

Backward Angle Omega Meson Electroproduction

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University
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**NSERC
CRSNG**

Outline

- Motivation, purpose and technique
- Theory
- Experiment
- Analysis
- Results and Outlook

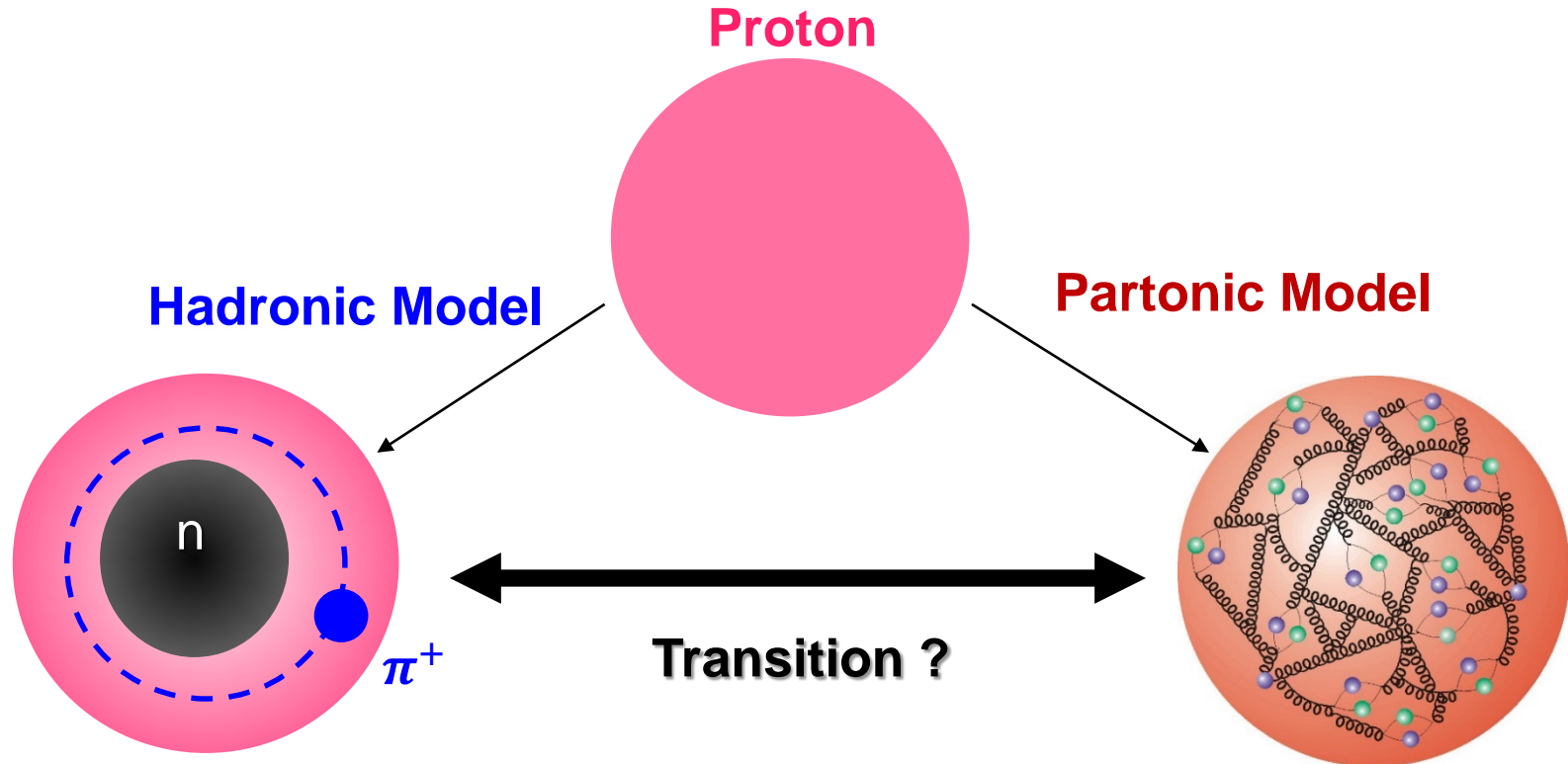
Motivation

■ Motivation

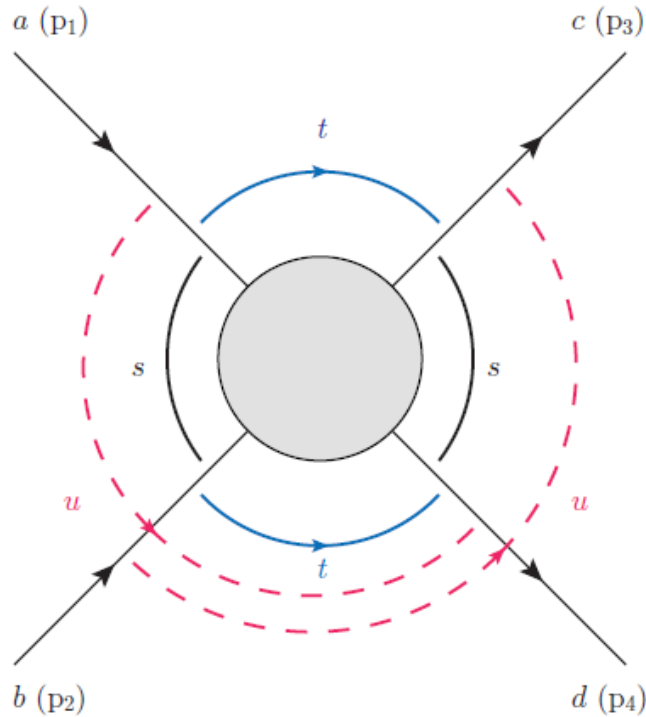
- Probing dynamic property of the proton structure
 - Dependent on the properties of the probe
- Studying the **transition** of QCD

■ Objective

- Establishing a new approach
 - Backward-angle (u -channel) observables
 - LT separation



Mandelstam variables (s, t, u -Channels)



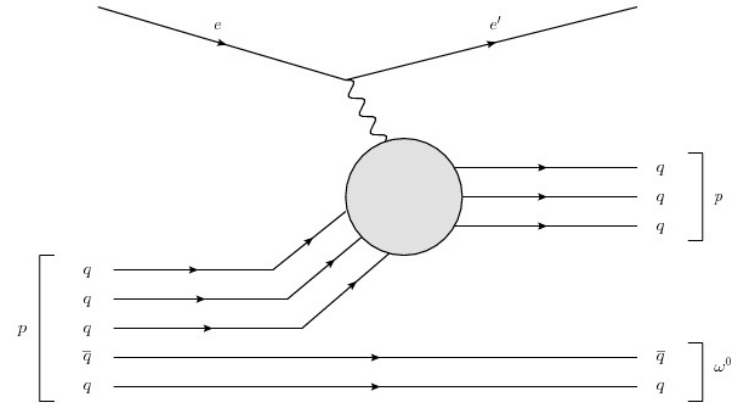
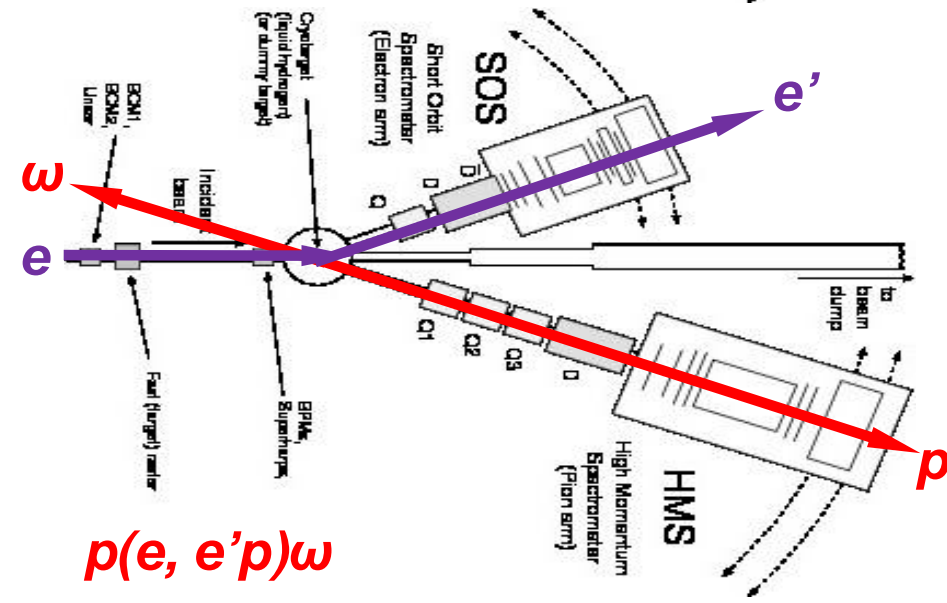
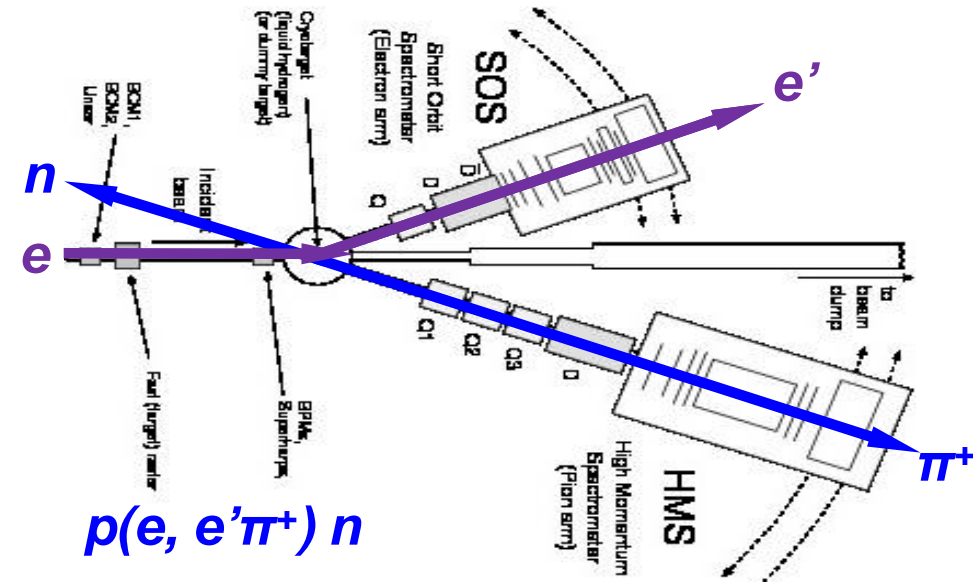
$$s = (p_1 + p_2)^2 = (p_3 + p_4)^2$$

$$t = (p_1 - p_3)^2 = (p_2 - p_4)^2$$

$$u = (p_1 - p_4)^2 = (p_2 - p_3)^2$$

- s : invariant mass of the system
- t : Four-momentum-transfer squared between **target before and after interaction.**
- u : Four-momentum-transfer squared between **virtual photon before interaction and target after interaction**
- **t -channel: $-t \sim 0$, after interaction**
 - **Target: stationary,**
 - **Meson: forward**
 - **Measure of how forward could the meson go.**
- **u -channel: $-u \sim 0$, after interaction**
 - **Target: forward**
 - **Meson: stationary**
 - **Measure of how backward could the meson go**

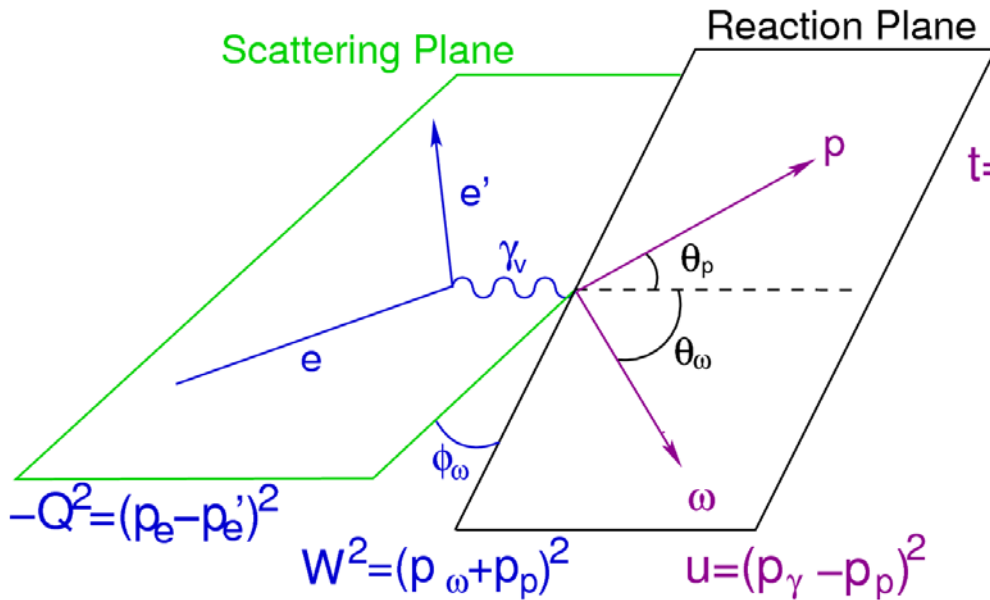
t -Channel π vs u -Channel ω^0 Production



Mark Strikman: A proton being knocked out of a proton process

- HMS along the q -vector (p_{γ^*})
 - p_{π^+} is parallel to p_{γ^*} (Forward)
 - p_{ω} is anti-parallel to p_{γ^*} (Backward)
- Exclusive channel!
 - $p(e, e' p)\omega$
 - We don't detect any part of decayed ω
 - Contain physics background
- Full L/T separation on this u -channel process
- One of the last Hall C 6 GeV analysis

Rosenbluth Separation



Virtual-photon polarization:

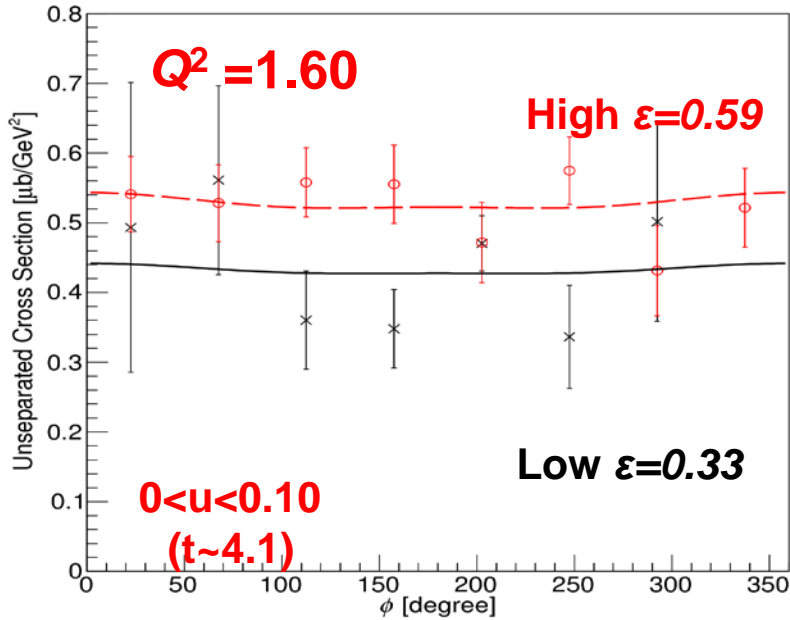
$$\epsilon = \left(1 + 2 \frac{(E_e - E_{e'})^2 + Q^2}{Q^2} \tan^2 \frac{\theta_{e'}}{2} \right)^{-1}$$

$$2\pi \frac{d\sigma}{dt d\phi} = \epsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

- Rosenbluth Separation requires

- **Separate measurements at different ϵ** (virtual photon polarization)
- All Lorentz invariant physics quantities: **Q^2 , W , t , u , remain constant**
- Beam energy, scattered e angle and virtual photon angle will change as the result, thus **event rates are dramatically different**

Separation Method



$$2\pi \frac{d\sigma}{dtd\phi} = \epsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

■ L/T separation

- Requires detailed comparison at **high** and low epsilon value
- High and low epsilon runs involved

■ Simple L/T separation

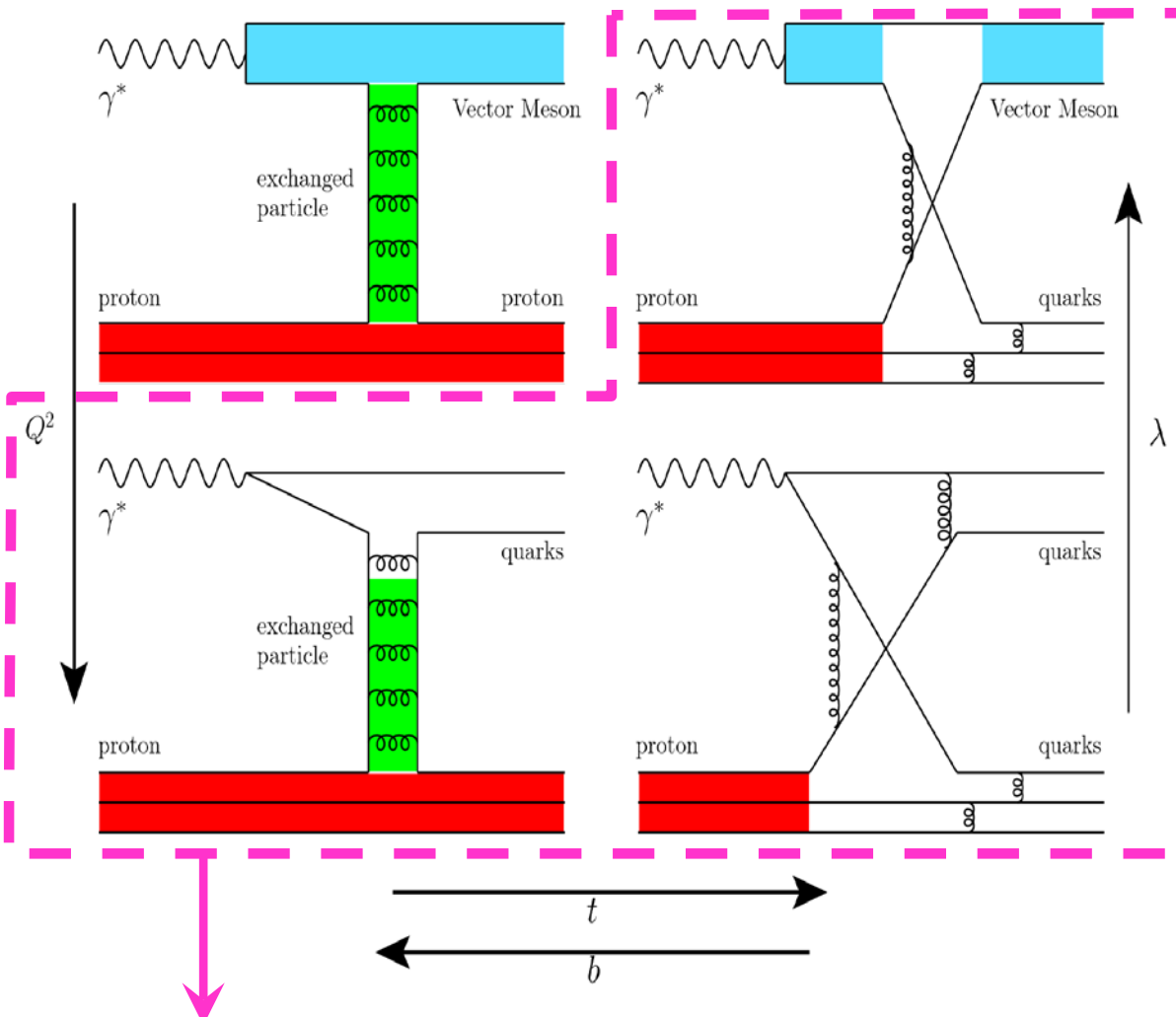
- $\sigma_{total} = \sigma_T + \epsilon \sigma_L$
 - σ_T : difference
 - σ_L : offset
 - σ_{LT} and σ_{TT} : modulation

■ Experimental Kinematics

- W is fixed
- Two Q^2 settings
- High and low epsilon runs for each Q^2 setting

T_{inc} MeV	P_{SOS} MeV	θ_e^* deg	ϵ	θ_q deg	θ_{pq} deg	θ_{HMS} deg	P_p MeV/c	P_{HMS} MeV/c	x	$-u$ GeV ²	$-t$ GeV ²
			$Q_{nominal}^2 = 1.60 \text{ GeV}^2$		$W_{nominal} = 2.21 \text{ GeV}$						
3772	785.79	43.09	0.328	9.53	+1.0 +3.0	10.53 12.53	2936.79 2913.20	2927.2	0.2855	0.087 0.129	4.025 3.983
4702	1715.79	25.73	0.593	13.28	0.0 -2.7 +3.0	13.28 10.58 16.28	2939.53 2917.79 2913.15	2927.2	0.2855	0.082 0.121 0.129	4.030 3.991 3.982
			$Q_{nominal}^2 = 2.45 \text{ GeV}^2$		$W_{nominal} = 2.21 \text{ GeV}$						
4210	770.83	51.48	0.270	9.19	1.4 3.0	10.59 12.14	3355.82 3324.12	3331.7	0.3796	0.184 0.241	4.778 4.721
5248	1808.83	29.43	0.554	13.61	0.0 3.0 -3.0	13.61 16.61 10.61	3363.86 3324.28 3324.49	3331.7	0.3796	0.169 0.241 0.240	4.793 4.721 4.722

