

# $u$ -channel Exclusive Electroproduction at Jefferson Lab

Garth Huber



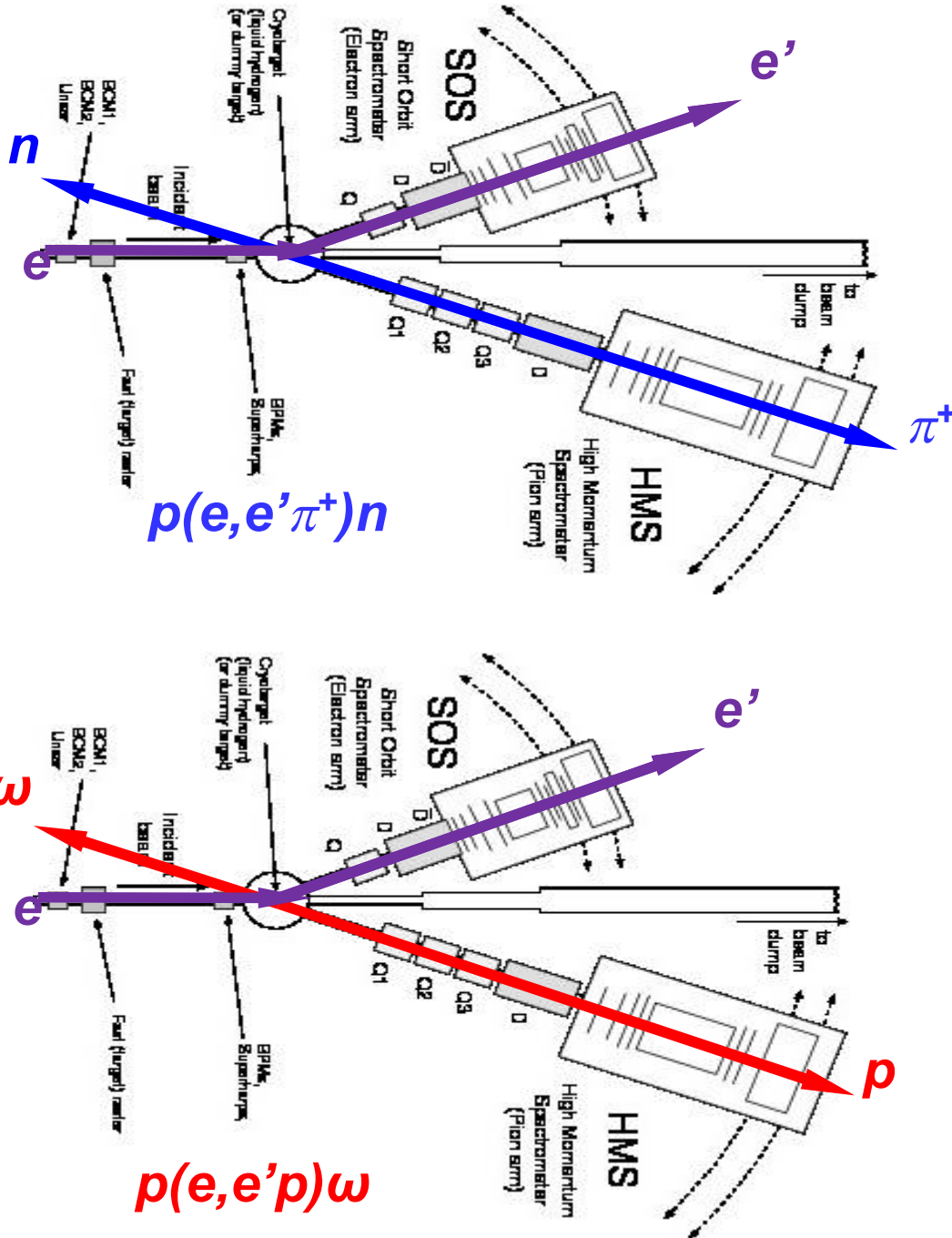
CFNS Workshop on Baryon Dynamics  
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Supported by:



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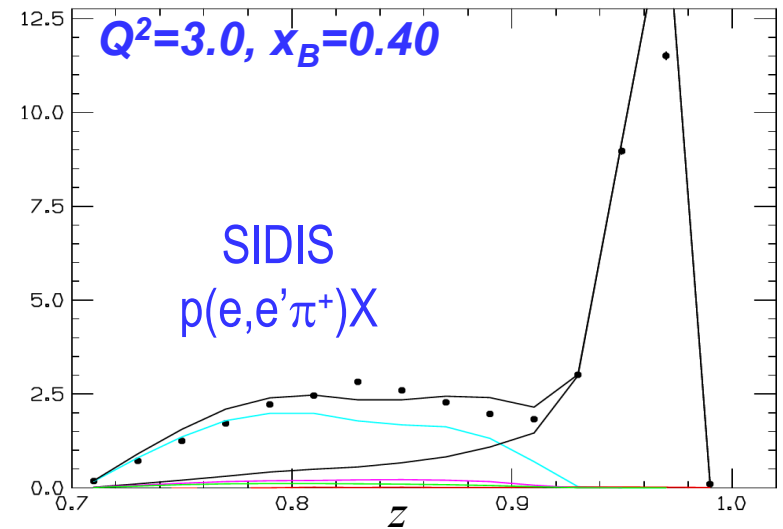
# $t$ -Channel $\pi^+$ vs $u$ -Channel $\omega$ Production



