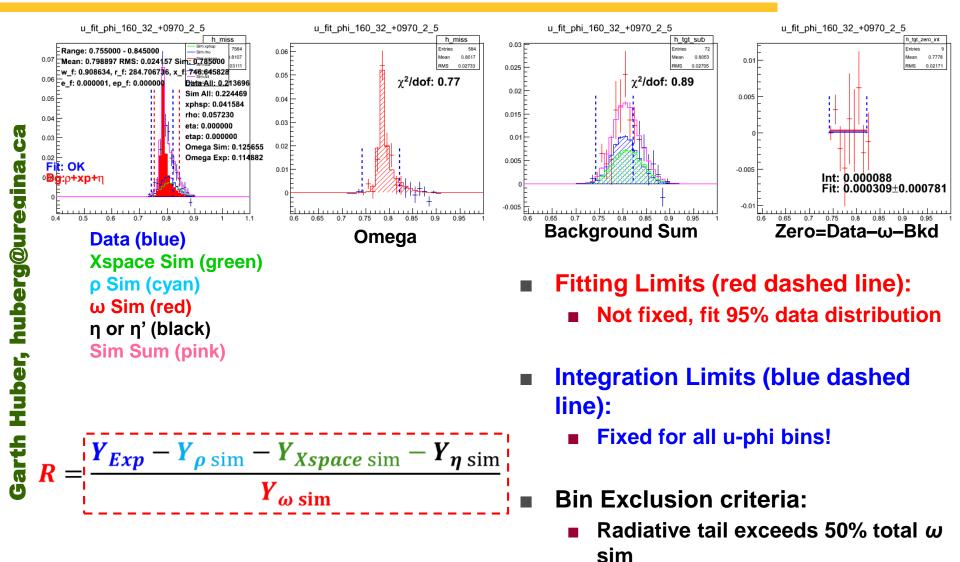
$p(e,e'p)\pi^0 Q^2$ -dependence projections $\operatorname{Versity}_{\text{of Regina}}$