Hadronic Model: Transition (Evolution) of Proton Structure

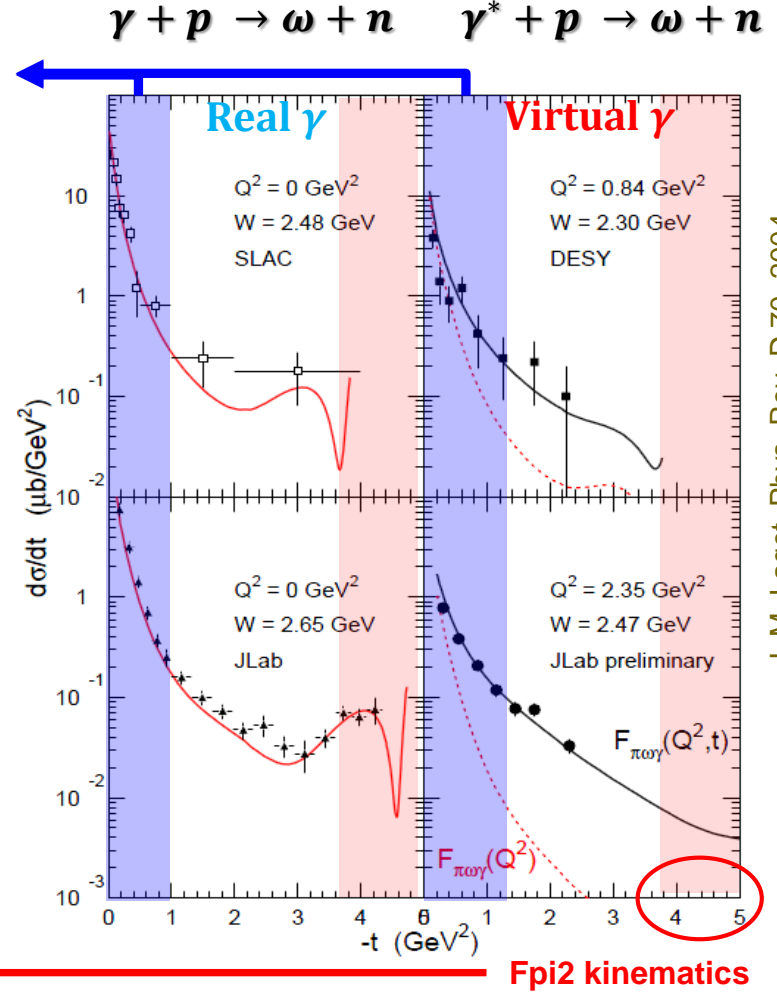
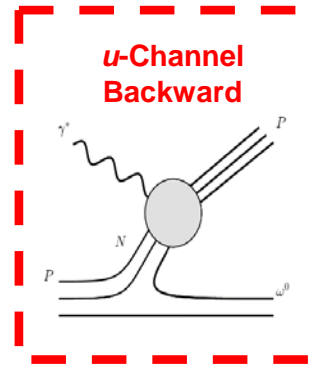
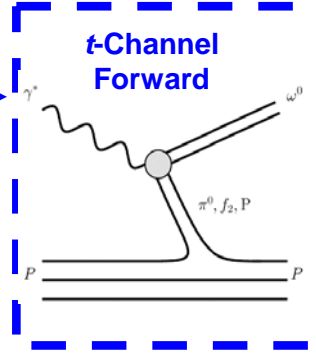
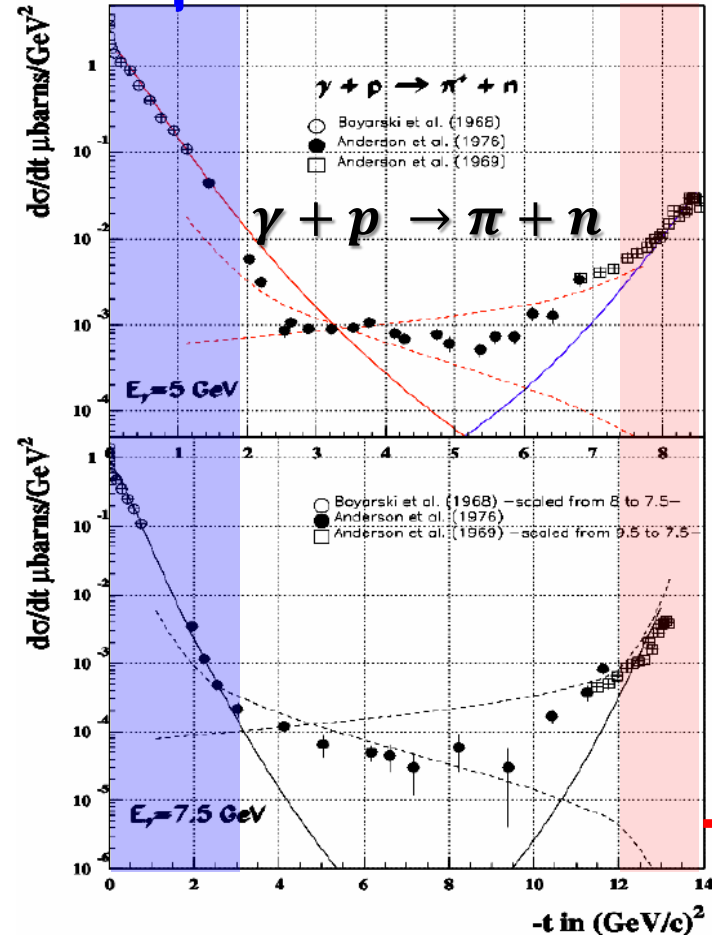


Evolution of the Proton Structure

- Physics observables
 - In t , $W(s)$, Q^2 , x
- x Evolution:
 - 0.2-0.3 valence quark distribution is pronounced
- W Evolution:
 - Above the resonance region
- Q^2 Evolution
 - Wavelength of the probe
- t Evolution
 - Impact parameter
- What about u ?

Hadronic Model: Regge Trajectory Model by JM Laget

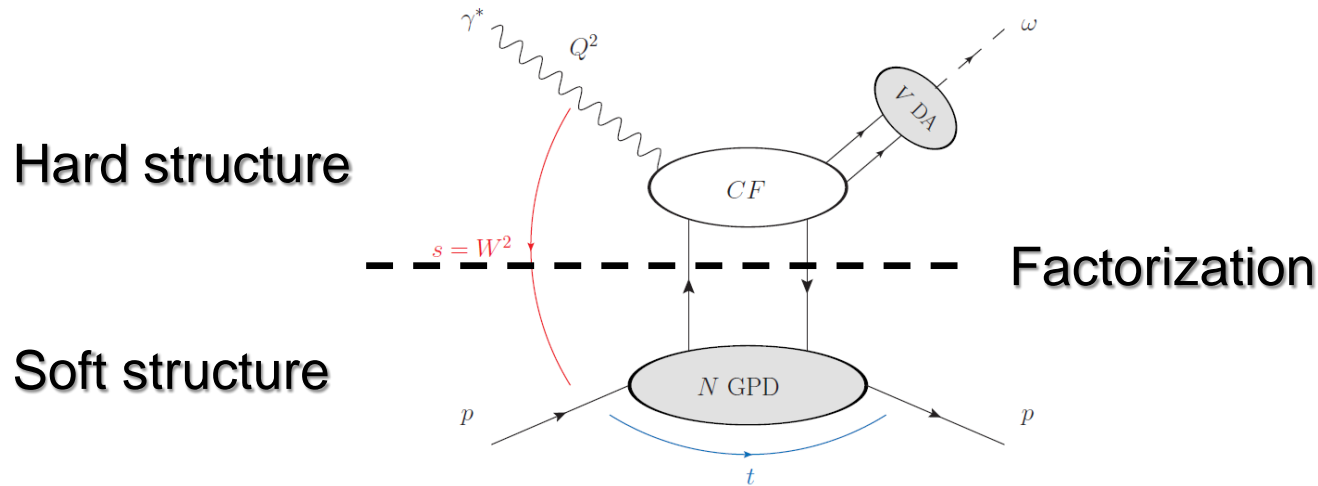
M. Guidal, J.-M. Laget, and M. Vanderhaeghen.
*Physics Letters B*400(1):6–11, 1997.



J. M. Laget, Phys. Rev. D 70, 2004

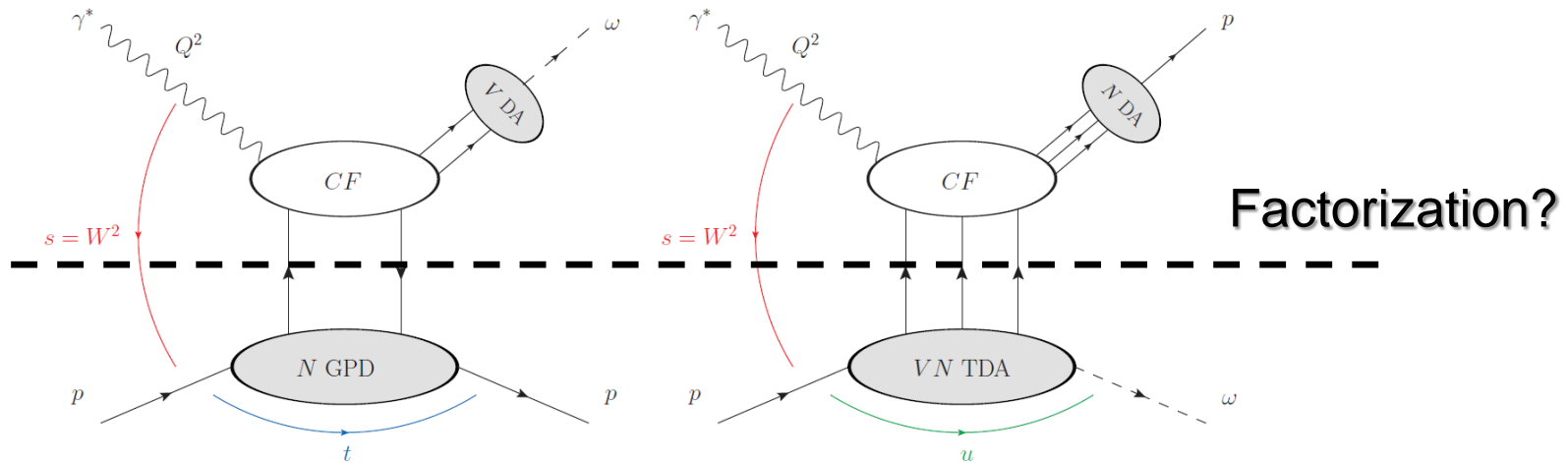
Soft structure -> Hard -> Soft transition !

Partonic Model: GPD and Factorization



- Generalized parton distribution (GPD)
 - Full spatial distribution of partons (quarks and gluons)
 - No known experimental access
 - Can be studied through factorization scheme at **sufficiently high Q^2**
 - Deep Virtual Compton Scattering (**DVCS**)
 - Deep Virtual Meson Production (**DVMP**)

Parton Based Model: TDA

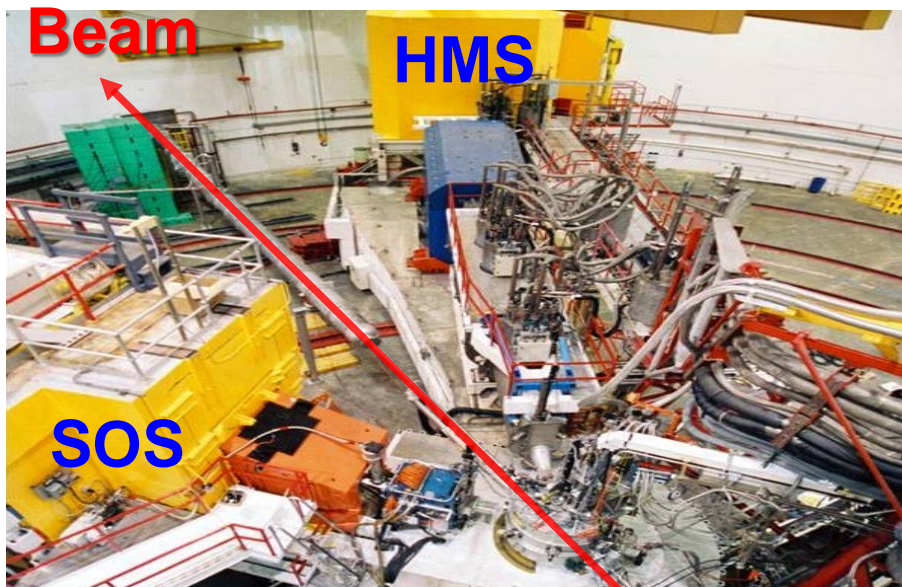


- **Nucleon to Meson Transition Distribution Amplitude (TDA)**
 - **Backward angle analog of GPD. Translate from $-t$ space to $-u$. Translate V DA to N DA**
 - **No consensus on the TDA factorization regime**
 - If t is impact parameter, **physical meaning of u is unclear.**

- **Interaction of Interest: u -channel pseudoscalar meson and vector meson productions**

- **Two Predictions of TDA:** (B. Pire, K. Semenov, L. Szymanowski, Phys. Rev. D, **91**, 094006 (2015))
 - The **dominance of the transverse polarization** of the virtual photon resulting in the suppression of the longitudinal cross section by at least $1/Q^2$: $\sigma_T > \sigma_L$.
 - The Characteristic $1/Q^8$ -scaling behaviour of the σ_T for a fixed Bjorken x .

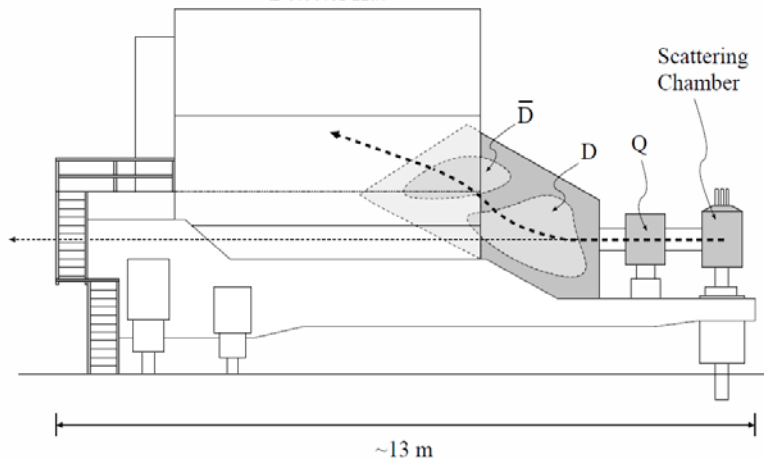
Experimental Details



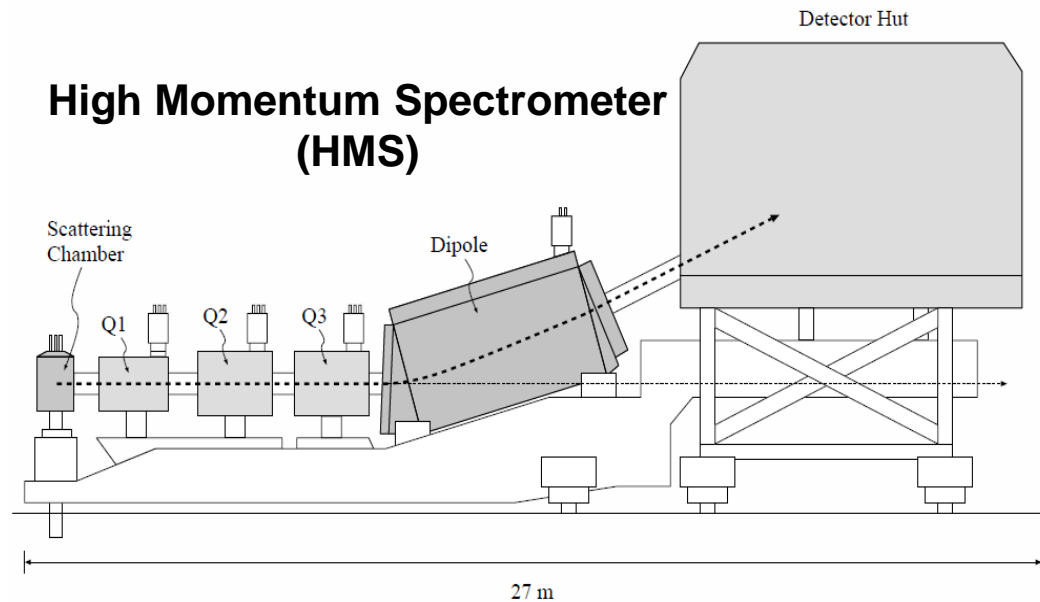
- **HMS (QQQD)**
 - **Angle Acceptance:** 6msr
 - **Momentum:** 0.5-7.5 GeV/c
 - **Momentum Acceptance:** +-9%
 - **Angular, Position Resolution:** 1mr and 1mm
- **SOS (QDDbar)**
 - **Angle Acceptance:** 9msr
 - **Momentum:** 0.1-1.8 GeV/c
 - **Momentum Acceptance:** +-20%

High Momentum Spectrometer (SOS)

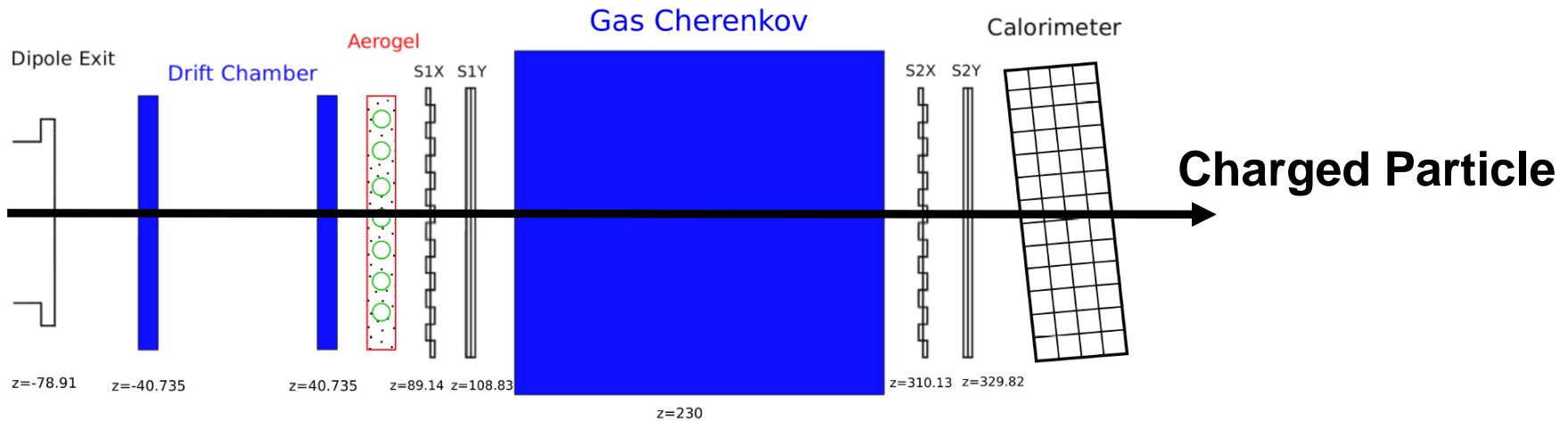
Detector Hut



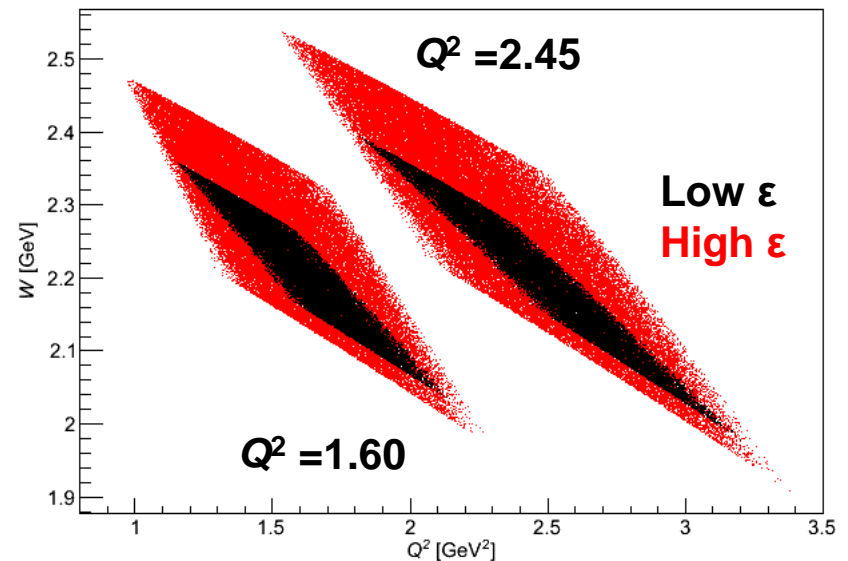
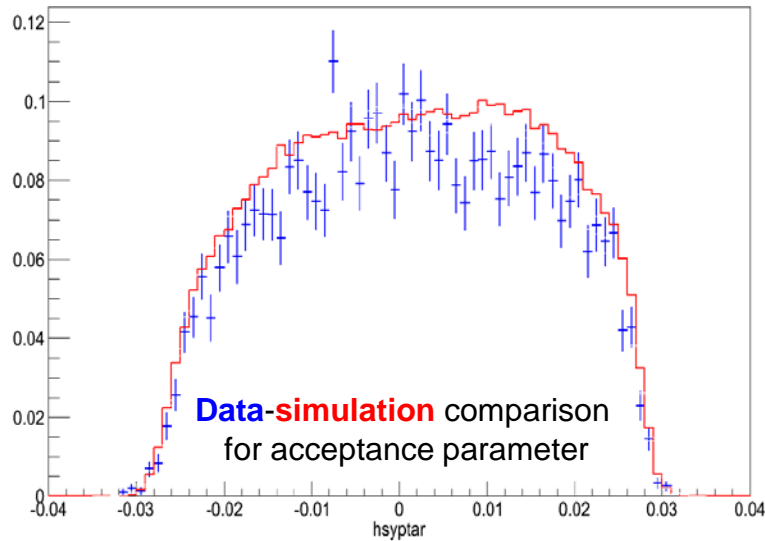
High Momentum Spectrometer (HMS)



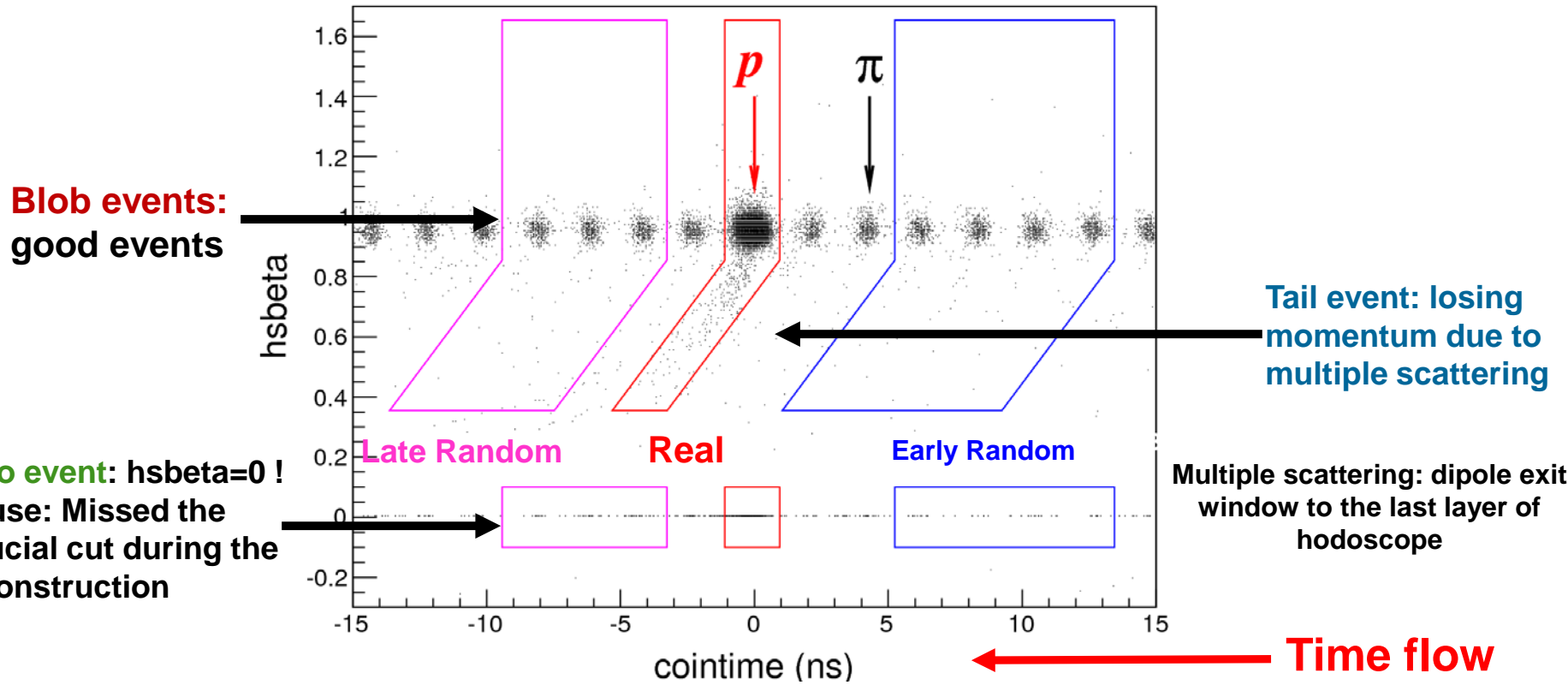
Experimental Setup and Acceptance



HMS detector (focal plane) layout, SOS is very similar
Trigger: 3/4 planes of Hodoscopes