## Hadron detected along $q$ -vector ( $p_{\gamma^*}$ )

- $p_{\pi^+}$  is parallel to  $p_{\gamma^*}$  (**forward**)
- $p_{\omega}$  is anti-parallel to  $p_{\gamma^*}$  (**backward**)
- Exclusive channel is kinematic endpoint at  $z \rightarrow 1$

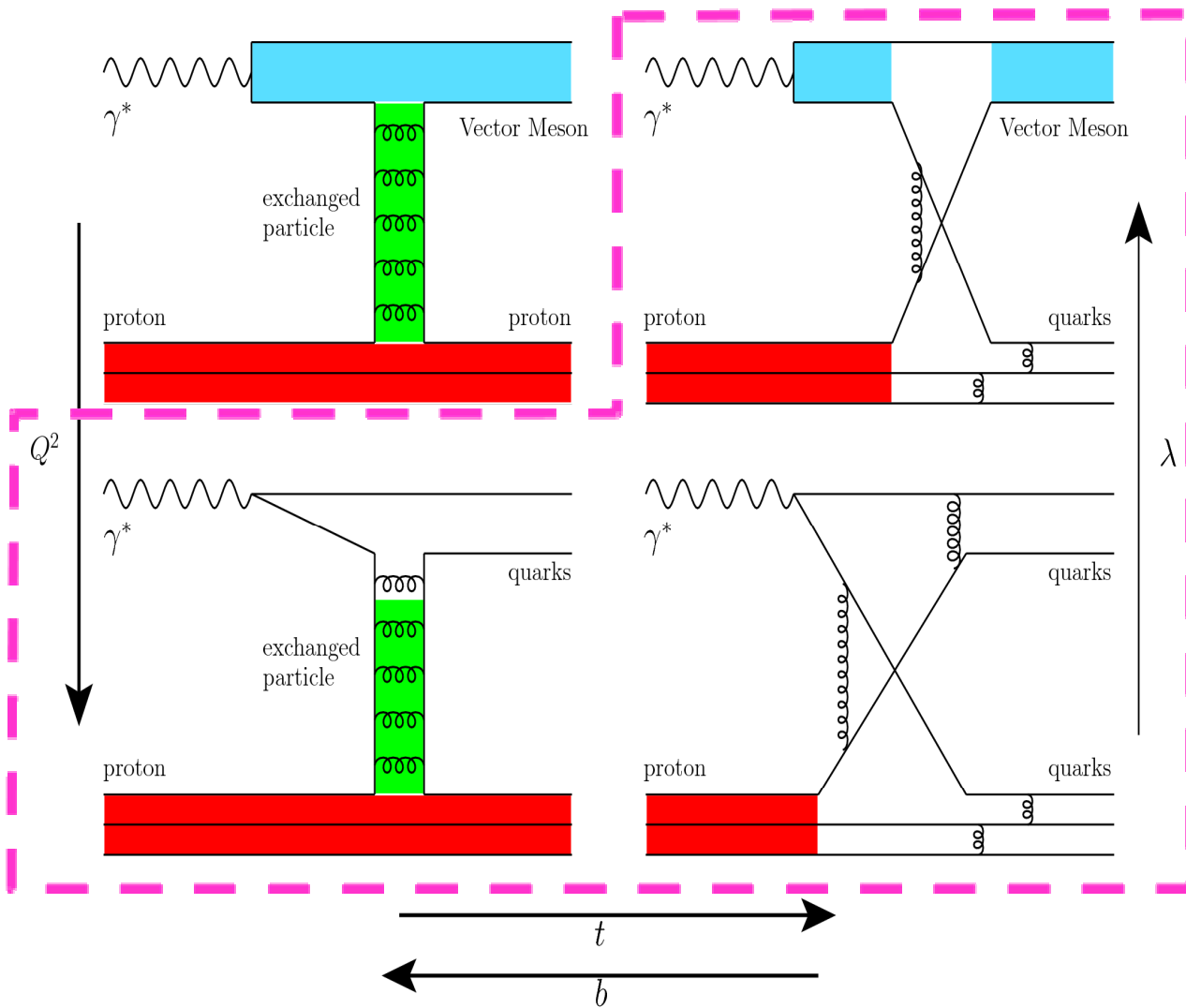
Exclusive  $p(e, e' \pi^+) n$



## $p(e, e' p) \omega$ Exclusive channel

- Full kinematic reconstruction of final state
- Do not detect any part of decayed  $\omega$