Missing Mass Background Removal



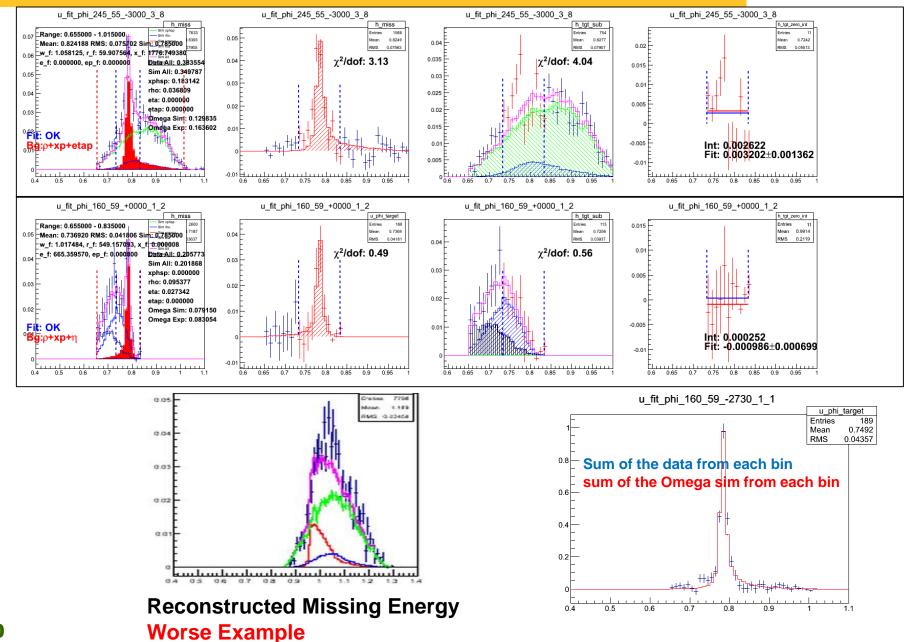
Less that 100 raw counts



29

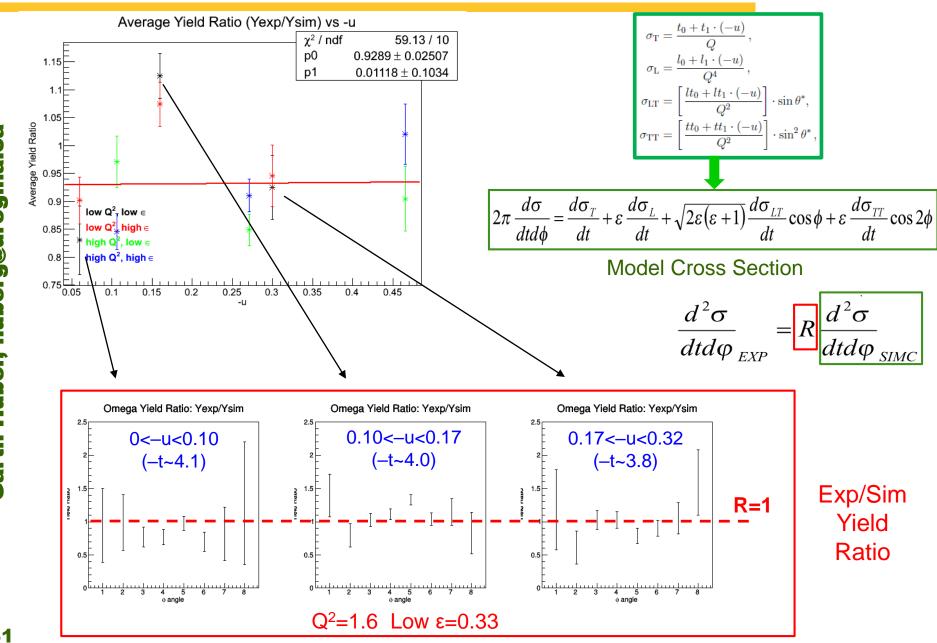
Background Extraction and Check





30

Yield Ratio and Model Cross–Section

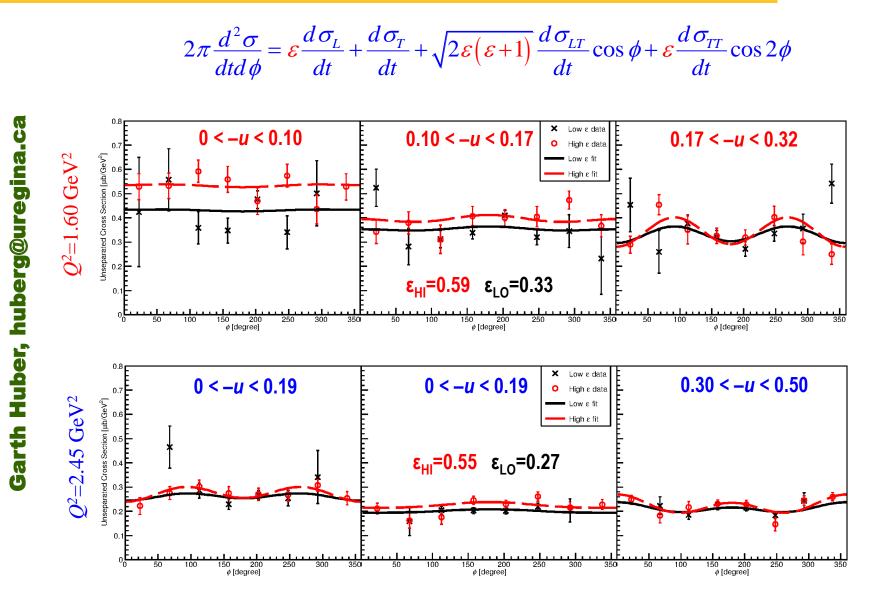


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of Regina

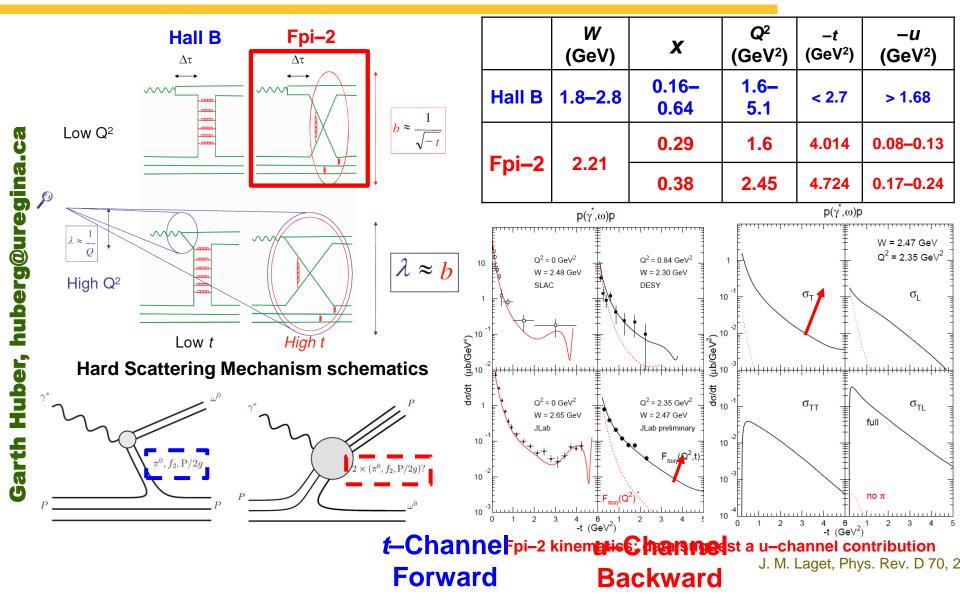
Unseparated Cross Sections





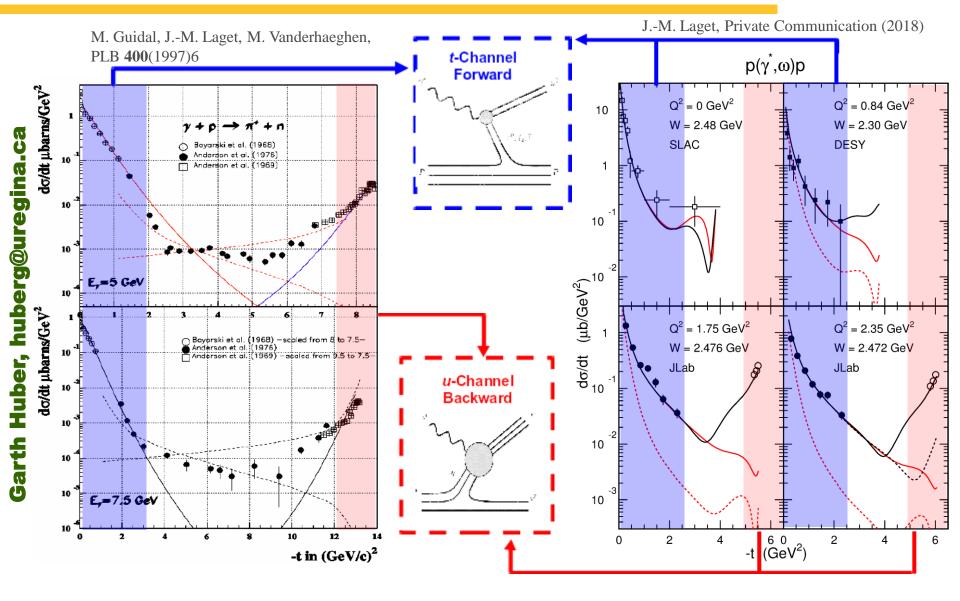
Regge Trajectory Model by J–M Laget





Hadronic Model: Regge Model by JM Laget





Soft structure → **Hard** → **Soft transition!**

Extension to Higher Q²



- 1. Determine if the backward angle peak observed in exclusive ω electroproduction occurs also in other channels, over a broad kinematic range.
- Measure the u-dependence of L/T-separated cross sections, to determine the relevance of Regge-rescattering and TDA mechanisms in JLab kinematics.
- 3. Assuming the backward angle peak is present, as expected, measure the σ_T/σ_L ratio over a wide Q² range for W>2 GeV.
 - Where does $\sigma_T * \sigma_L$, as predicted by TDA formalism?
- 4. Determine the Q²–dependence of σ_T at fixed x_B .
 - Where does $\sigma_T \sim 1/Q^8$ as predicted by TDA formalism?



- Halls B,C 6 GeV data hint at applicability of backward-angle factorization mechanism as early as Q²=2.5 GeV²
- If this interpretation is correct, it can be confirmed by *u*-channel CT measurements such as A(e,e'p)π⁰
- The observation of CT in A(e,e'p)π⁰ by Q2=14 GeV2, when it is absent in A(e,e'p), would be a considerable achievement
- Other Considerations:
 - In the quasi-elastic process, the observed fast nucleon is part of the nuclear target. In the TDA picture, the fast proton comes from the partons of the original proton target.
 - It is not obvious that the fast proton from the *u*-channel interaction is the same as the original construct of the "original" valence quarks, thus would it really inherit all of the properties from the original proton?
 - Is the proton from the fast proton quasi-elastic process the same as the fast u-channel fast proton, and could this proton experience color transparency?