Coincidence Subtraction

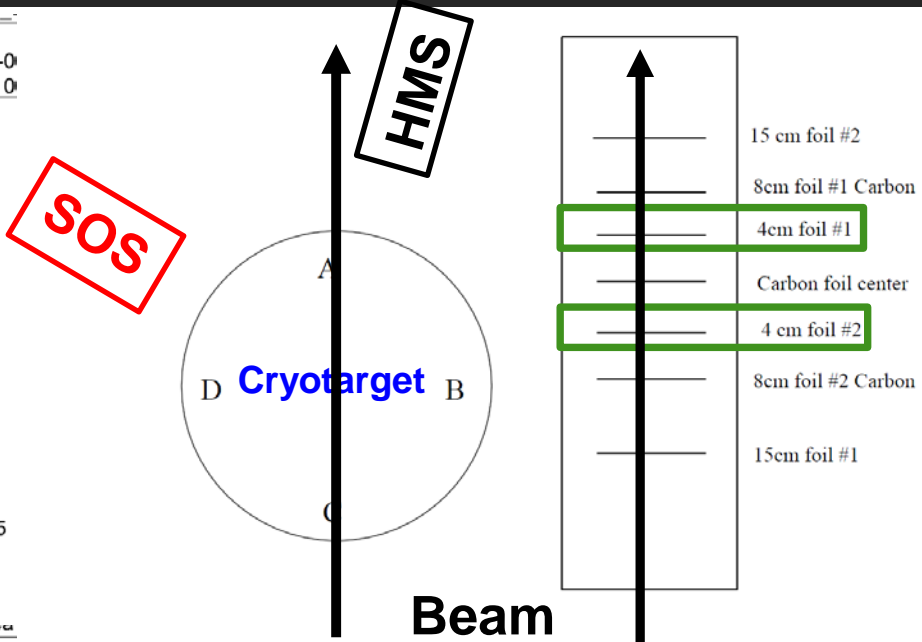
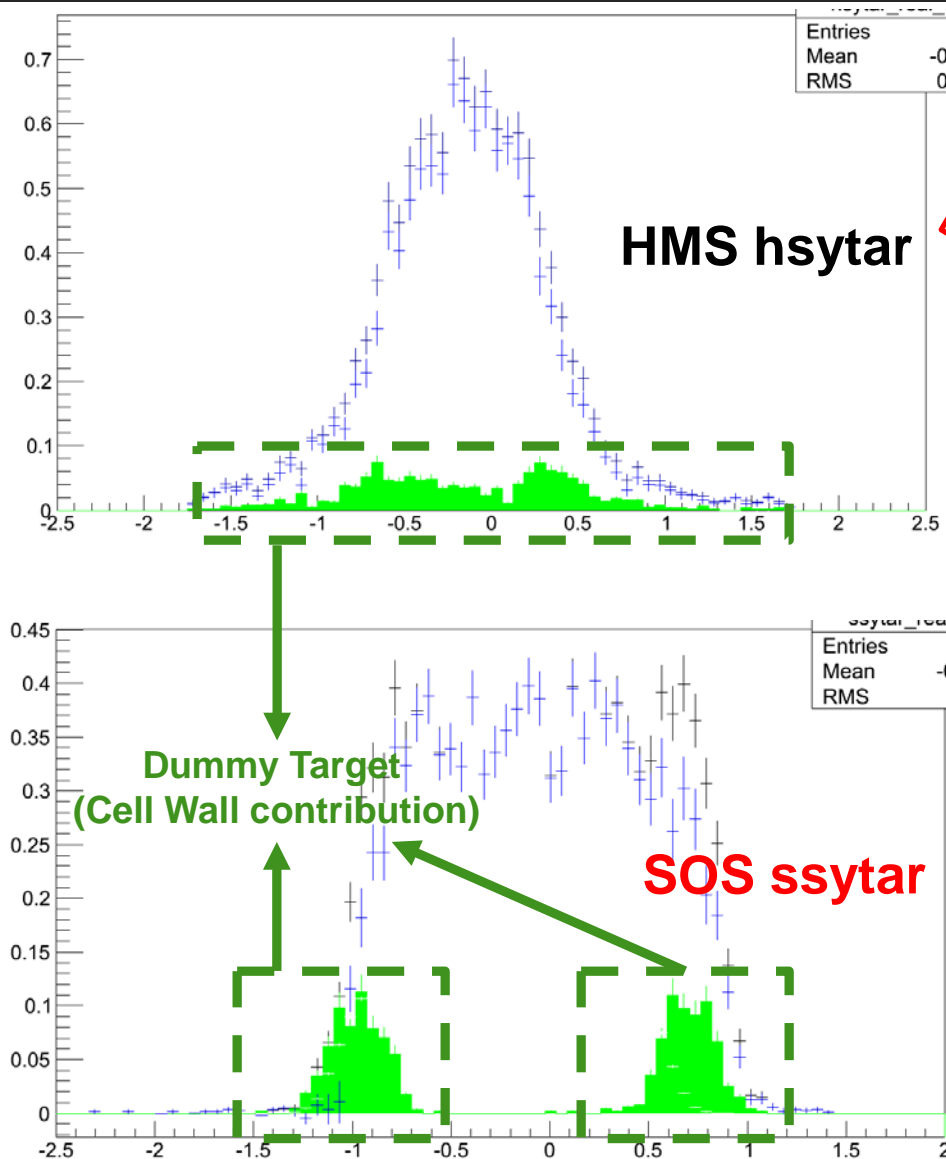


■ Random subtraction:

$$\text{Coincidence proton} = \text{Real Events} - \left(\frac{\text{Late Random Events} + \text{Early Random Events}}{7} \right)$$

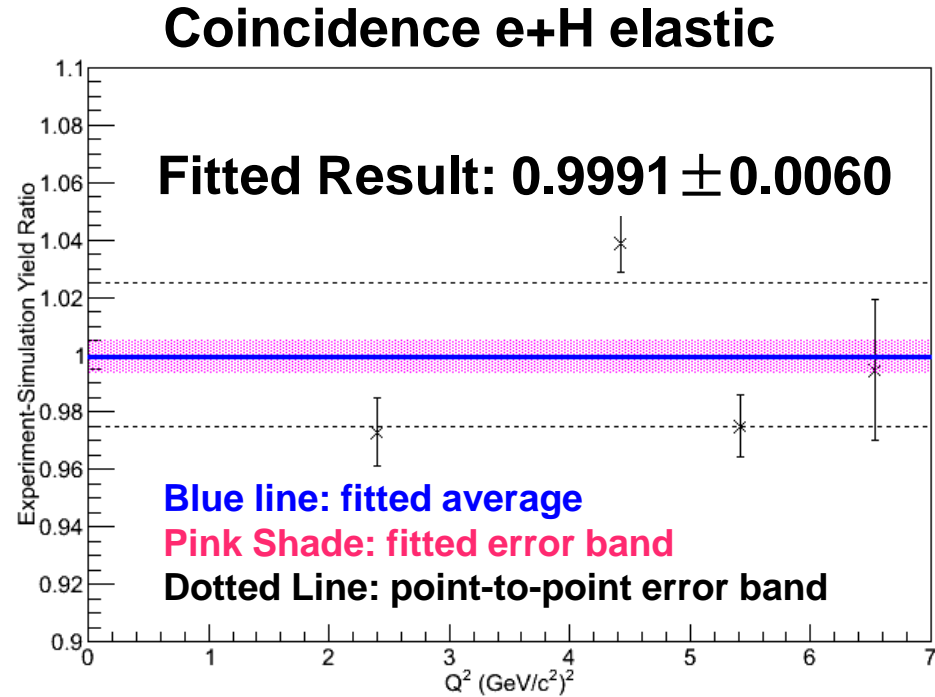
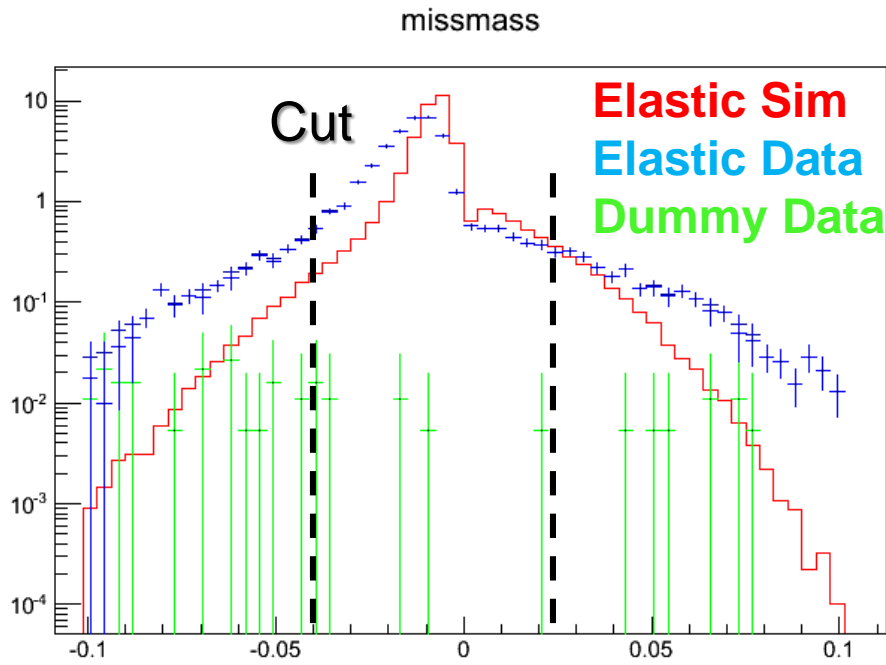
■ Missing proton due to scattering, absorption: ~7%

Dummy Subtraction



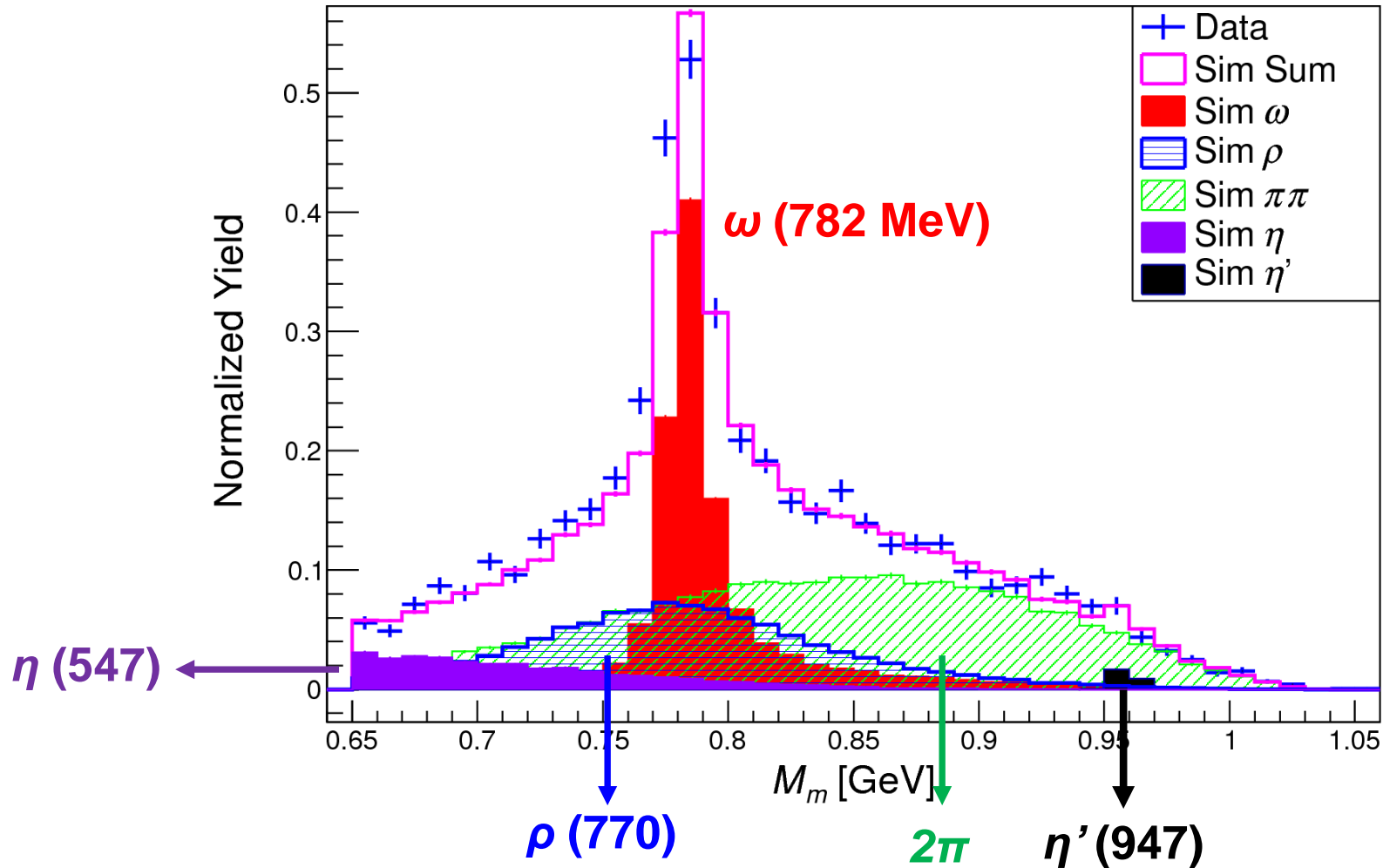
- **Cryotarget**
 - Tuna can shaped
 - With thin Al cell wall
- **Dummy Target**
 - 4cm apart Al sheets
 - Dummy target distribution is corrected for the real/dummy target thickness difference before subtracted from the real proton events

Analysis: e+H Elastic Cross-Section



- Extracted cross section is consistent with Bosted, AMT (Arrington, Melnitchouk, Tjon Phys. Rev. C 76, 035205 (2007)) and Brash empirical e-p elastic cross section parameters.
- $\pm 2.0\%$ (point to point) error from Heep will be included to the final Omega analysis systematics

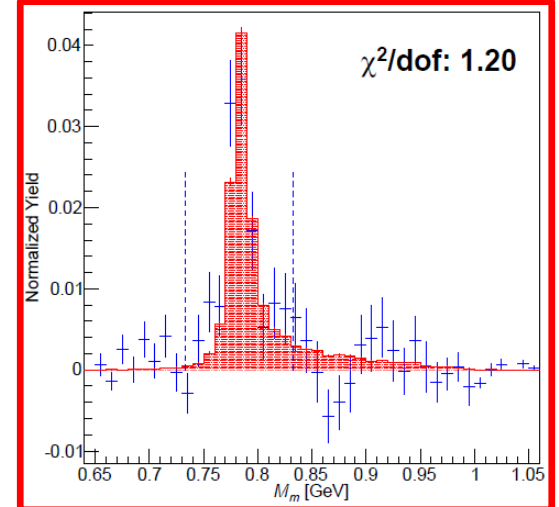
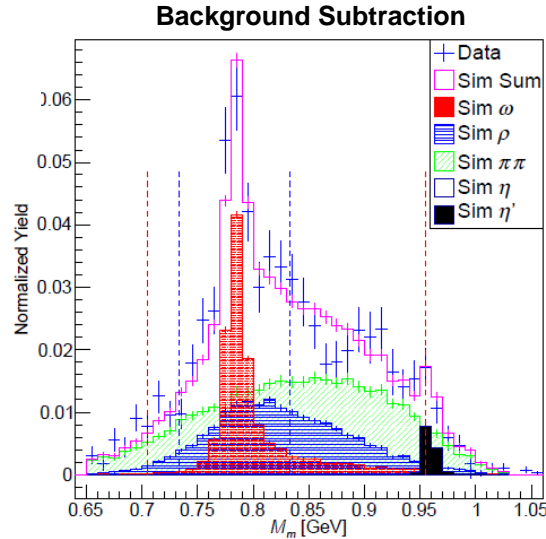
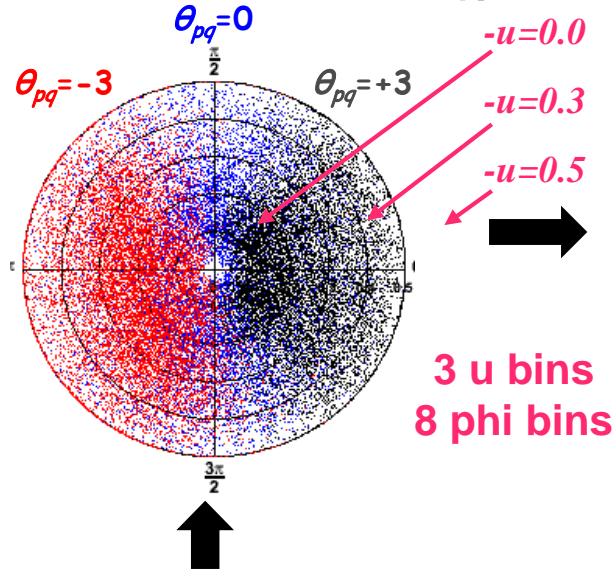
Physics Background Subtraction



HERMES Empirical parameterization with Soding factor **Width from PDG with Ae^{-Bu} dependence**

Iterative Procedure (Recipe) to A Full LT Separation

Improve ϕ coverage by taking data at multiple HMS angles, $-3^\circ < \theta_{pq} < +3^\circ$.

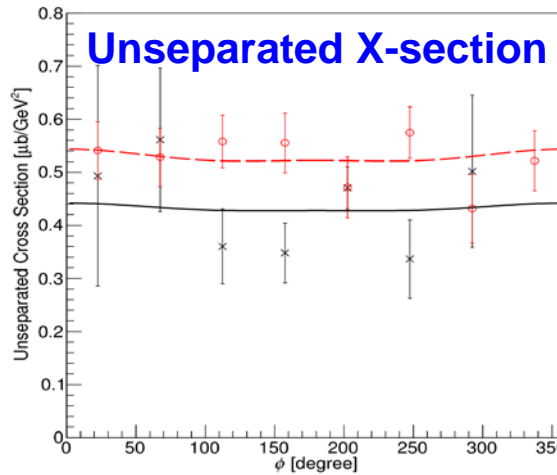


$$R = \frac{Y_{Exp} - Y_{\rho \text{ sim}} - Y_{Xspace \text{ sim}} - Y_{\eta \text{ sim}}}{Y_{\omega \text{ sim}}}$$

Combine ratios for settings together, propagating errors accordingly.

$$\frac{d^2\sigma}{dt d\phi}_{EXP} = R \frac{d^2\sigma}{dt d\phi}_{SIMC}$$

Empirical Model

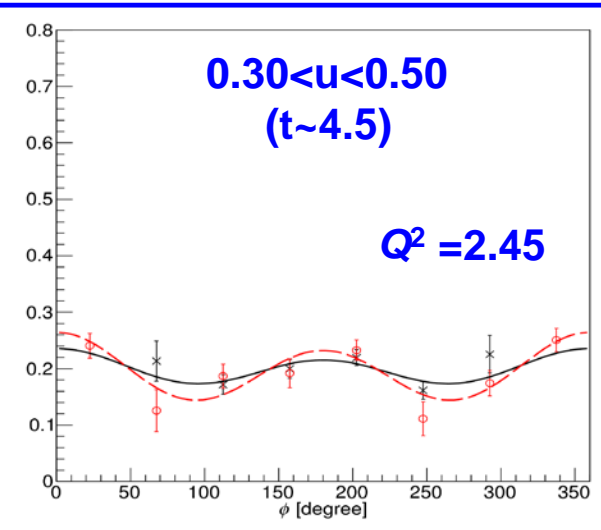
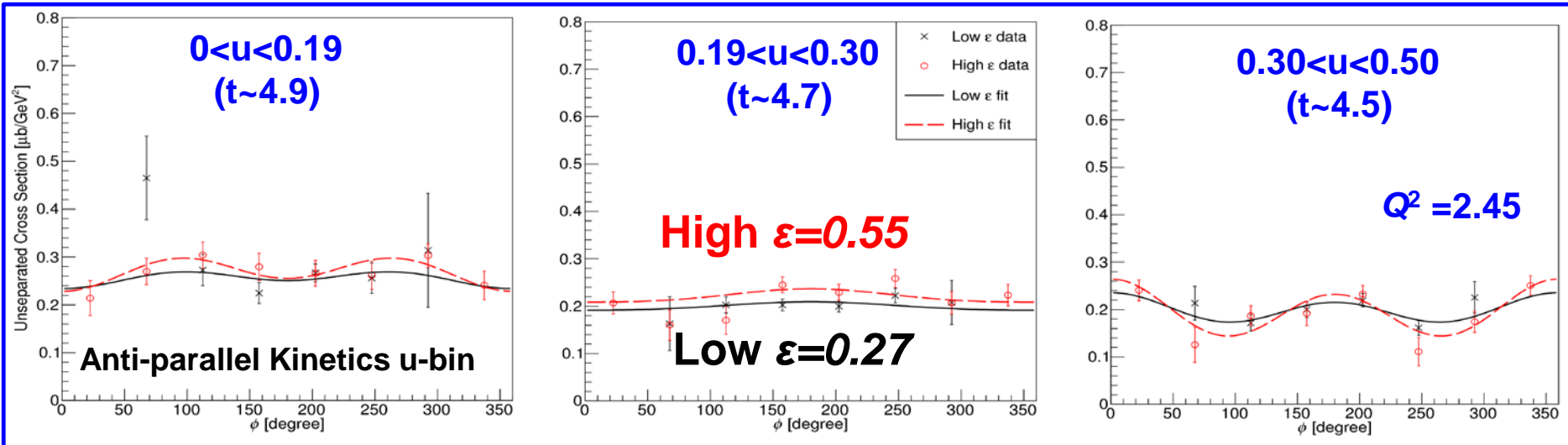
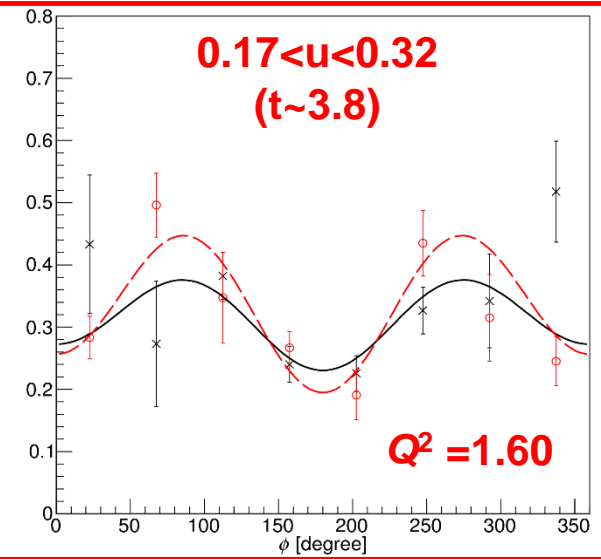
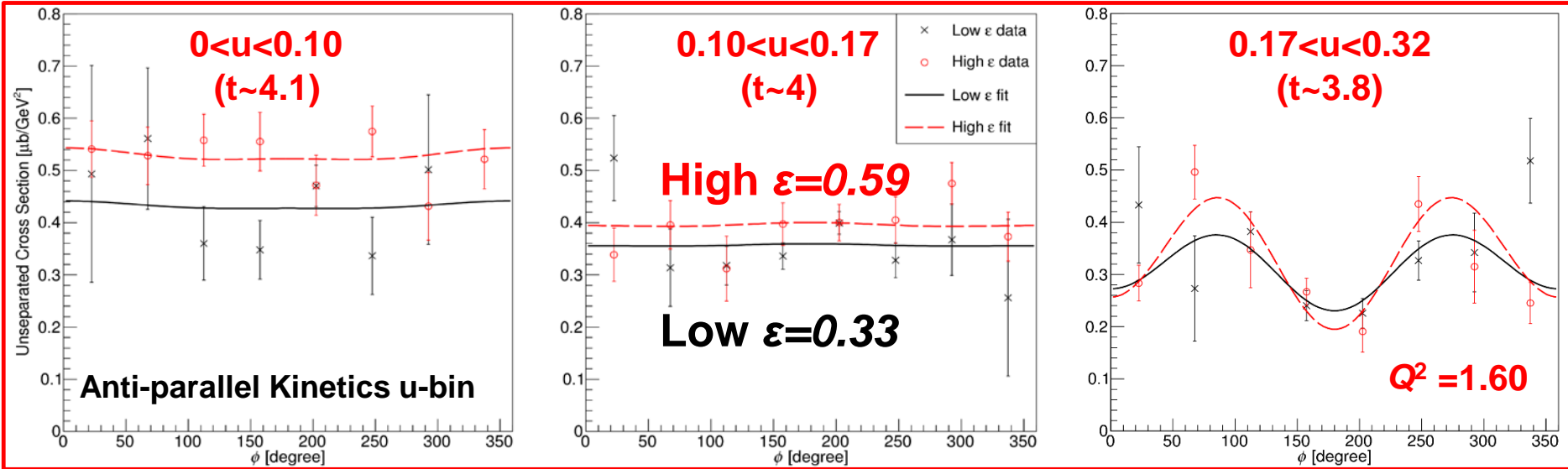