# Hadronic Model: Evolution of Proton Structure



Evolution of the Proton Structure

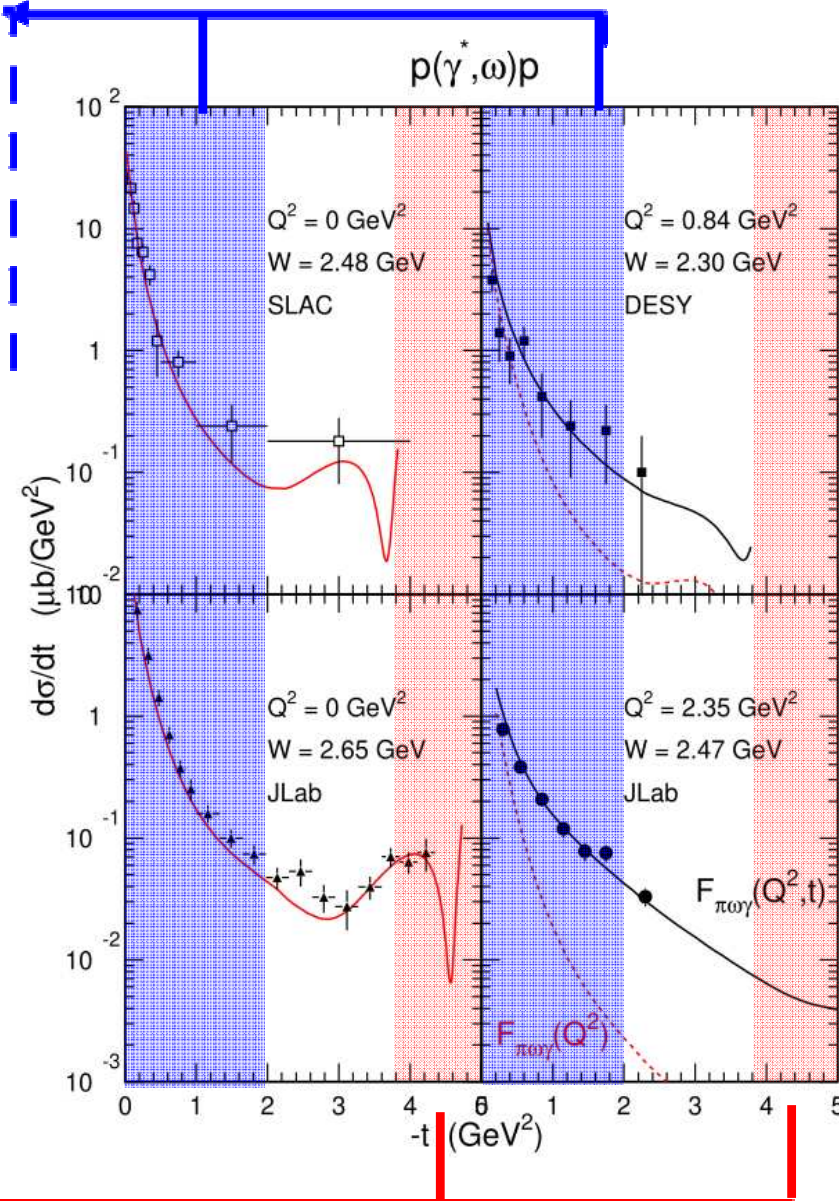
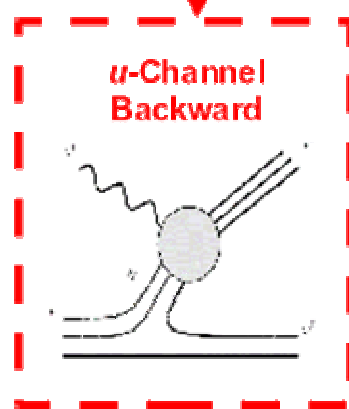
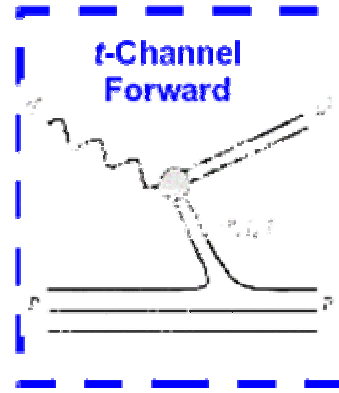
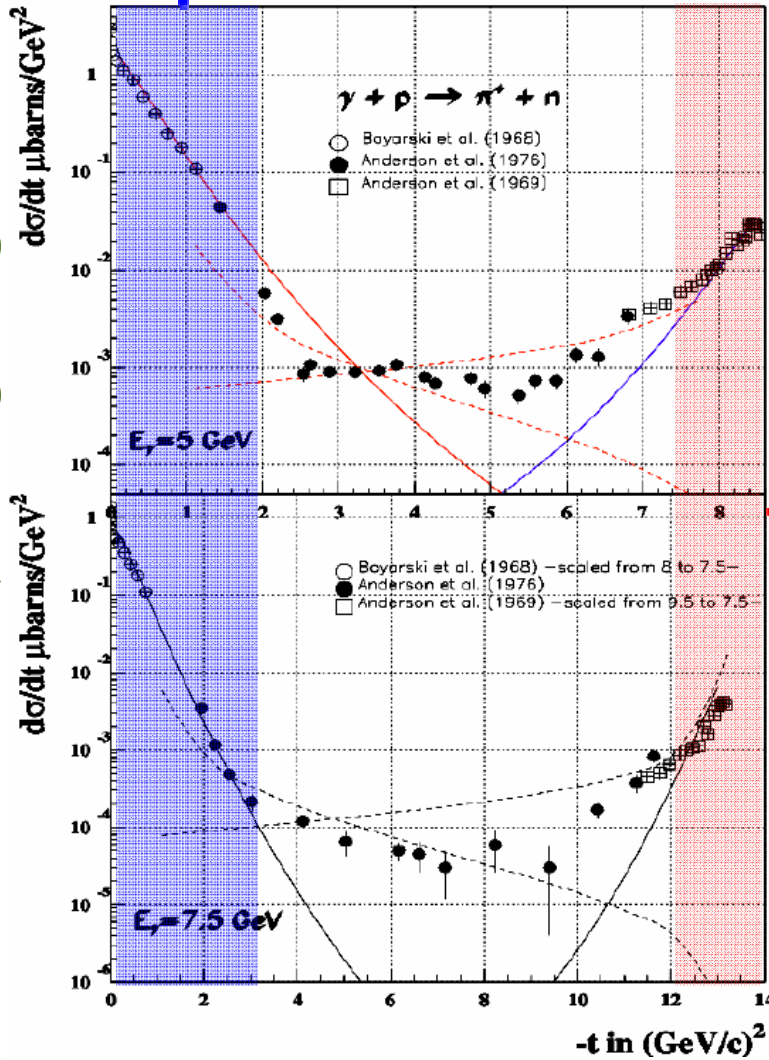
- Physics observables
  - $t$ ,  $W(s)$ ,  $Q^2$ ,  $x$
- $x$  Evolution:
  - 0.2–0.3 valence quark distribution pronounced
- $W$  Evolution:
  - Above resonance region
- **$Q^2$  Evolution**
  - **Wavelength of  $\gamma^*$  probe**
- **$t$  Evolution**
  - **Impact parameter**  
( $b \sim 1/\sqrt{-t}$ )
- What about  $u$ ?
  - **Baryon exchange processes**

# Hadronic Model: Regge Model by JM Laget

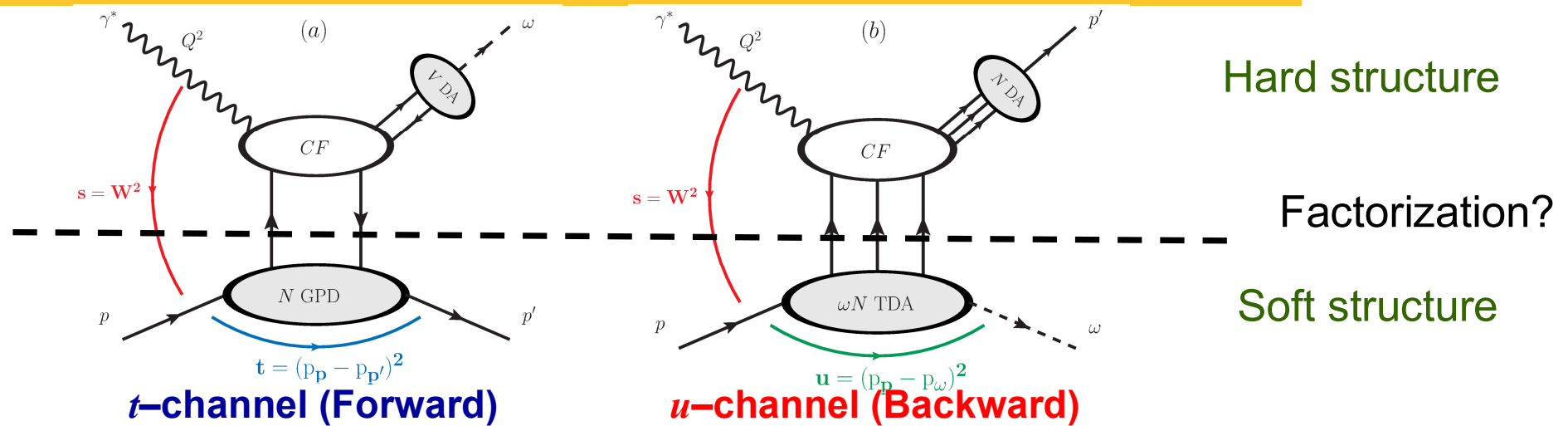
M. Guidal, J.-M. Laget, M. Vanderhaeghen, PLB 400(1997)6

J.-M. Laget, Prog.Part.Nucl.Phys. 111(2020)103737

Garth Huber, huberg@uregina.ca



Soft structure → Hard → Soft transition



## Baryon to Meson Transition Distribution Amplitude (TDA)

- Extension of collinear factorization to backward angle regime. Further generalization of the concept of GPDs.
- Backward angle factorization first suggested by Frankfurt, Polykaov, Strikman, Zhalov, Zhalov at JLab 2002 Exclusive Reactions Workshop.
- TDAs describe the transition of nucleon to 3-quark state and final state meson. *[gray oval of plot b]*
- A fundamental difference between GPDs and TDAs is that TDAs are defined as hadronic matrix elements of 3-quark operator, while GPDs involve quark-antiquark operator.
- **Can be accessed experimentally in backward angle meson electroproduction reactions.**