Extract T, L, LT, TT via simultaneous fit

$$2\pi \frac{d\sigma}{dt d\phi} = \frac{d\sigma_T}{dt} + \varepsilon \frac{d\sigma_L}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

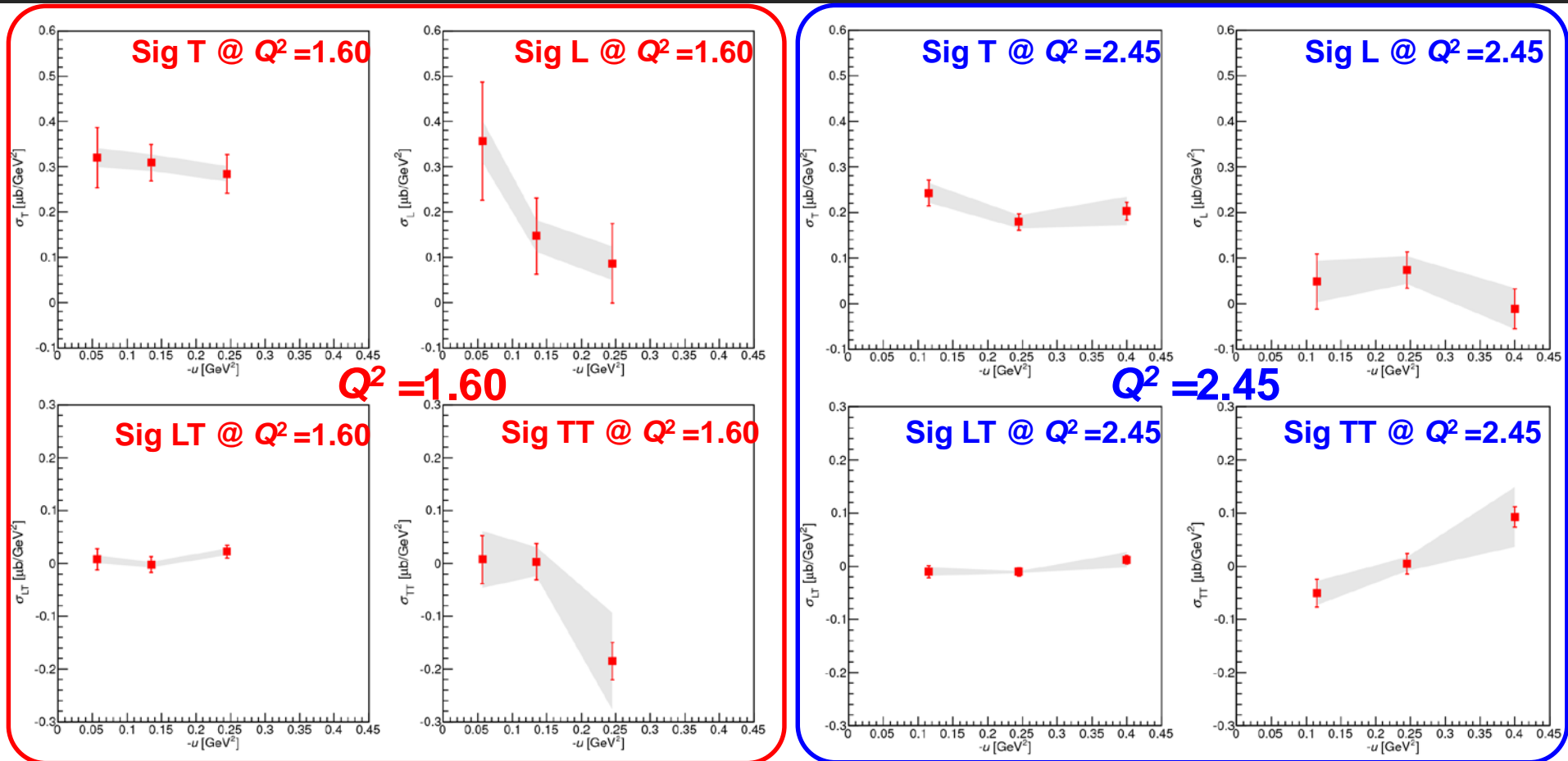
Unseparated Cross Section (Money Plot)

$$2\pi \frac{d\sigma}{dt d\phi} = \frac{d\sigma_T}{dt} + \varepsilon \frac{d\sigma_L}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$



Separated Cross Section

$$\frac{d\sigma}{dt} \text{ VS } -U$$



Observations:

- SigT fall slow, SigL fall faster
- SigLT is small, Sig TT has sign flip for different Q^2 values

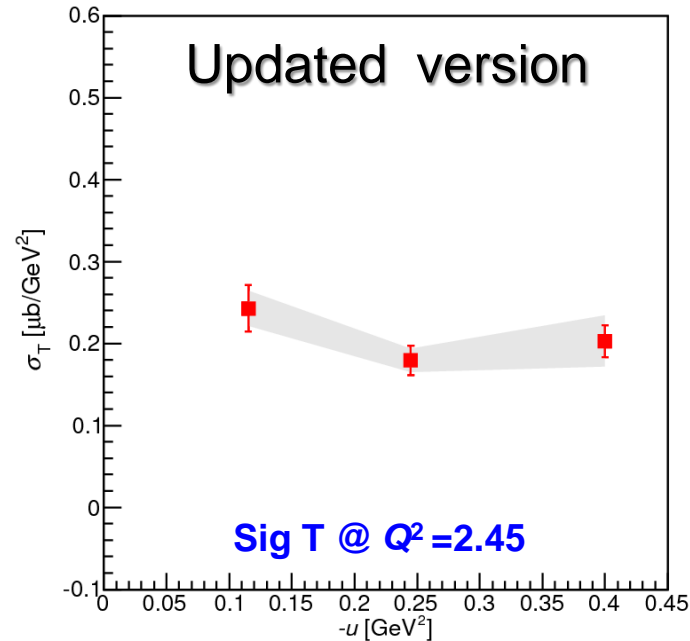
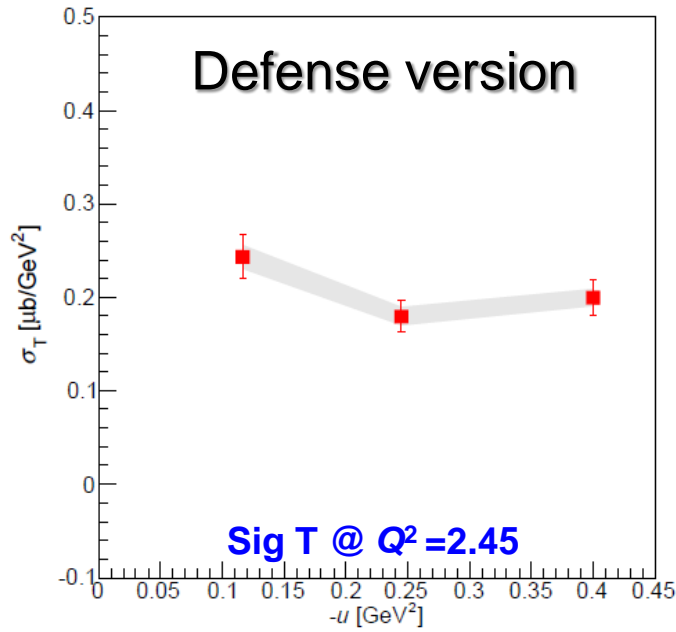
Uncertainties

Correction	Uncorrelated (Pt-to-Pt) (%)	ϵ uncorr. u corr. (%)	Correlated (scale) (%)	Section
HMS Cherenkov			0.02	Sec. 3.6.3
HMS Aerogel			0.04	Sec. 5.3.7
SOS Calorimeter			0.17	Sec. 3.6.4
SOS Cherenkov			0.02	Sec. 3.6.3
HMS beta	0.4			Sec. 5.1.2
HMS Tracking		0.4	1.0	Sec. 5.3.3
SOS Tracking		0.2	0.5	Sec. 5.3.3
HMS Trigger		0.1		Sec. 3.7
SOS Trigger		0.1		Sec. 3.7
Target Thickness		0.3	1.0	Secs. 3.5.2, 5.3.5
CPU LT		0.2		Sec. 5.3.2.2
Electronic LT		0.1		Sec. 5.3.2.1
Coincidence Blocking			0.1	Sec. 5.3.6
$d\theta$	0.1	0.7-1.1		Ref. [3]
dE_{Beam}	0.1	0.2-0.3		Ref. [3]
dp_e	0.1	0.1-0.3		Ref. [3]
$d\theta_p$	0.1	0.2-0.3		Ref. [3]
PID		0.2		Sec. 5.1.1
Beam Charge		0.3	0.5	Sec. 3.4
Radiative Correction		0.3	1.5	Sec. 4.1.4
Acceptance	1.0	0.6	1.0	Sec. 3.8
Proton Interaction			0.7	Sec. 5.3.9
Background Fitting Limit	2.0	0.8	0.8	Secs. 6.5.3, 6.10.2
ω Integration Limit	1.7	1.0	0.3	Secs. 6.6, 6.10.2
Model Dependence	0.7			Secs. 6.2.1, 6.10.2
Total	2.9	1.7-2.0	2.6	

- Unseparated σ
 - Statistical
 - Systematic Error
 - Uncorrelated Error
 - ϵ uncorrelated u correlated
 - Scale error

- Model dependent Error to the separated (Scale error)
 - Parameterization
 - ϕ limits
 - u limits (small contribution)

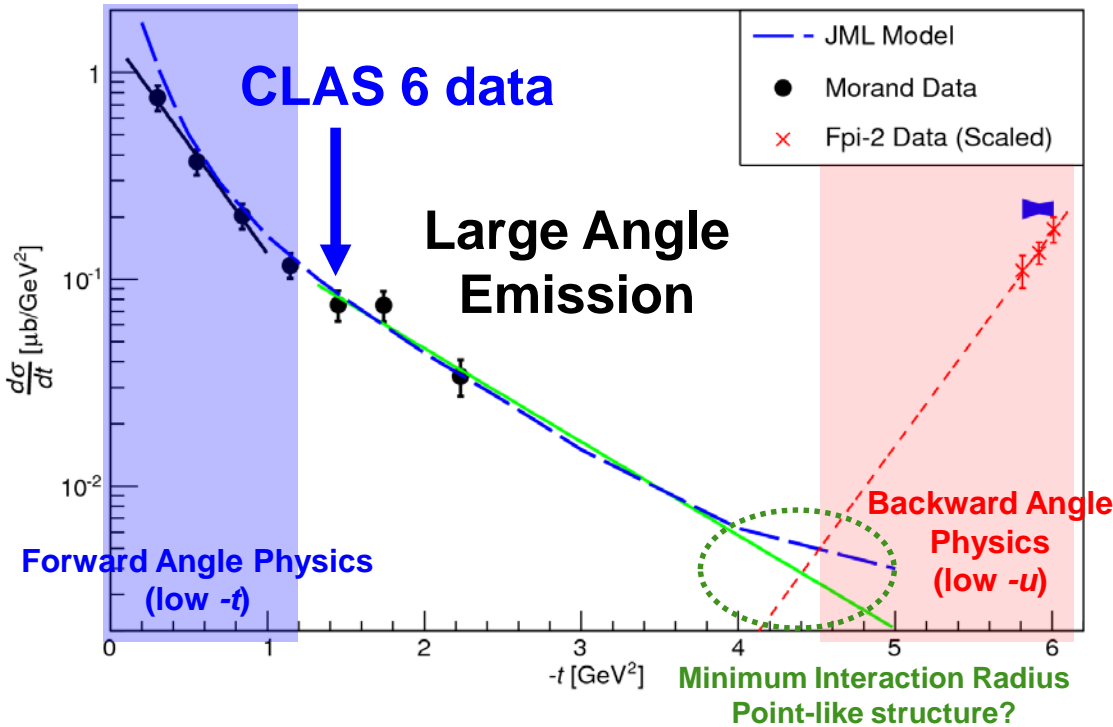
Updated Uncertainties since the Thesis



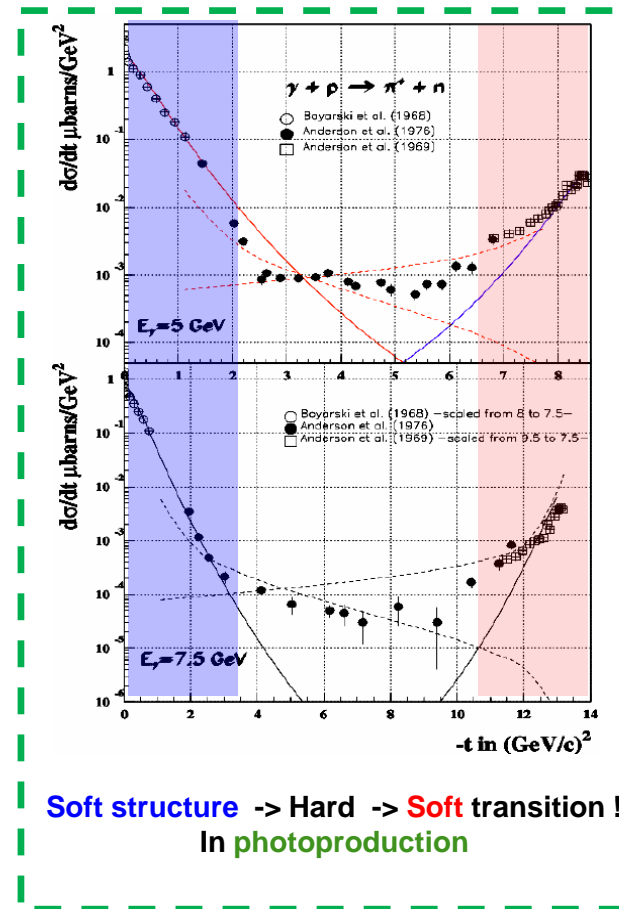
- Fitting Error is now used as the Statistical Error
- New method used for computation the scale error
- Sig_LT and Sig_TT now have scale error band

Hadronic Model: Backward Angle Omega Electroproduction Peak !

$$\gamma^* + p \rightarrow p + \omega, W = 2.47 \text{ GeV}, Q^2 = 2.35 \text{ GeV}^2$$



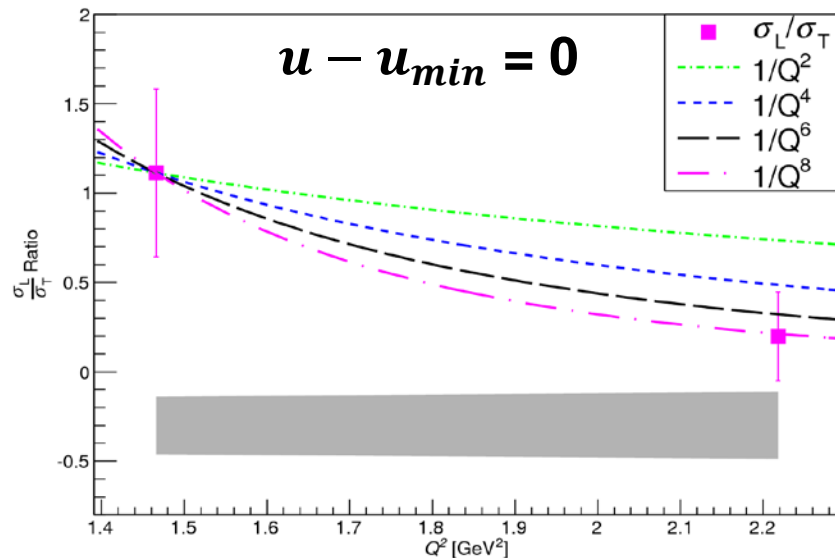
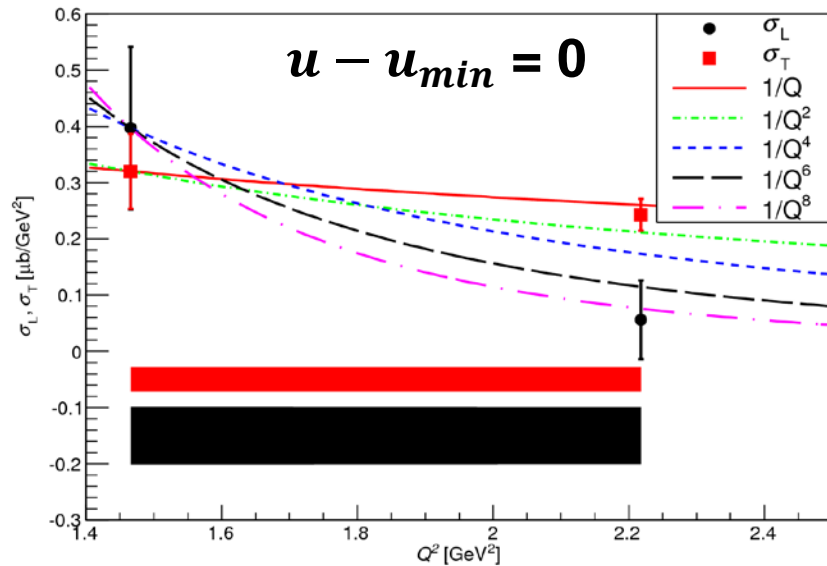
Soft structure \rightarrow **Hard** \rightarrow **Soft transition !**
First time in electroproduction



Soft structure \rightarrow **Hard** \rightarrow **Soft transition !**
In photoproduction

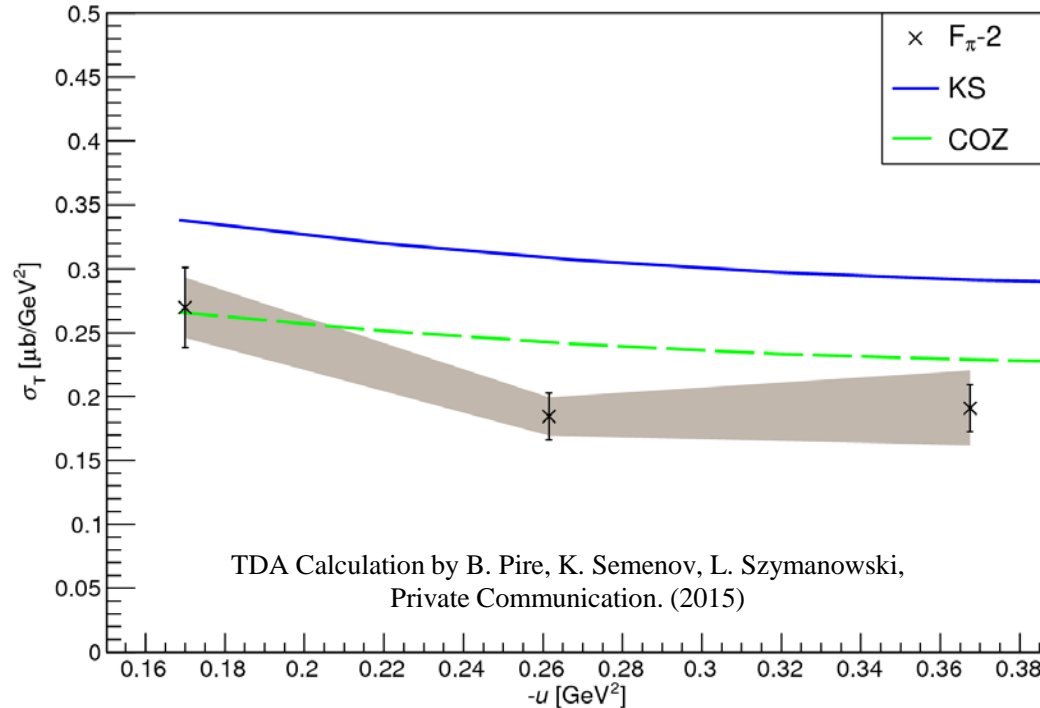
- **First observation for the backward ω electroproduction peak!**
- **Calls for the resurrection of the backward angle study through Regge based model (JML, etc.)**

Scaling of σ_L , σ_T and σ_L/σ_T Ratio



- σ_L drops expected $\sim 1/Q^8$
 - Close to expectation
- σ_T is almost constant !
- Dominance of σ_T observed at higher $Q^2 = 2.45$, confirms the TDA prediction

Partonic Model: TDA Prediction (Private Communication)



- Optimal Q^2 range for TDA: $>10 \text{ GeV}^2$
- TDA prediction has impressive agreement with data at $Q^2 = 2.45 \text{ GeV}^2$
- Studying the effectiveness of JML model and TDA model is equivalent to studying the evolution of the proton structure

Conclusion

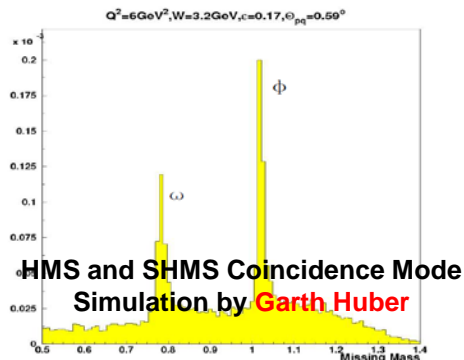
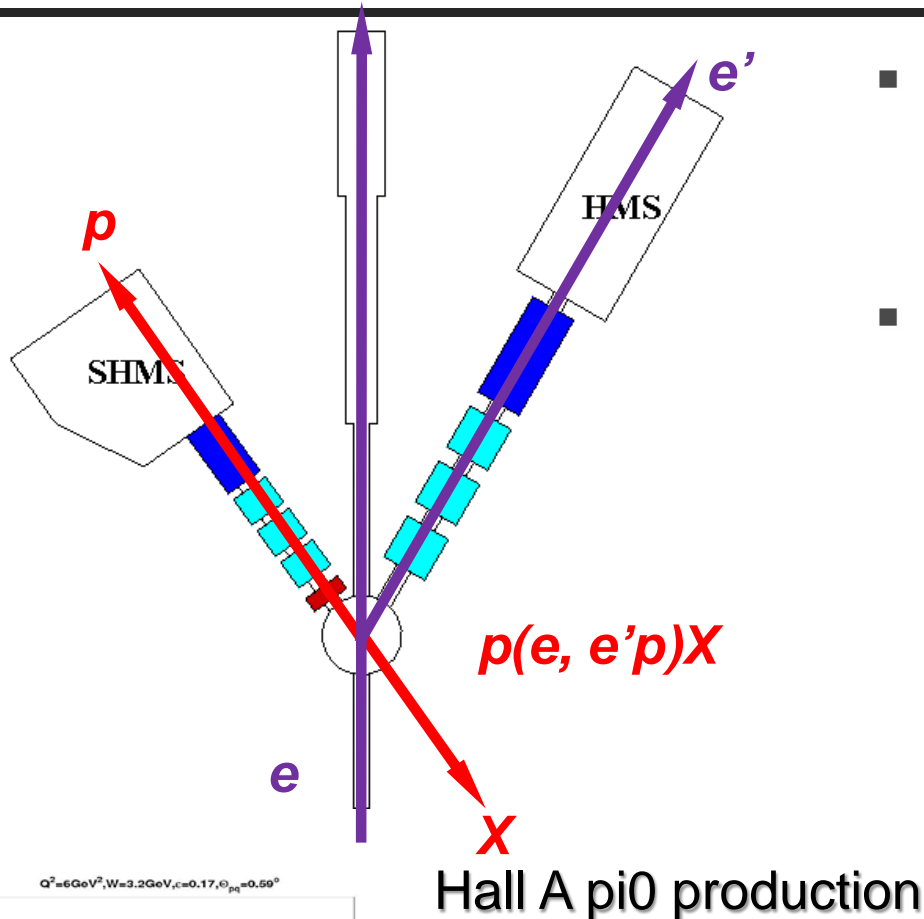
- u -channel omega electroproduction peak observed for the first time
- σ_T has $\sim 1/Q$ dependence, where σ_L has $\sim 1/Q^8$ dependence. Dominance of σ_T over σ_L observed at $Q^2 = 2.45 \text{ GeV}^2$
- At **$Q^2 = 2.45 \text{ GeV}^2$** , TDA prediction agrees with data !