- **Forward angle kinematics**,  $-t \sim -t_{min}$  and  $-u \sim -u_{max}$ , in the regime where handbag mechanism and GPD description may apply, Skewness is defined in usual manner:

$$\xi_t = \frac{p_1^+ - p_2^+}{p_1^+ + p_2^+} \text{ where } p_{1,2} \text{ refer to light cone } + \text{ components}$$

in  $\gamma^*(q) + p(p_1) \rightarrow \omega(p_\omega) + p'(p_2)$

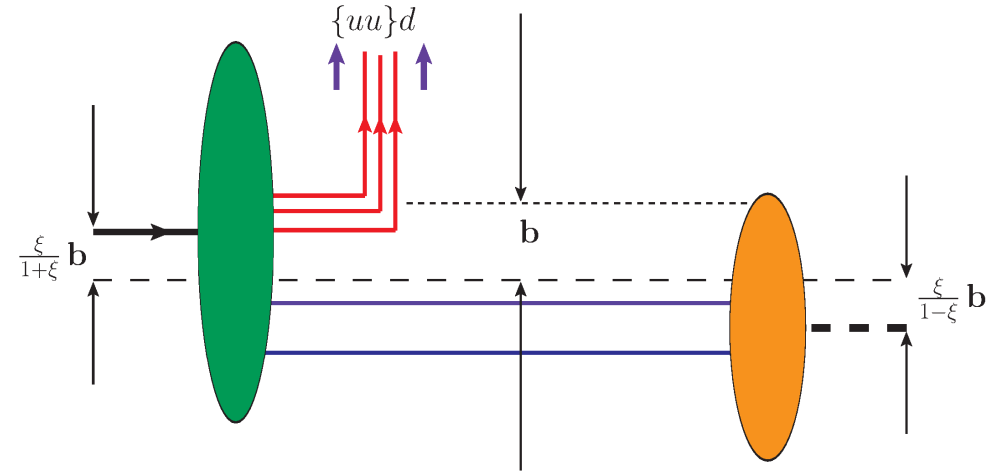
- **Backward angle kinematics**,  $-u \sim -u_{min}$  and  $-t \sim -t_{max}$ , Skewness is defined with respect to  $u$ -channel momentum transfer in TDA formalism

$$\xi_u = \frac{p_1^+ - p_\omega^+}{p_1^+ + p_\omega^+}$$

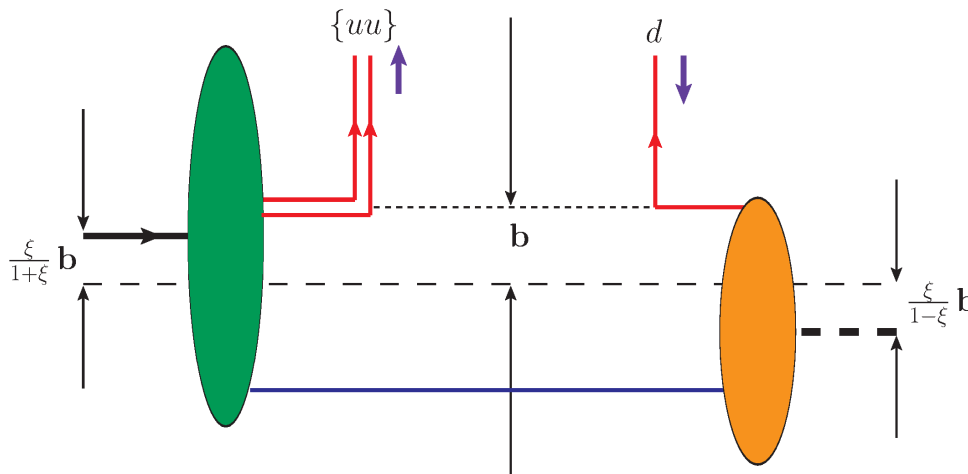
- GPDs depend on  $x$ ,  $\xi_t$  and  $t = (\Delta^t)^2 = (p_2 - p_1)^2$   
TDAs depend on  $x$ ,  $\xi_u$  and  $u = (\Delta^u)^2 = (p_\omega - p_1)^2$
- Impact parameter space interpretation of TDAs is similar to GPDs, except one has to Fourier transform with respect to  $\Delta^u_T \approx (p_\omega - p_1)_T$