Message to the world and thank you

- **Studying the model effectiveness in both Regge Based Model and TDA is the studying the QCD transition**
- **Established a new experimental access to the previously accessible kinematics**
- **Abstracted the theory framework that can be used to study the previously ignored backward angle process**
- **Final release of the result calls for more studies on backward angle physics, particularly among the junior physicist.**

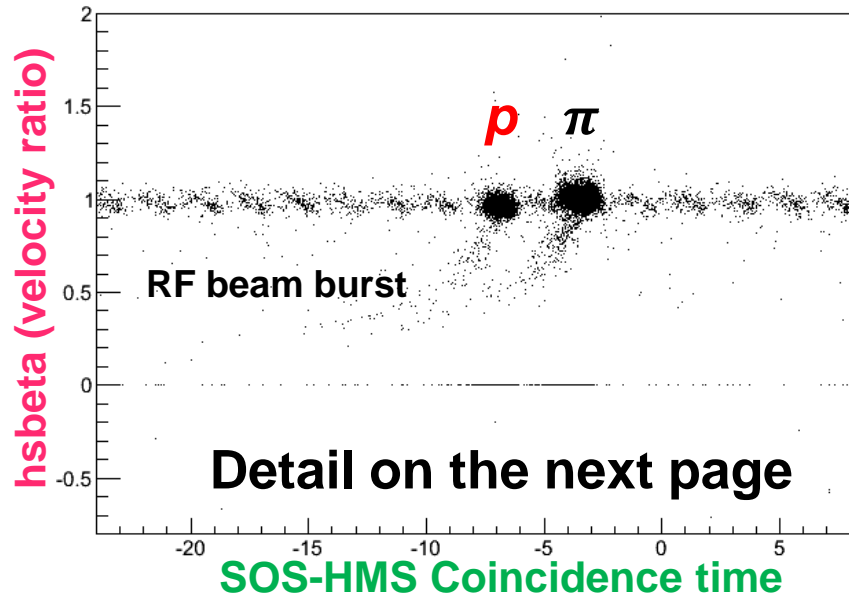
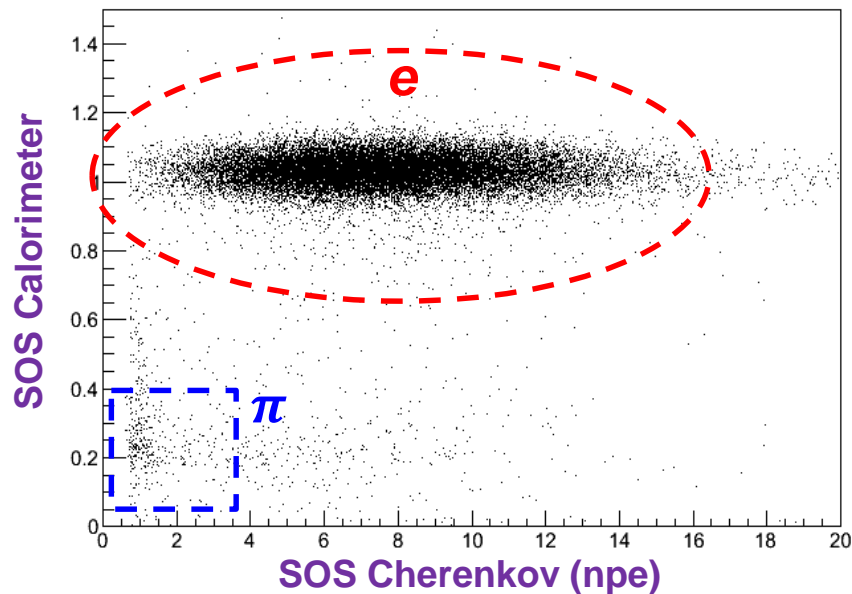
Backup

Future Backward Meson Production Opportunities

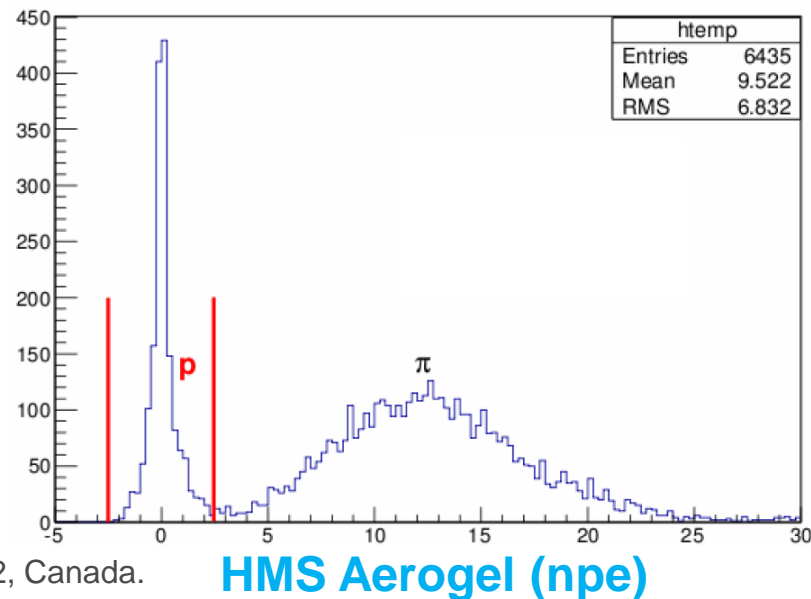


- **6 GeV data mining**
 - Pion transparency experiment (E92-110)
 - 2 GeV and 4.7 GeV (poor statistics)
- **Upcoming 12 GeV experiment**
 - Fpi-12 experiment (E12-06-101):
 - $\eta, \eta', \omega, \phi(s\bar{s}), \rho$
 - $\omega, \phi(s\bar{s})$ production ratio would yield valuable information.
 - Large Emission Experiment at CLAS: E12-12-007
 - $\phi(s\bar{s})$
 - Potential LOI (2018): **Backward π^0** production at Hall C.
- Backward-angle program with Panda @ GSI

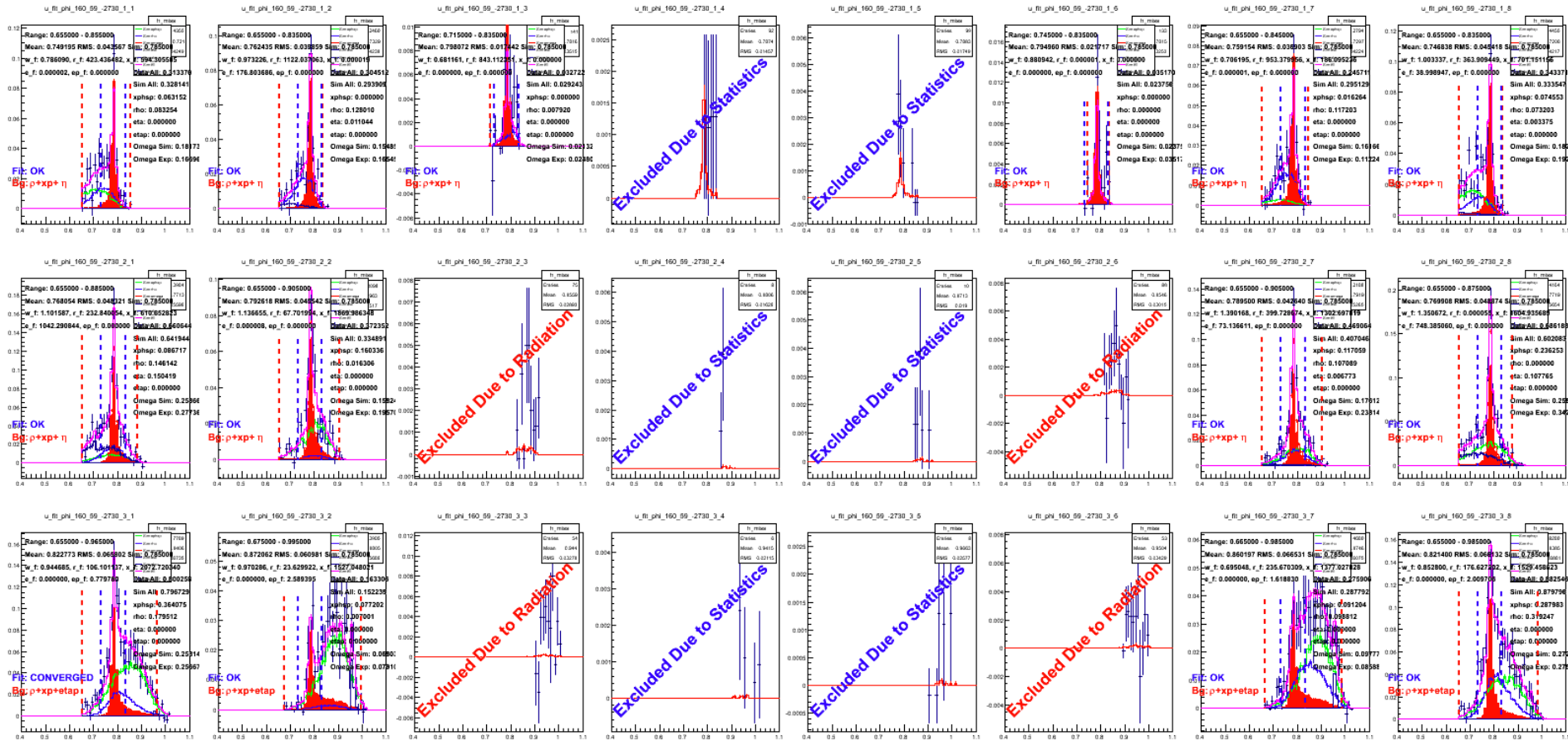
PID Cuts



- SOS: select **electron**
 - Calorimeter cut
 - Cherenkov cut
 - HMS: select **proton**
 - Coincidence timing cut
 - Hebeta (particle velocity)
 - Aerogel Cut
 - Cherenkov Cut: veto e^+
- 99% efficiency**



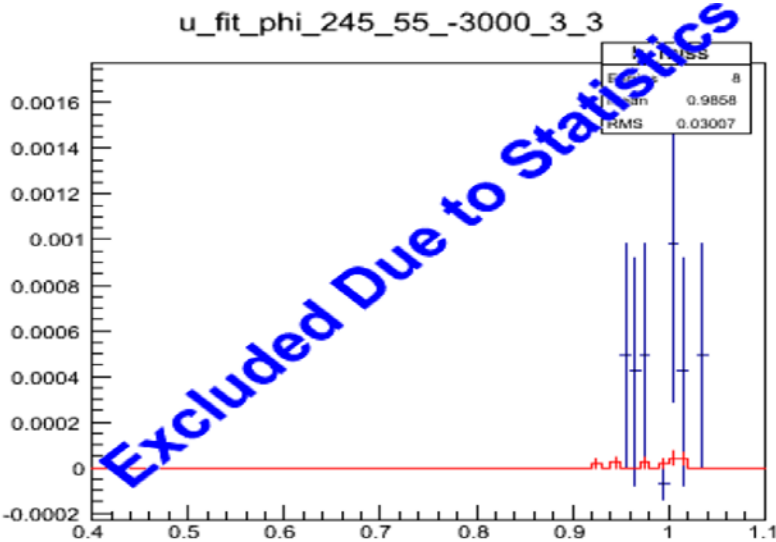
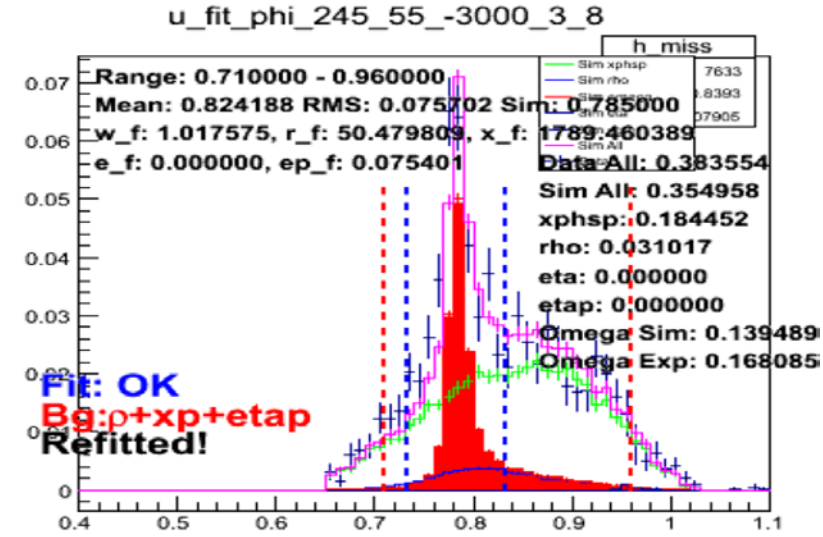
Missing Mass Distribution Background Extraction



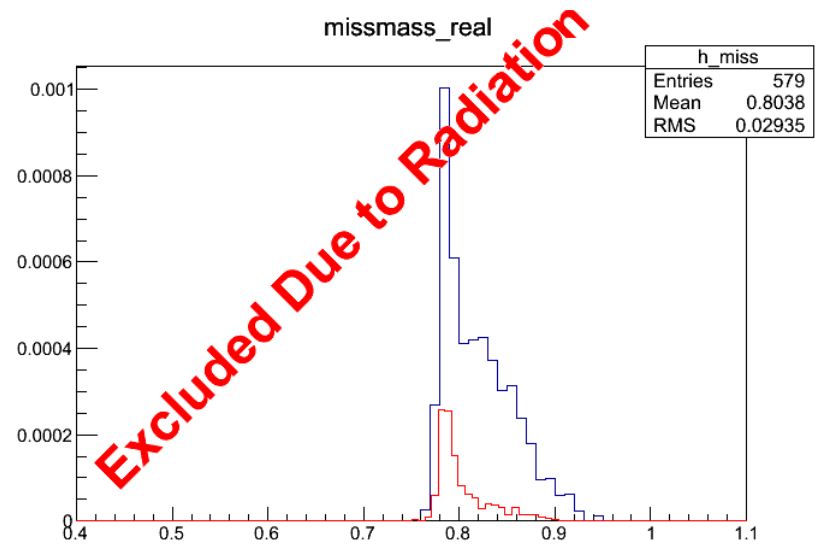
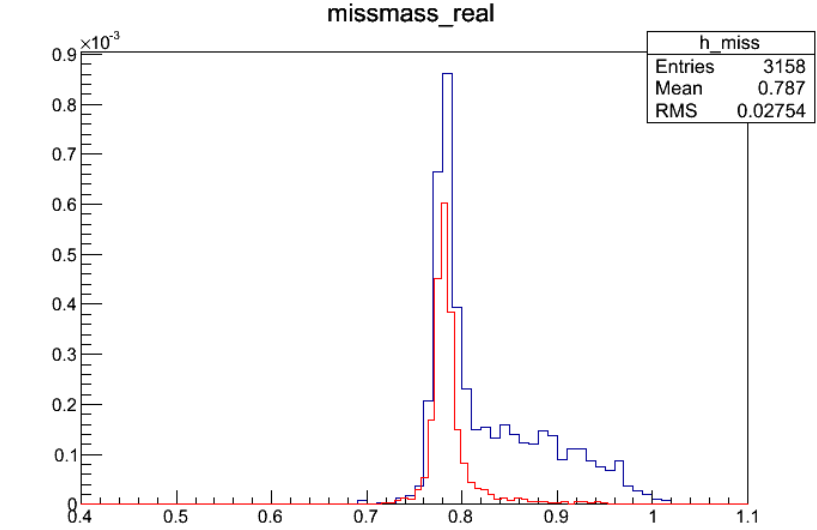
- Integration limits and fitting limits
- Exclusion criteria
 - Exclude the radiative only omega bins
 - Exclude the low statistics bins

Bin Exclusion criteria

Low Statistics



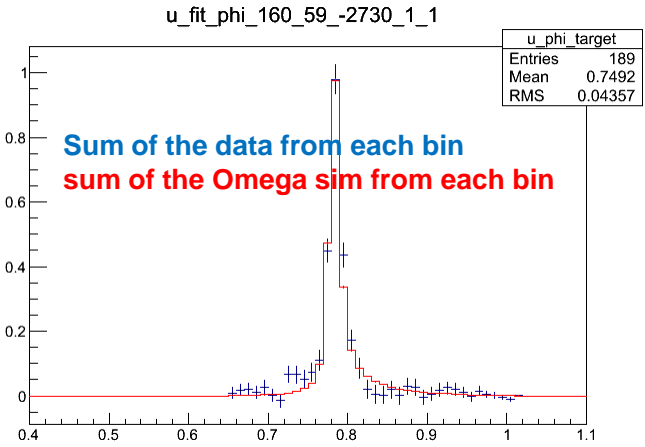
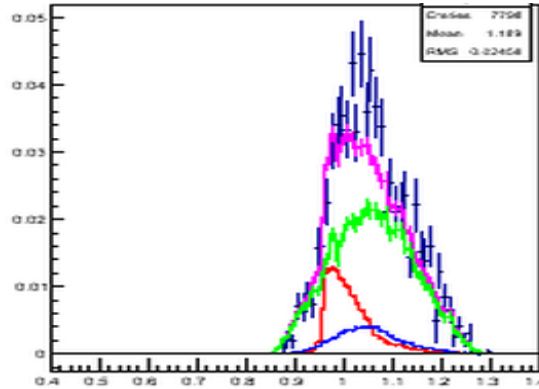
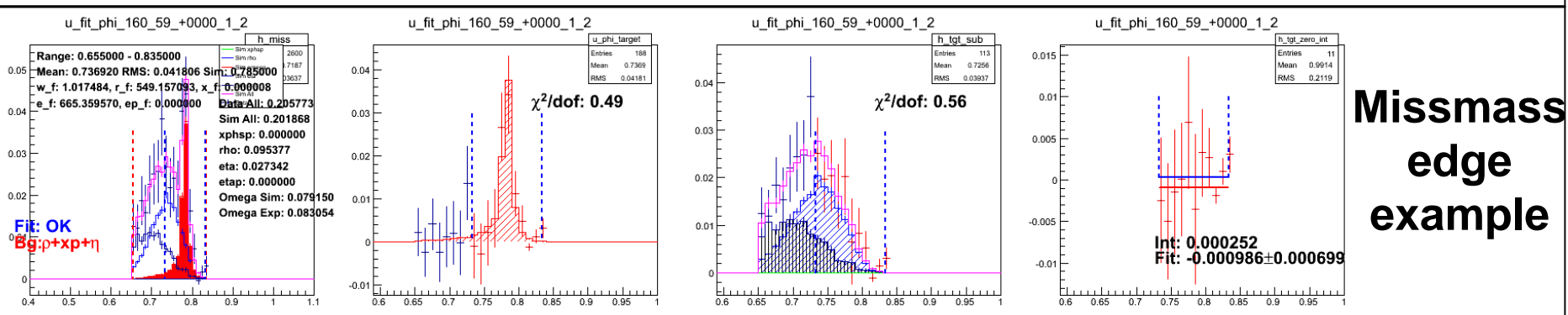
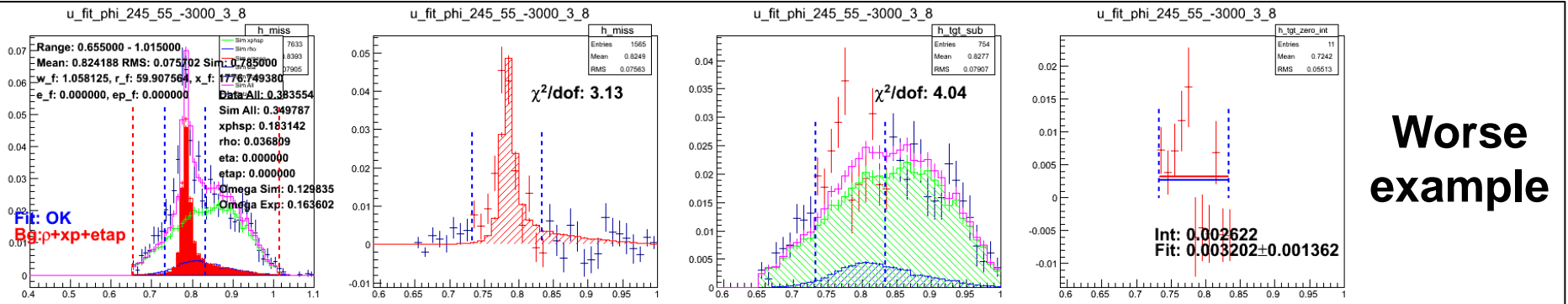
Radiative Tail