# Impact parameter Interpretation of TDA

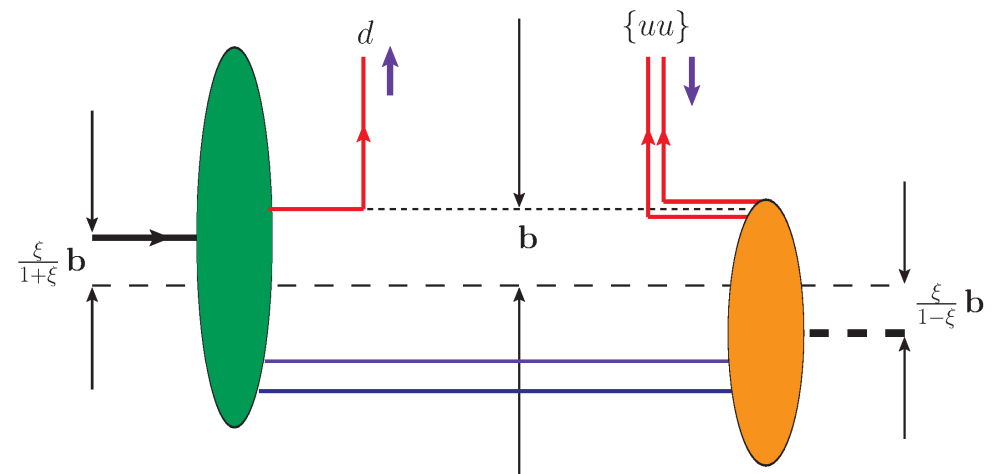
- After integrating over one momentum fraction  $x_i$ , the three exchanged quarks can be treated as an effective diquark+quark pair
- Impact picture then looks very much like that for GPDs



ERBL :  $x_3 = w_3 + \xi \geq 0$ ;  $x_1 + x_2 = \xi - w_3 \geq 0$ ;  
 $\rightarrow$  All 3 quark momentum fractions  $x_i$  positive



DGLAP I :  $x_3 = w_3 + \xi \leq 0$ ;  $x_1 + x_2 = \xi - w_3 \geq 0$ ;  
 $\rightarrow$  One  $x_i$  negative

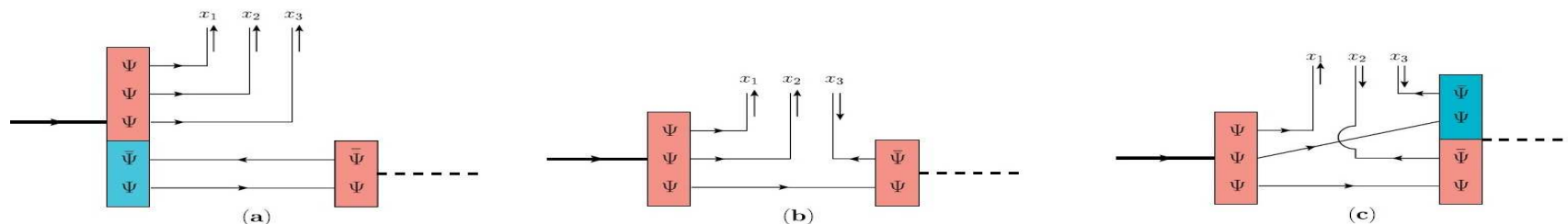


DGLAP II :  $x_3 = w_3 + \xi \geq 0$ ;  $x_1 + x_2 = \xi - w_3 \leq 0$ ;  
 $\rightarrow$  Two  $x_i$  negative

# Partonic Interpretation of TDA

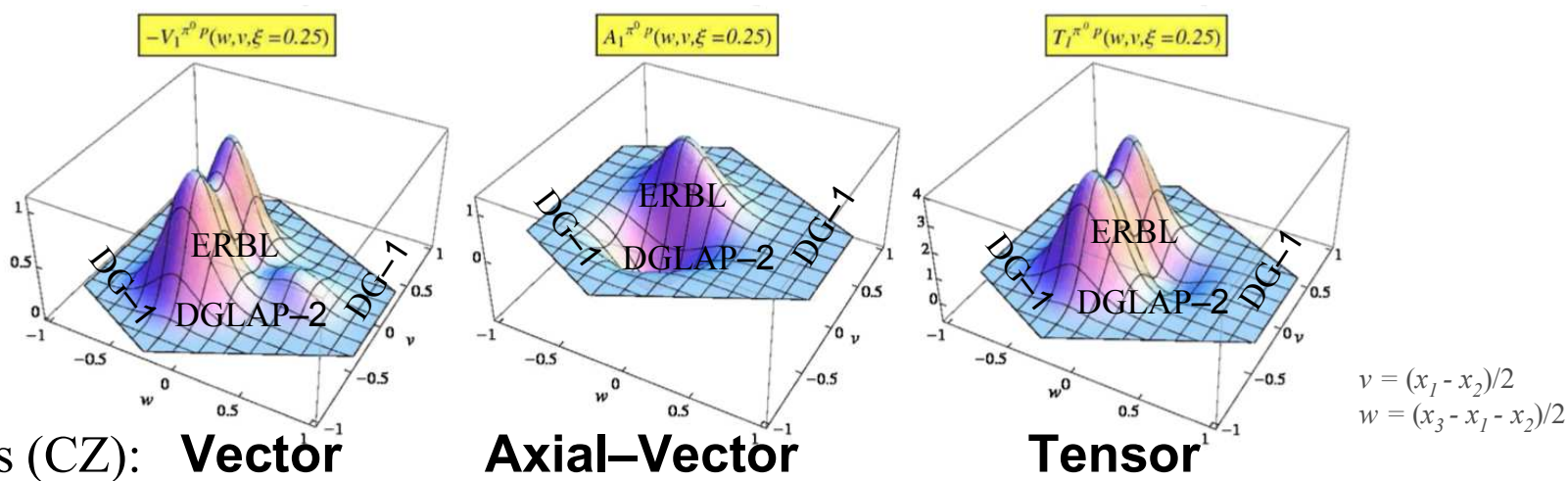
## Main reactions of interest to date:

- Backward angle exclusive  $\pi^0$ ,  $\pi^+$ ,  $\rho$ ,  $\omega$ ,  $\phi$  production
- Backward angle DVCS



## Interpretation of $\pi N$ TDAs in light-cone quark model

- Quark sea contrib to baryon wf (ERBL region)
- Minimal Fock states of baryon & meson (DGLAP-1) region
- Quark sea contribution to meson wf (DGLAP-2)



Model based on spectral representation w/ CZ sol for DA as input (function of quark-diquark coord)

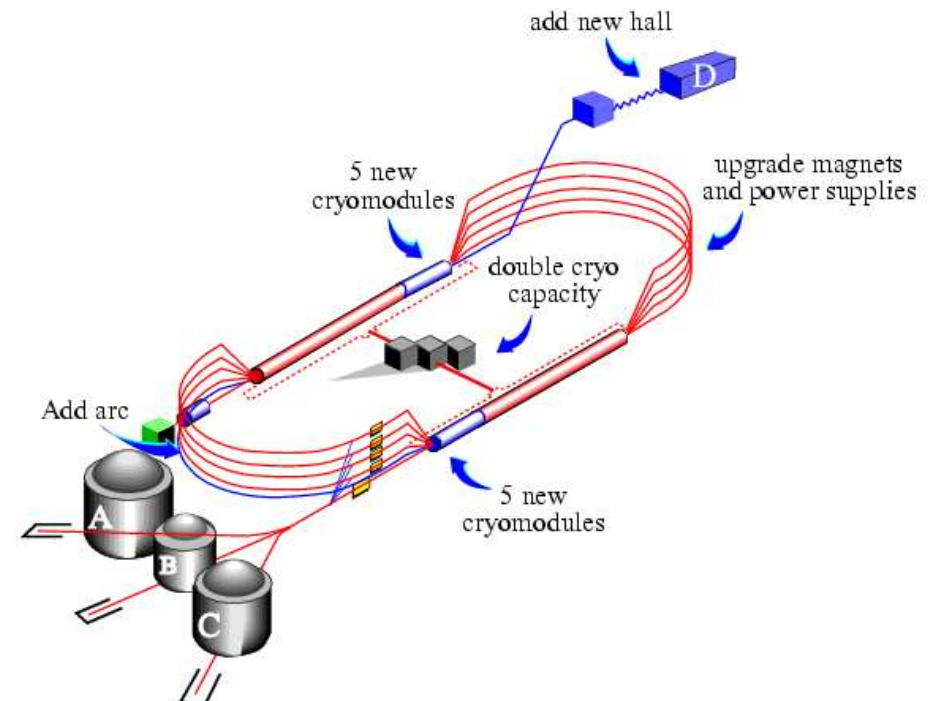


- **Kinematical regime for collinear factorization involving TDAs is similar to that involving GPDs:**
  - $x_B$  fixed
  - $|u|$ –momentum transfer small compared to  $Q^2$  and  $s$
  - $Q^2$  and  $s$  sufficiently large

## Two Key Predictions in Factorization Regime:

- **Dominance of transverse polarization** of virtual photon, resulting in suppression of longitudinal cross section by at least  $1/Q^2$ :  $\sigma_T \gg \sigma_L$
- Characteristic  $1/Q^8$ –scaling behavior of  $\sigma_T$  for fixed  $x_B$
- Early scaling for GPD physics occurs  $2 < Q^2 < 5 \text{ GeV}^2$ 
  - Maybe something similar occurs for TDA physics...

- Exclusive ERBL and DGLAP<sub>1,2</sub> regions are somewhat analogous to  $J/3q$ ,  $J+2q$ ,  $J+q$  exchange processes in SIDIS  $u$ -channel, could have different Junction contributions
- **Very difficult to selectively probe ERBL and DGLAP regions.** In an exclusive process, one has to exchange entire baryon in  $u$ -channel, and the problem is even more complicated than familiar deconvolution problem for GPDs
  - **Only exception appears to be at high  $\xi_u$ , where DGLAP regions disappear, so dominant picture (e.g. for impact parameter interpretation) is ERBL based one**
  - In general, JLab kinematics are expected to be more ERBL dominated, while EIC kinematics will be more DGLAP region
- Comparing exclusive  $u$ -channel processes for different final states (e.g.  $\pi^0$ ,  $\rho^0$ ,  $\omega$ ,  $\varphi$ ) might help disentangle any Junction contributions from hadron form factor parts