Background Extraction and Check

Worse example

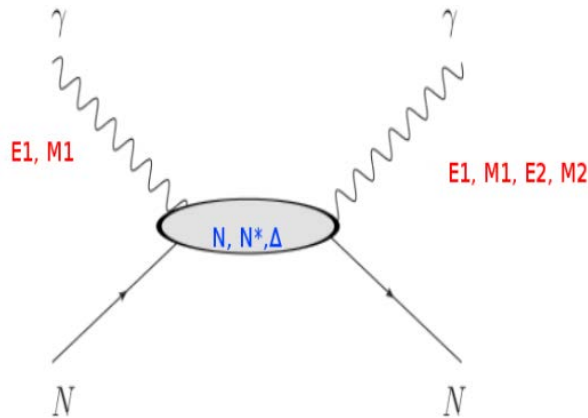
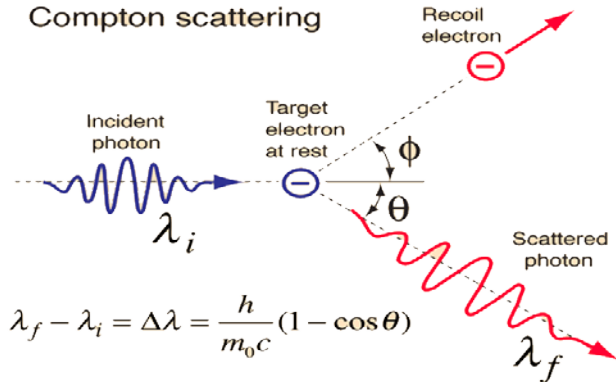
Missmass edge example



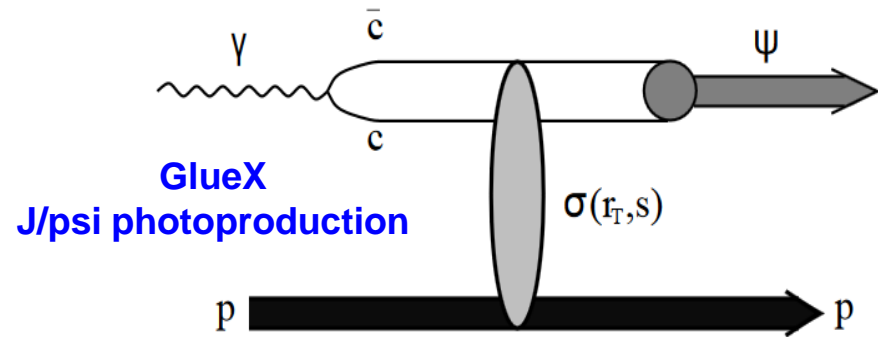
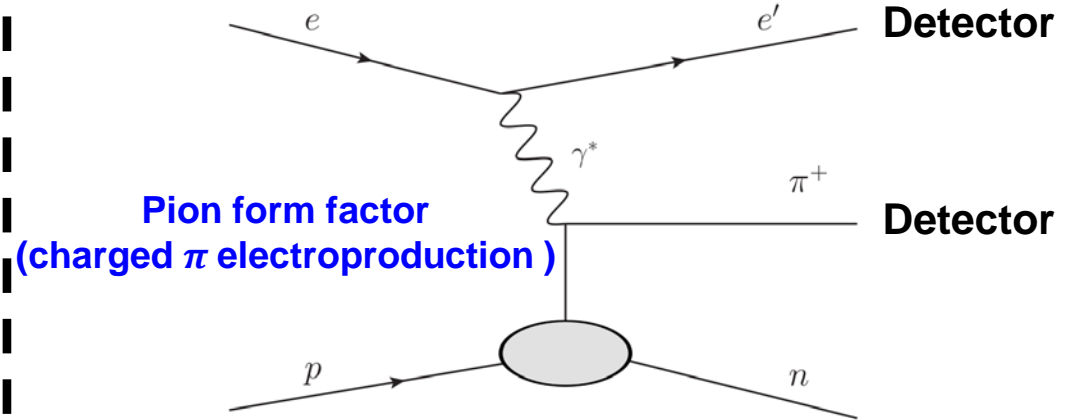
Reconstructed Missing Energy For the **worse example**

Standard Physics at Hall C (Jefferson Lab)

s-Channel Physics



t-Channel Physics

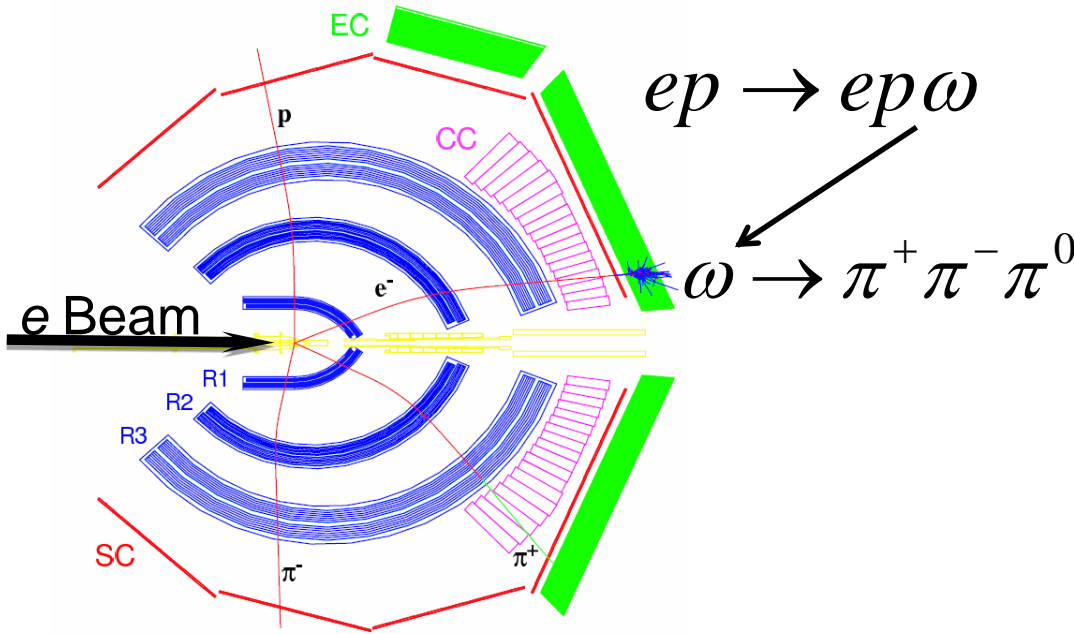


All could be parameterized in four Lorentz invariant Quantities: x , $W(\sqrt{s})$, Q^2 and t

What about u ? Should we include u ?

High t Data from CLAS Hall B (2005)

Morand et al., Eur. Phys. J. A 24, 445 (2005).



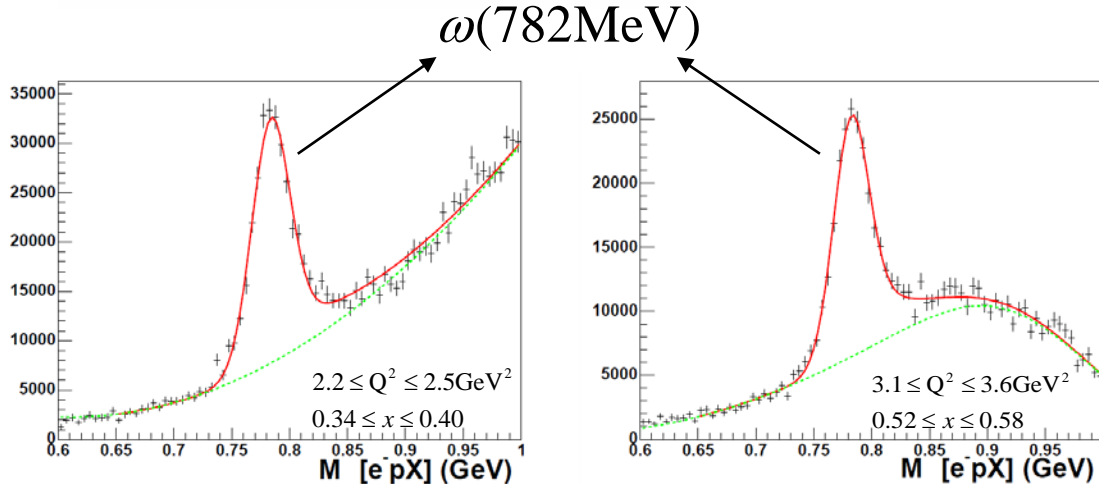
- Hall B Experiment e1-6
 - Oct 2001 – Jan 2002
 - Beam energy: 5.754 GeV
- Kinematic coverage:
 - W : 1.8-2.8 GeV
 - Q^2 : 1.6-5.1 GeV²
 - $-t$: < 2.7 GeV²
 - x : 0.16-0.64

- Event selection:

$$ep \rightarrow ep\pi^+ X$$

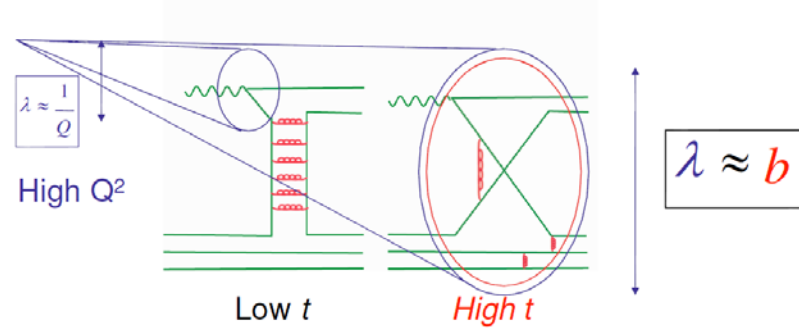
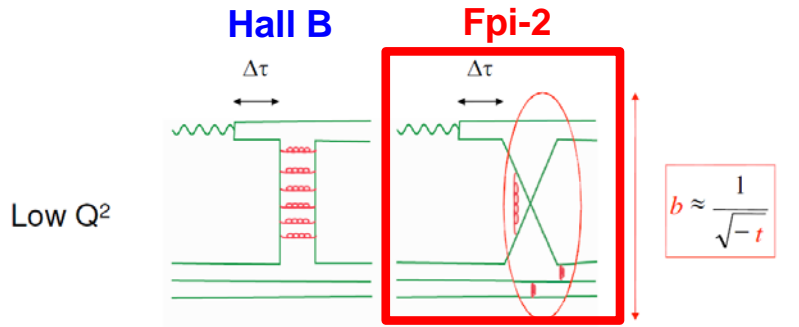
- Reconstructed $e-pX$ missing mass consistent with the ω mass

- Data published in 2005:
 - Morand et al., Eur. Phys. J. A 24, 445 (2005).



Missing mass reconstruction $e-pX$

Regge Trajectory Model by JM Laget



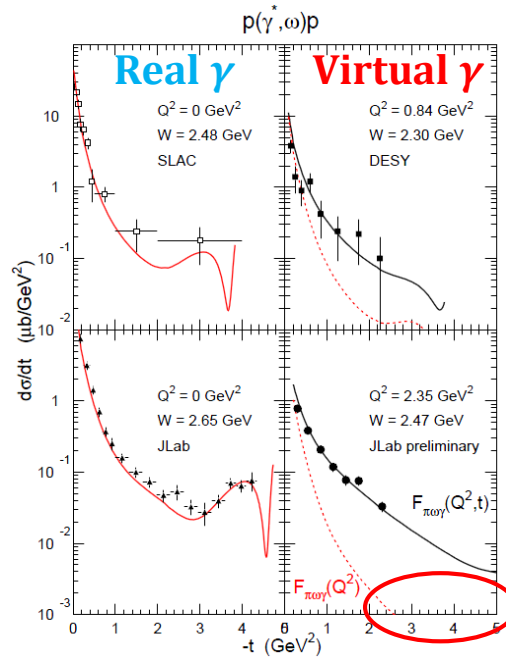
Hard Scattering Mechanism schematics



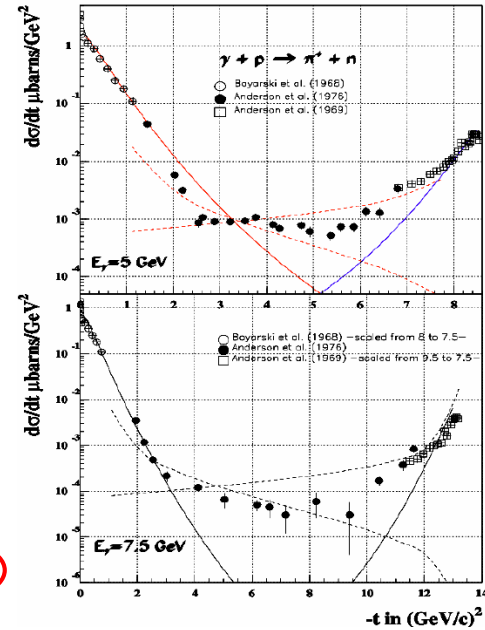
t-Channel Forward

u-Channel Backward

	W (GeV)	X	Q^2 (GeV ²)	$-t$ (GeV ²)	$-u$ (GeV ²)
Hall B	1.8-2.8	0.16-0.64	1.6-5.1	< 2.7	> 1.68
Fpi-2	2.21	0.29	1.6	4.014	0.08-0.13
		0.38	2.45	4.724	0.17-0.24



Fpi2 kinematics



J. M. Laget, Phys. Rev. D 70, 2004

Nucleon Fragmentation Process

Before interaction

$e + H$



After interaction

n (938 MeV)



Remains at target position

■ $H(e, e' \pi^+)n$

t -channel



SOS



HMS

u -channel

ω (770 MeV)



Remains at target position

■ $H(e, e' p)\omega$



SOS



HMS

■ Exclusive Channel: ω is not tagged Allows for kinematic settings which was previously not available

Standard nucleon Fragmentation gives a weird picture

Allows for kinematic settings which was previously not available

Omega Data Analysis

- Fpi-2 (E01-004) 2003
 - Spokesperson: **Garth Huber, Henk Blok**
 - Standard HMS and SOS (e) configuration
 - **Electric form factor of charged** through exclusive π production

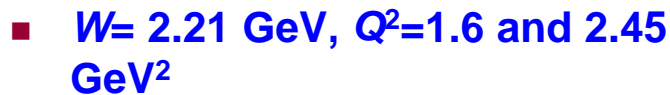
- Primary reaction for Fpi-2



- In addition, we have for free



- Kinematics coverage

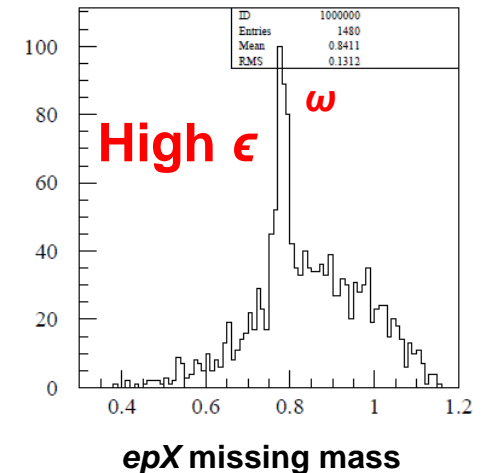
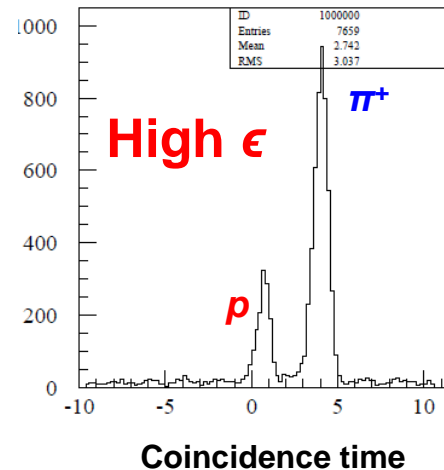
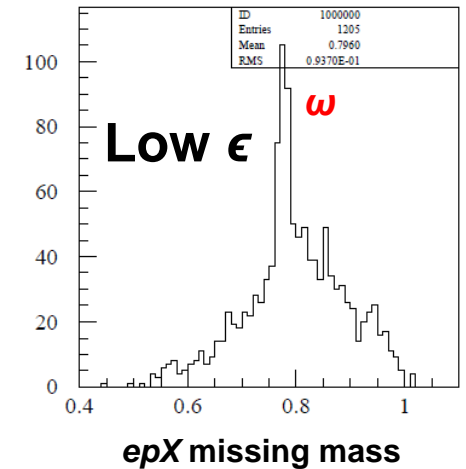
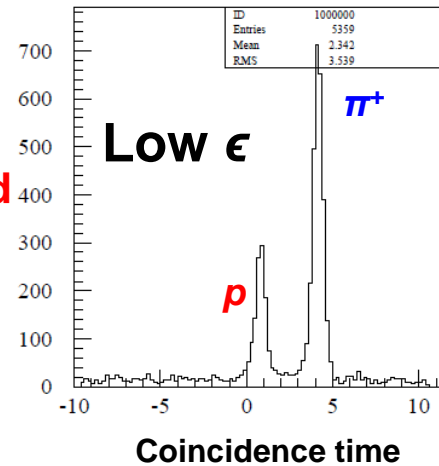


- Two ϵ settings for each Q^2

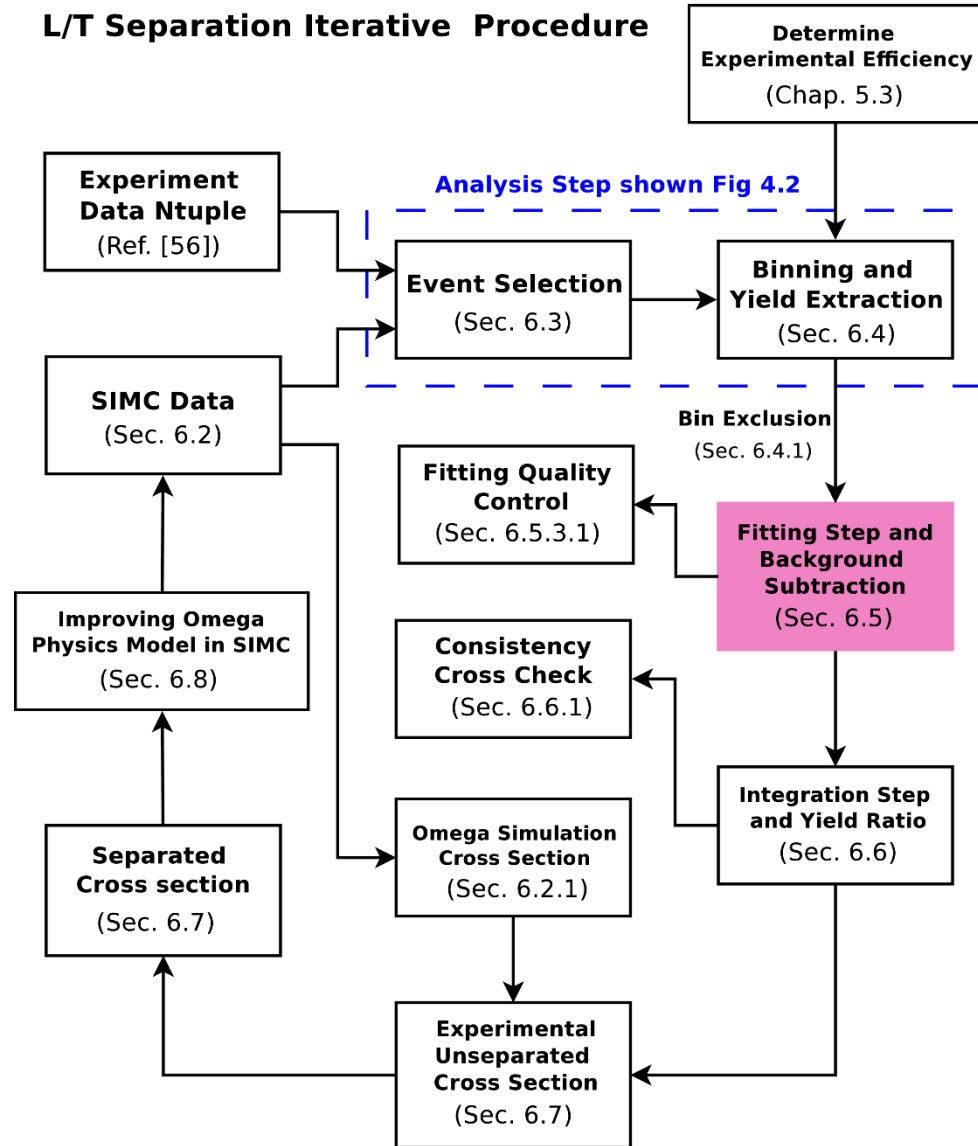
$Q^2=2.45$ GeV²

2003

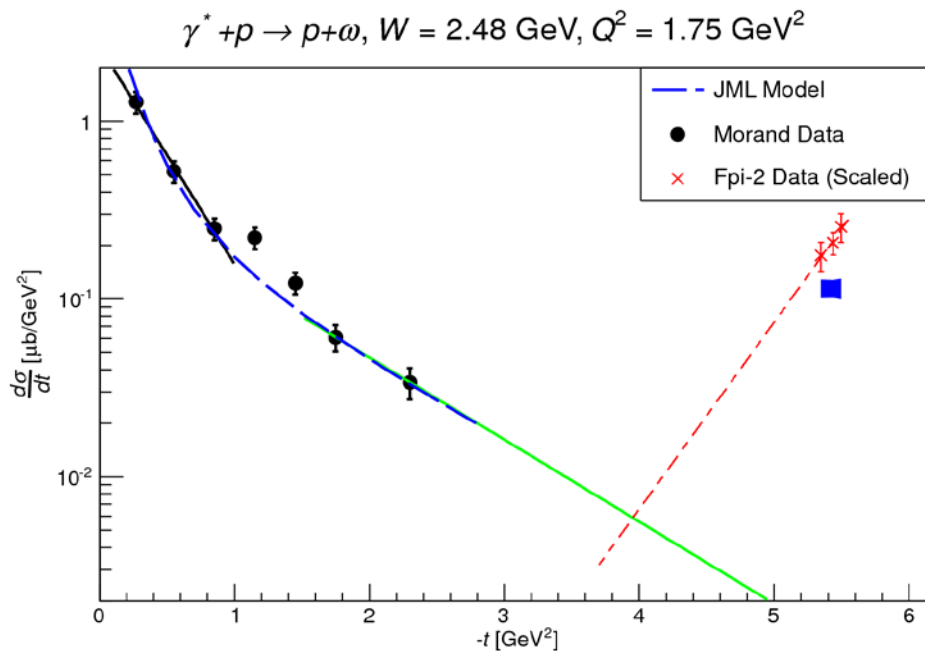
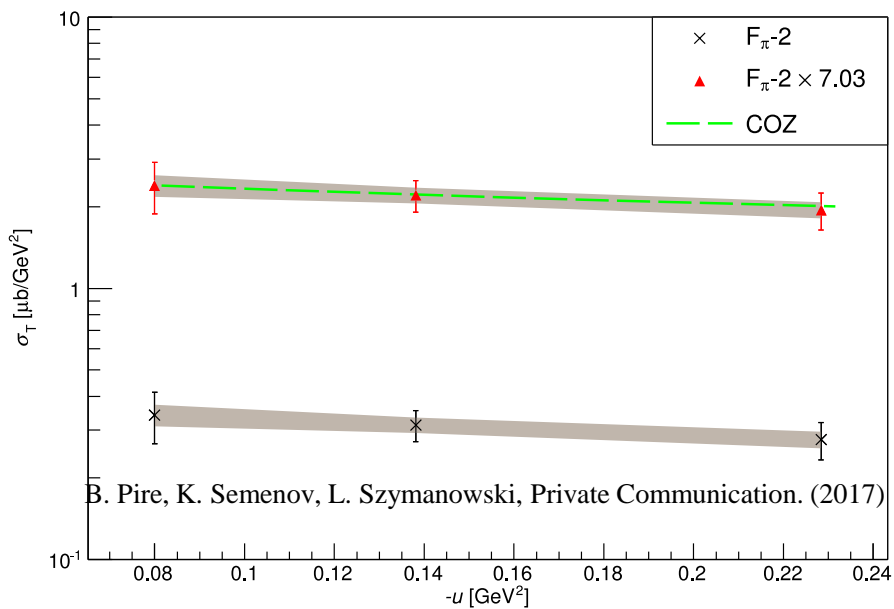
2003/07/25 08.56



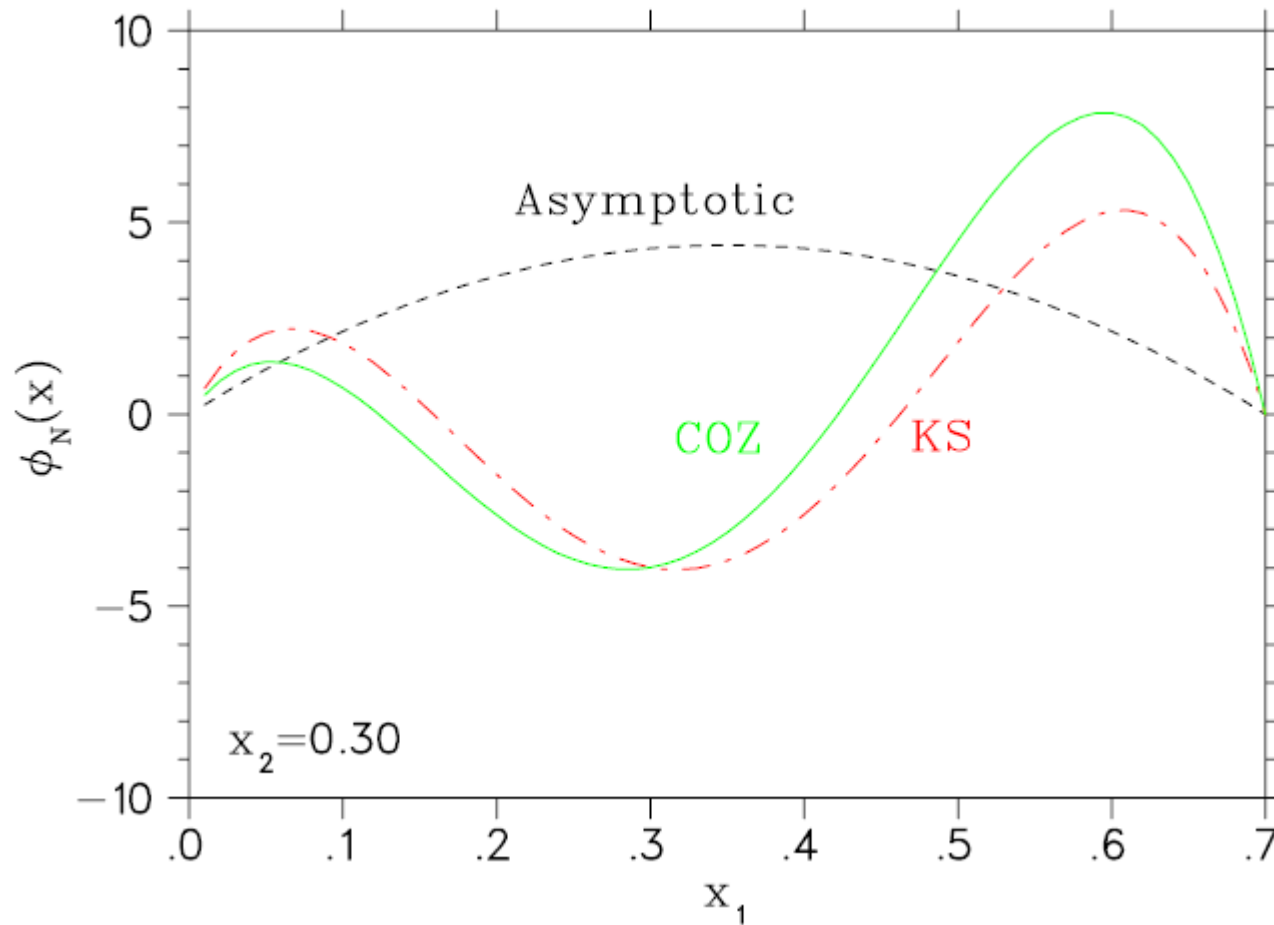
L/T Separation Iterative Procedure



TDA @ $Q^2 = 1.60 \text{ GeV}^2$



Nucleon DA Model



Missing Mass Distribution Background Extraction

Data (blue point)
Xspace Sim (green)
 ρ Sim (light blue)
 ω Sim (red)
 η or η' (black)
Simulation Sum (pink)

Omega

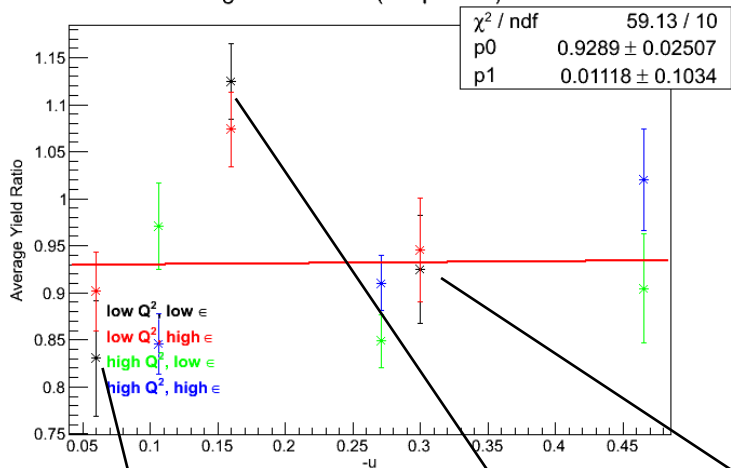
$$R = \frac{Y_{Exp} - Y_{\rho sim} - Y_{Xspace sim} - Y_{\eta sim}}{Y_{\omega sim}}$$

Background Sum Zero= Data – Omega- Bg

- **Fitting Limits (red dashed line):**
 - Not fixed, fit 95% data distribution
- **Integration Limits (blue dashed line):**
 - Fixed for all u-phi bins!
- **Bin Exclusion criteria:**
 - Radiative tail exceeds 50% total ω sim
 - Less than 100 raw counts

Yield Ratio and Simulated Cross-Section

Average Yield Ratio (Yexp/Ysim) vs -u



$$\sigma_T = \frac{t_0 + t_1 \cdot (-u)}{Q},$$

$$\sigma_L = \frac{l_0 + l_1 \cdot (-u)}{Q^4},$$

$$\sigma_{LT} = \left[\frac{lt_0 + lt_1 \cdot (-u)}{Q^2} \right] \cdot \sin \theta^*,$$

$$\sigma_{TT} = \left[\frac{tt_0 + tt_1 \cdot (-u)}{Q^2} \right] \cdot \sin^2 \theta^*,$$

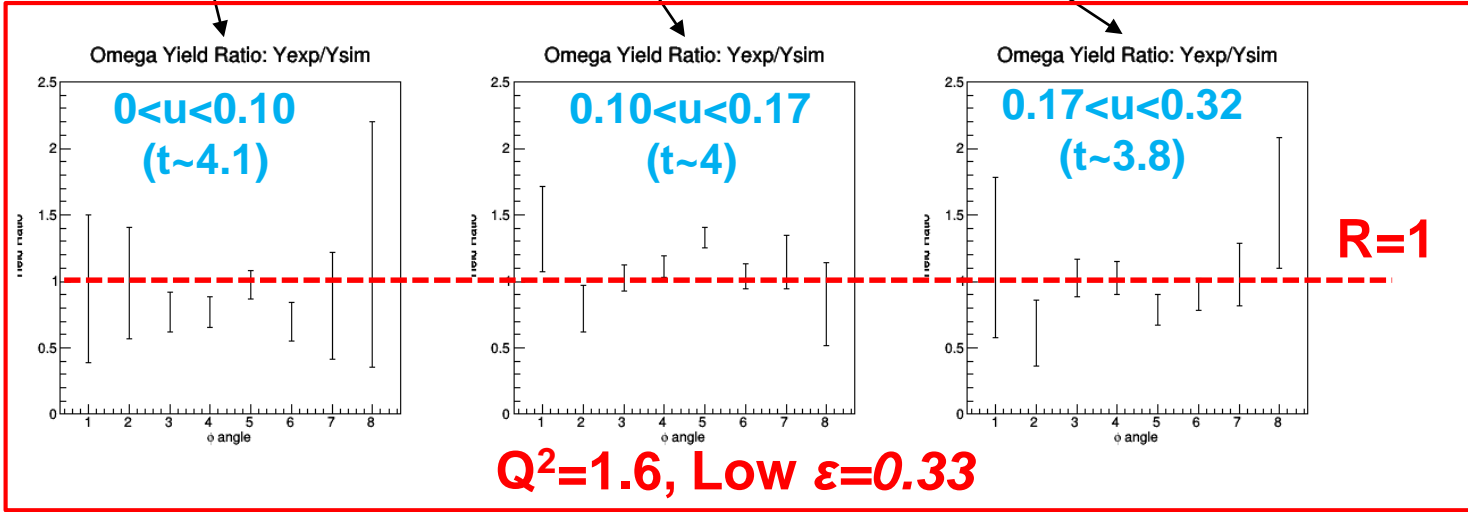
$$2\pi \frac{d\sigma}{dtd\phi} = \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

Model Cross Section

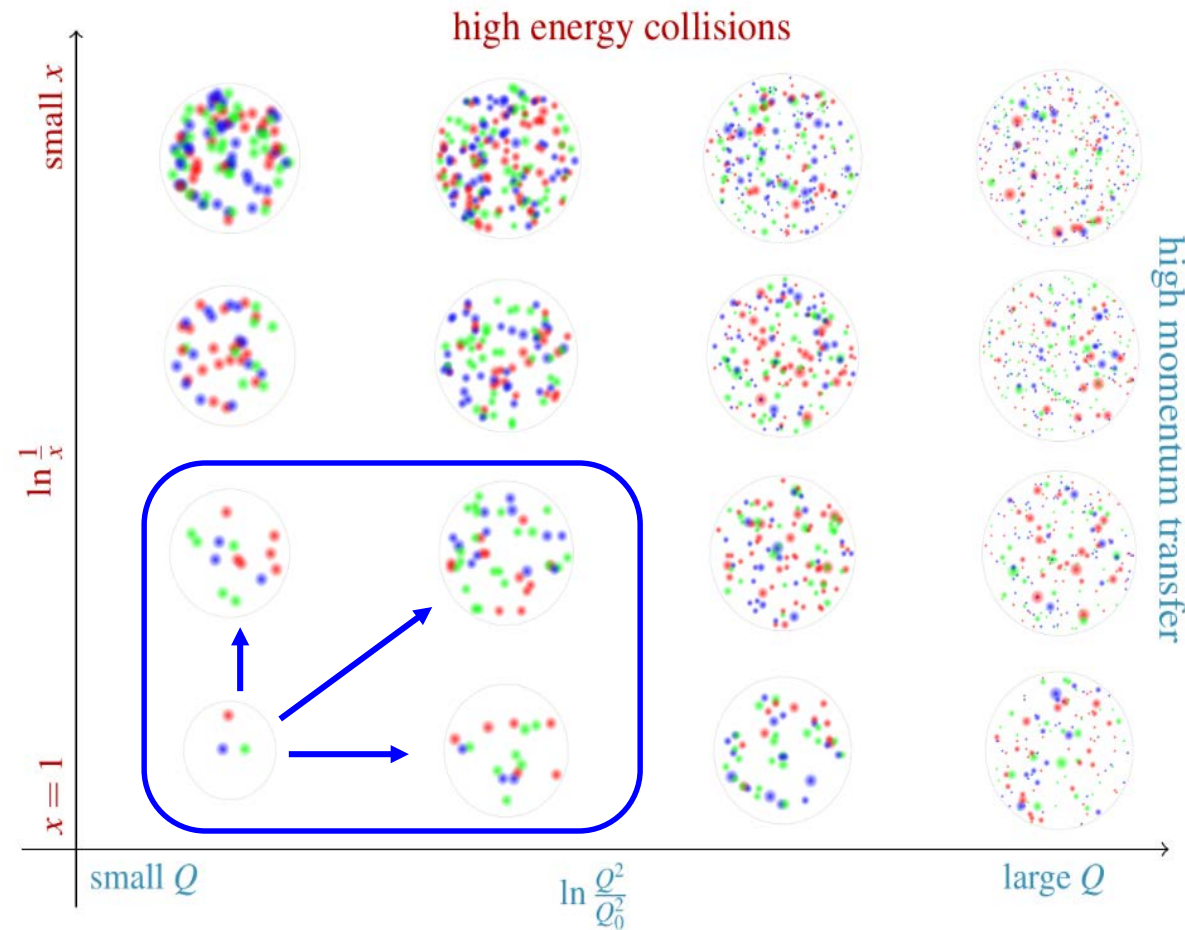
$$\frac{d^2\sigma}{dtd\phi}_{EXP} = R \frac{d^2\sigma}{dtd\phi}_{SIMC}$$

Exp/Sim Yield Ratio

R=1



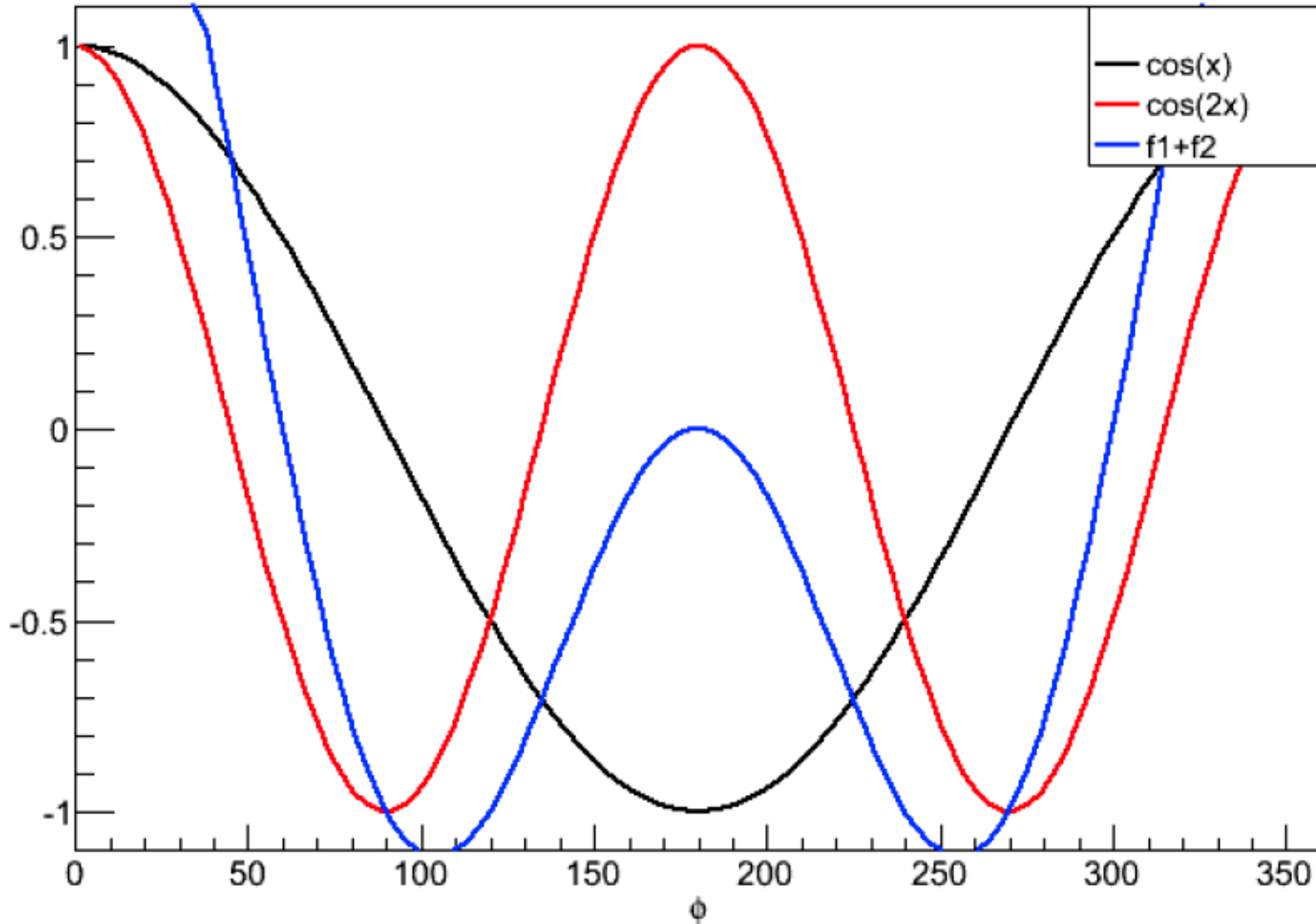
Proton Structure: Known and Unknown



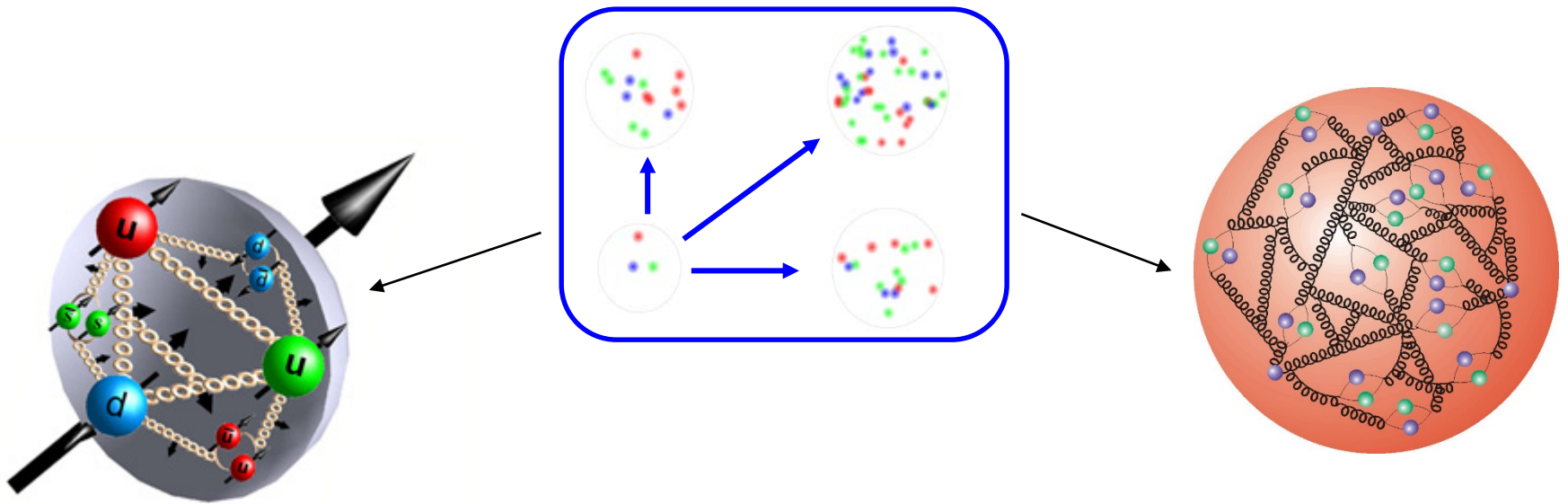
- Proton
 - Dynamic Structure
 - Parton Distribution
 - Interaction
- Static proton structural map is known
- Unknown
 - **Transition (evolution)** of the proton structure
 - General description of the proton structure
- **Goal: Study the transition of the proton structure**

Modulus Check for SigLT and SigTT

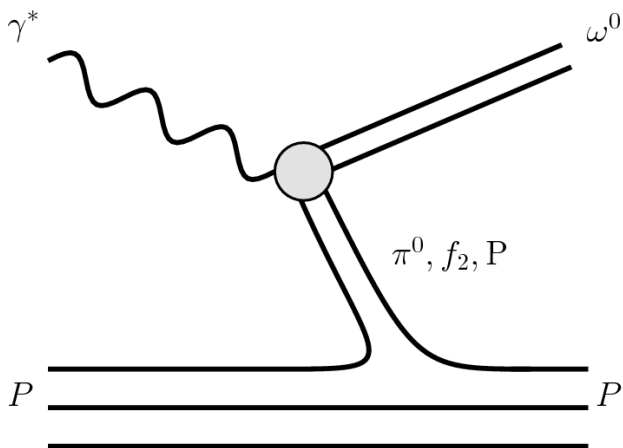
Function Modulus Check



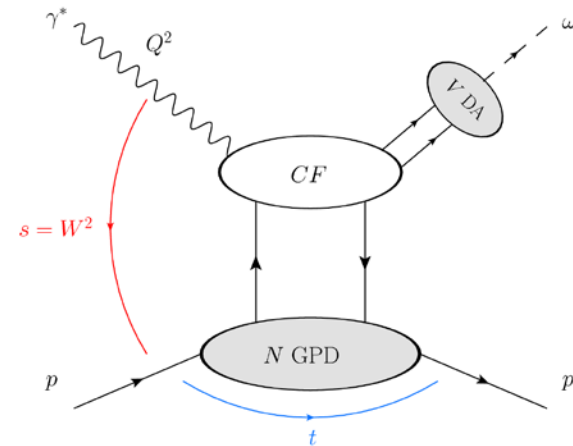
Proton Structure Description



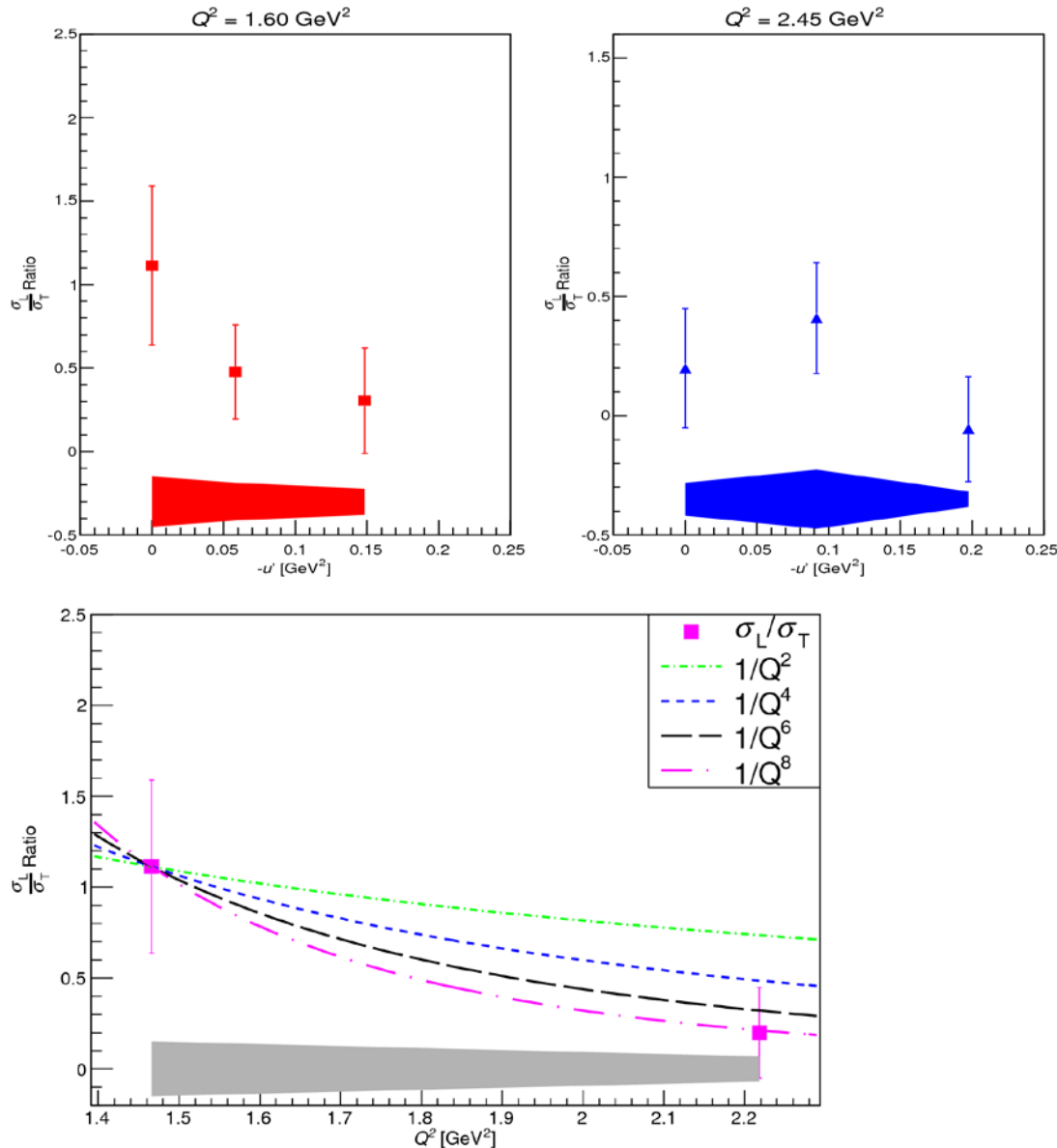
■ Hadronic Model



■ Partonic Model

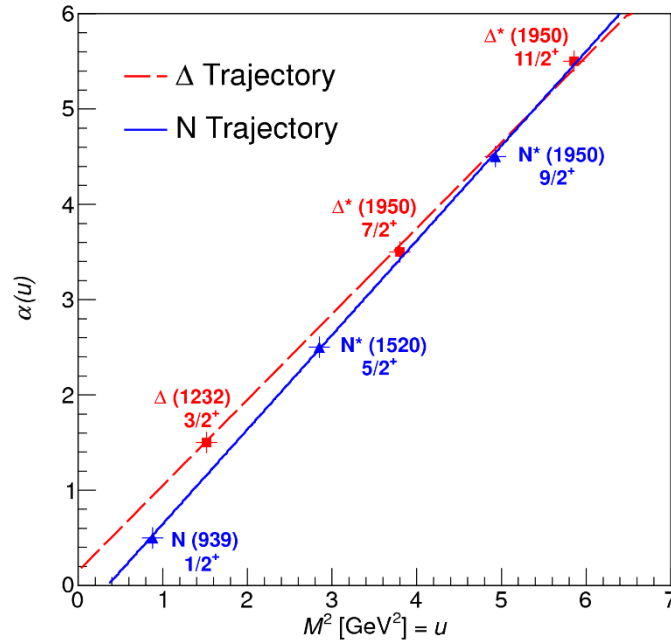
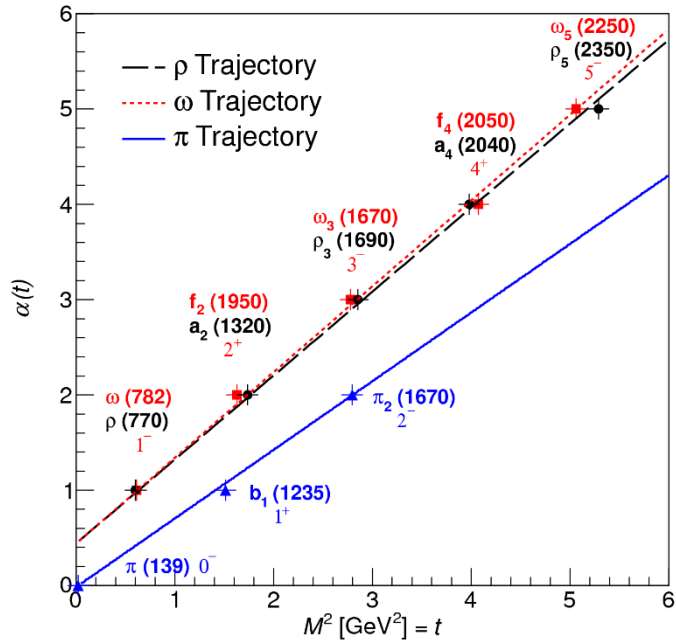


Scaling of σ_L , σ_T and σ_L/σ_T Ratio

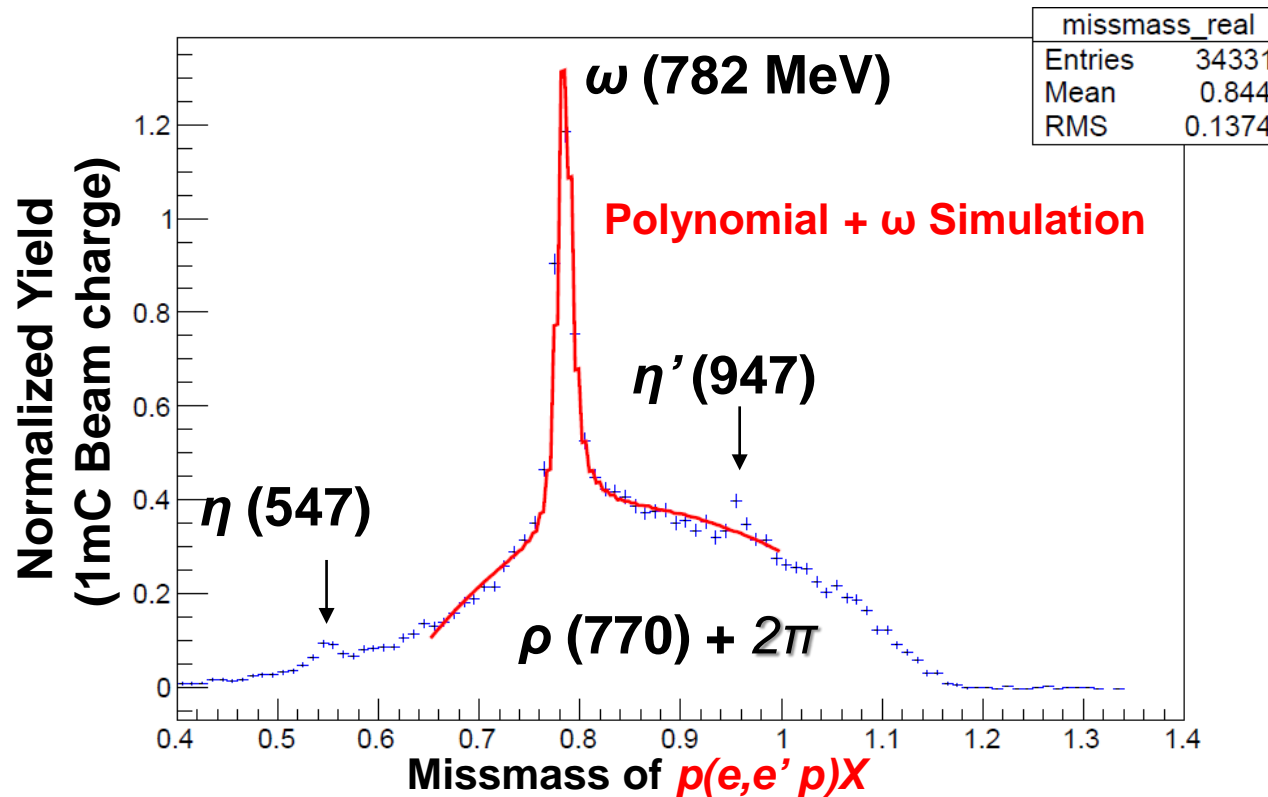


- Dominance of σ_T observed at higher $Q^2 = 2.45$, confirms the TDA prediction
- σ_L drops expected $\sim 1/Q^8$
- σ_T is almost constant

Trajectory

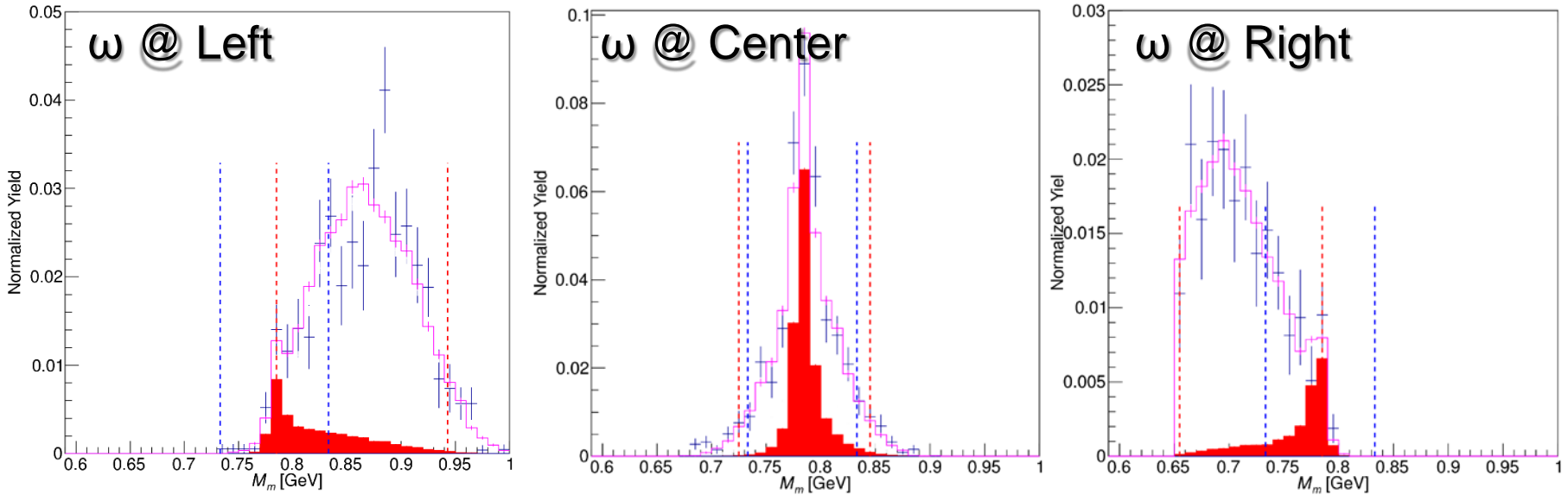


Proof: These are not Elastic Events!



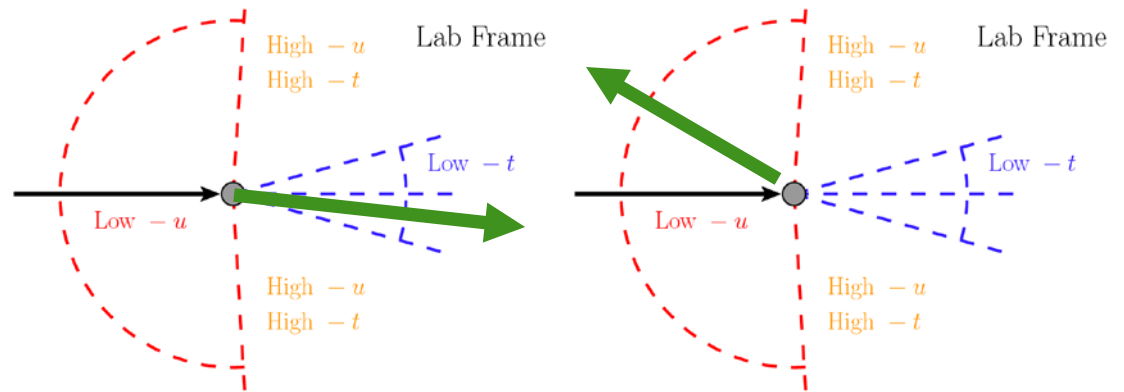
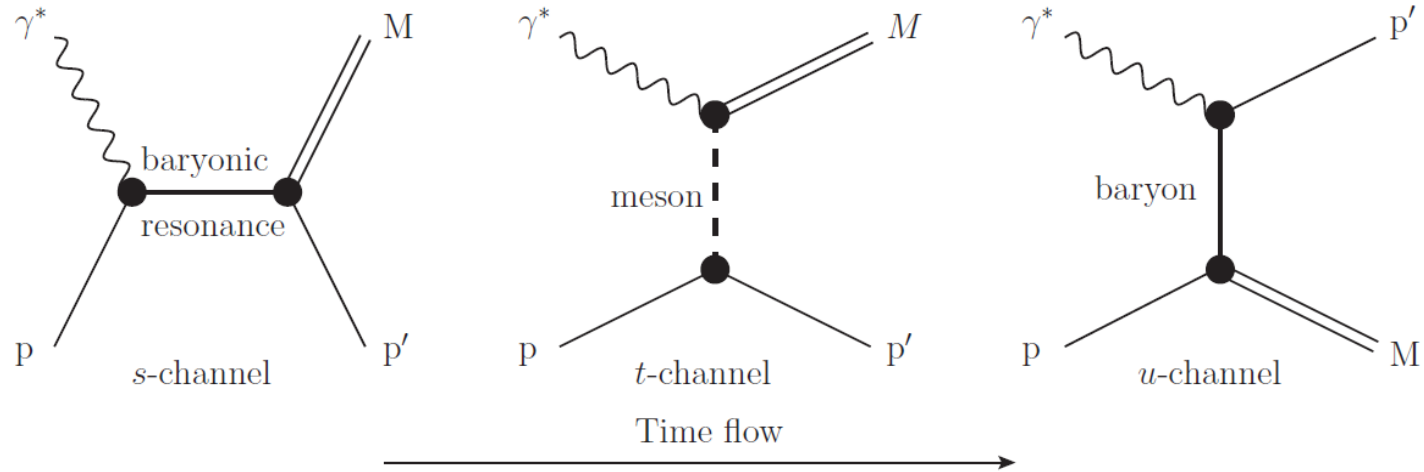
- **Good News!**
 - We see **other Scalar and Vector Mesons**: ρ , η , η' , *two- π phasespace*
- **Bad News!**
 - Channel is **not clean!**
- **Worse News!**
 - **We can't use Polynomial fit !!**

Missing Mass Distribution

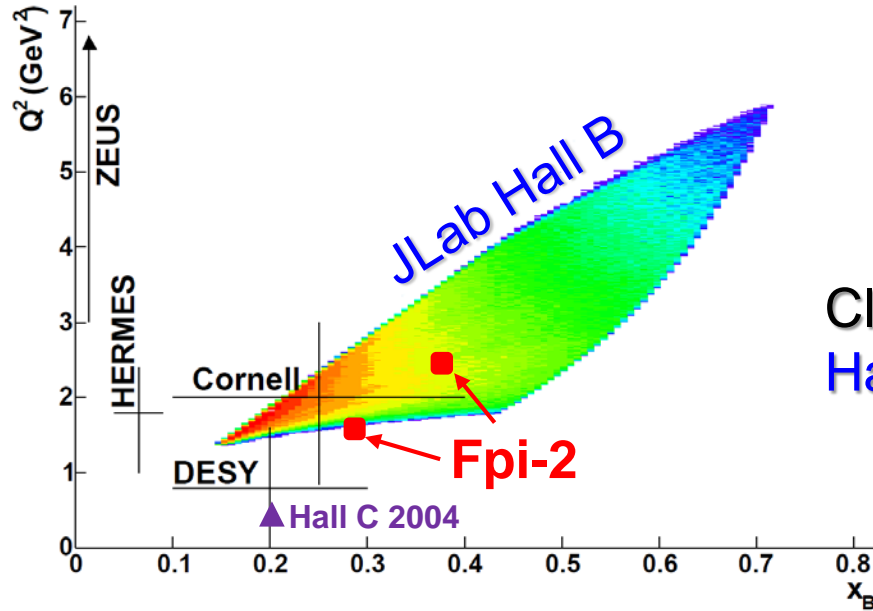


- **Most Challenging Issue: Background Subtraction!**
- **Omega is not always in the center**
- **Four sets of Monte-Carlo is used fit the data**
 - $\omega + \rho + \text{Phase-space} + \eta \text{ or } \eta'$

Mandelstam variables (s, t, u -Channels)



Exclusive ω Electro-Production Data



Closest data set to ours is the
Hall B Morand data

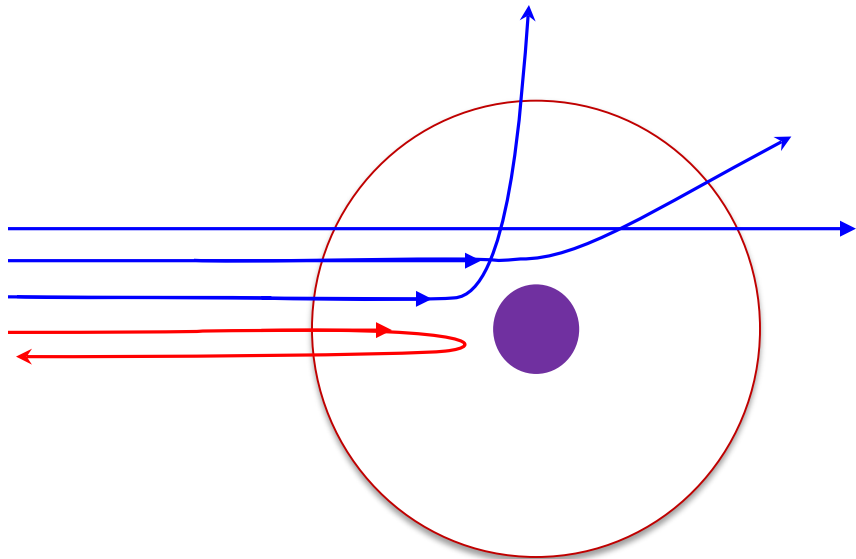
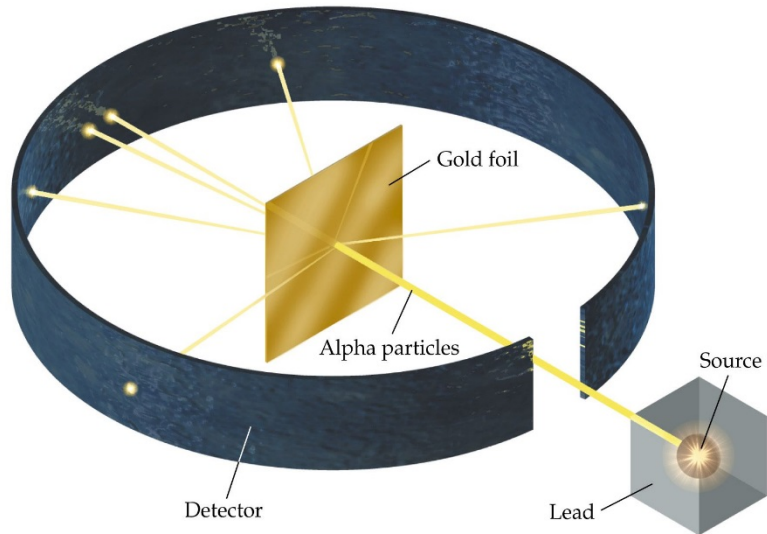
	Q^2 GeV ²	W GeV	x	$-t$ GeV ²
HERMES (Airapetian et al., 2014)	> 1	3-6.3	0.06-0.14	< 0.2
DESY (Joos et al., 1977)	0.3-1.4	1.7-2.8	0.1-0.3	< 0.5
Zeus (Breitweg et al., 2000)	3-20	40-120	~0.01	< 0.6
Cornell (Cassel et al., 1981)	0.7-3	2.2-3.7	0.1-0.4	<1
JLab Hall C (Ambrozewicz et al., 2004)	~0.5	~1.75	0.2	0.7-1.2
JLab Hall B (Morand et al., 2005)	1.6-5.1	1.8-2.8	0.16-0.64	<2.7
JLab Fpi-2 (2017)	1.6, 2.45	2.21	0.29, 0.38	4.0, 4.74

σ_T and σ_L Uncertainty Propagation

$$\frac{\delta\sigma_T}{\sigma_T}(\%) = \frac{1}{(\epsilon_1 - \epsilon_2)} \sqrt{\epsilon_1^2 \left(\frac{\delta\sigma_1}{\sigma_1}\right)^2 \left(1 + \frac{\epsilon_2}{R}\right)^2 + \epsilon_2^2 \left(\frac{\delta\sigma_2}{\sigma_2}\right)^2 \left(1 + \frac{\epsilon_1}{R}\right)^2}, \quad (6.35)$$

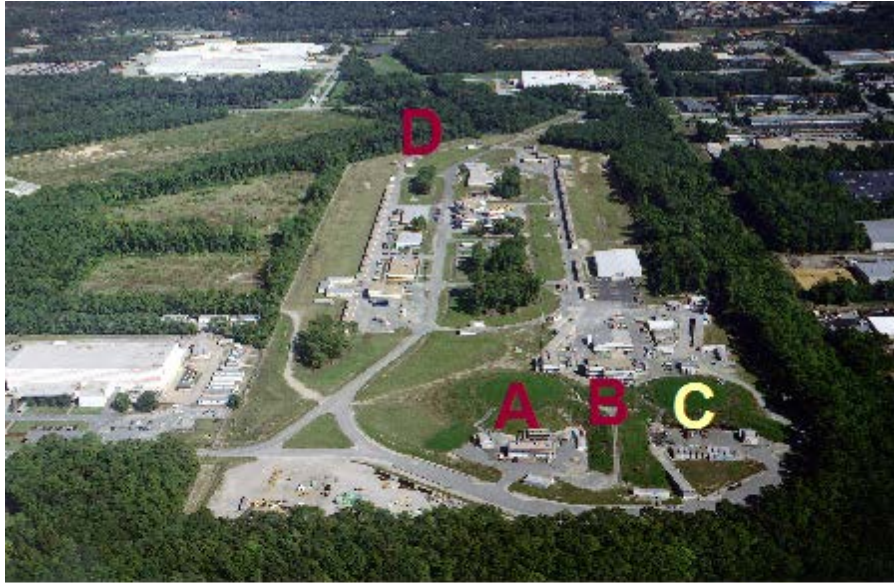
$$\frac{\delta\sigma_L}{\sigma_L}(\%) = \frac{1}{(\epsilon_1 - \epsilon_2)} \sqrt{\left(\frac{\delta\sigma_1}{\sigma_1}\right)^2 (R + \epsilon_1)^2 + \left(\frac{\delta\sigma_2}{\sigma_2}\right)^2 (R + \epsilon_2)^2}, \quad (6.36)$$

Rutherford Experiment Atomic Structure



- Rutherford Experiment:
 - Need both **forward** and **backward** scattered alpha particles to yield complete atomic structure!
- What about nucleons?
 - Does **t-channel** physics contain all the nucleon structure information?
 - **u-channel** physics contain **unique information** whose meaning is unclear (B. Pire et. al)
- How do we **access u-channel** physics?

Jefferson Lab Hall C



- **Main Structure**
 - Two Super-Conducting Linear Accelerators
 - Experimental Hall: A ,B, C, D
- **Hall C**
 - High precision high beam current
 - LT separation
- **April 2017: 12 GeV upgrade completed**
 - New spectrometer is on line