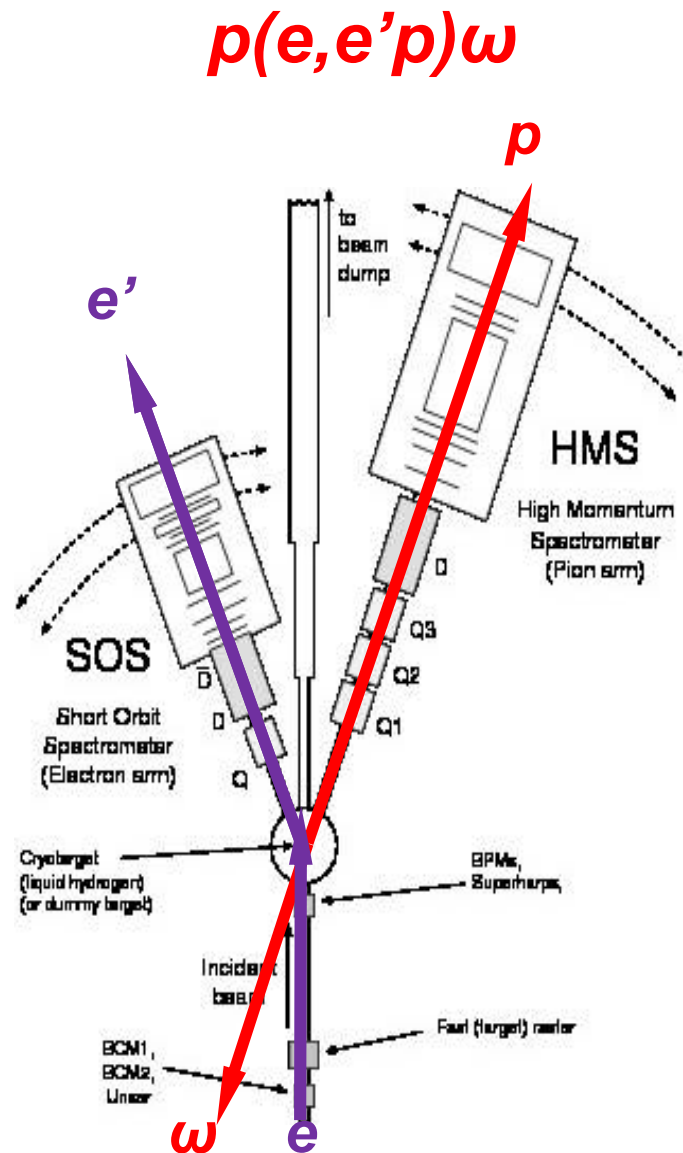
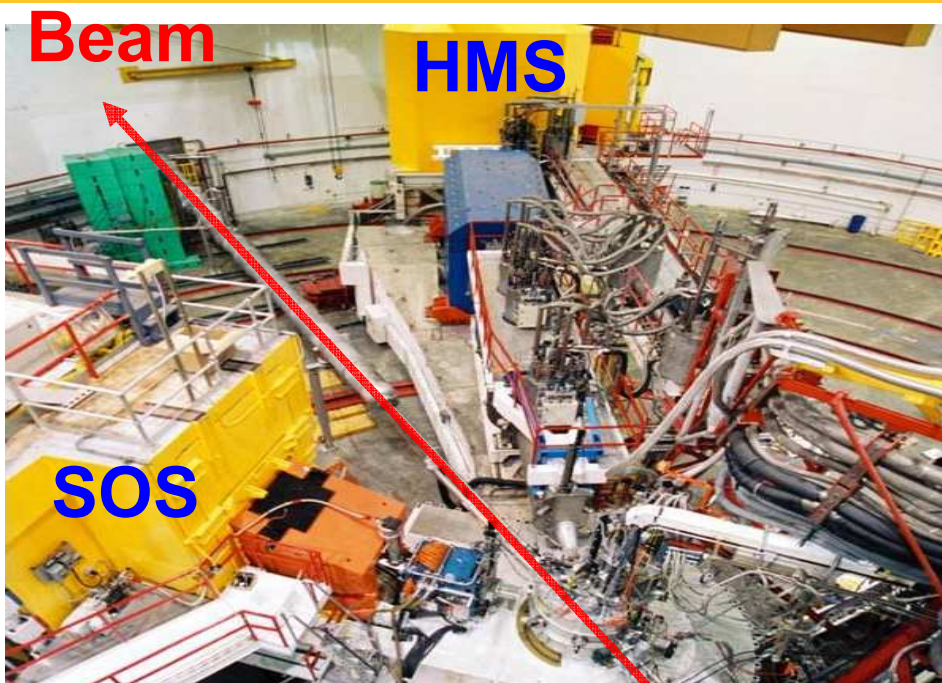
Two 1.5 GHz Superconducting Linear Accelerators provide electron beam for Nucleon & Nuclear structure studies.

- **Beam energy  $E \rightarrow 12$  GeV.**
- **Beam current  $>100 \mu\text{A}$ .**
- **Duty factor 100%, 85% polarization.**
- **Experiments in all 4 Halls can receive beam simultaneously.**



# “6 GeV” JLab Hall C Experimental Setup

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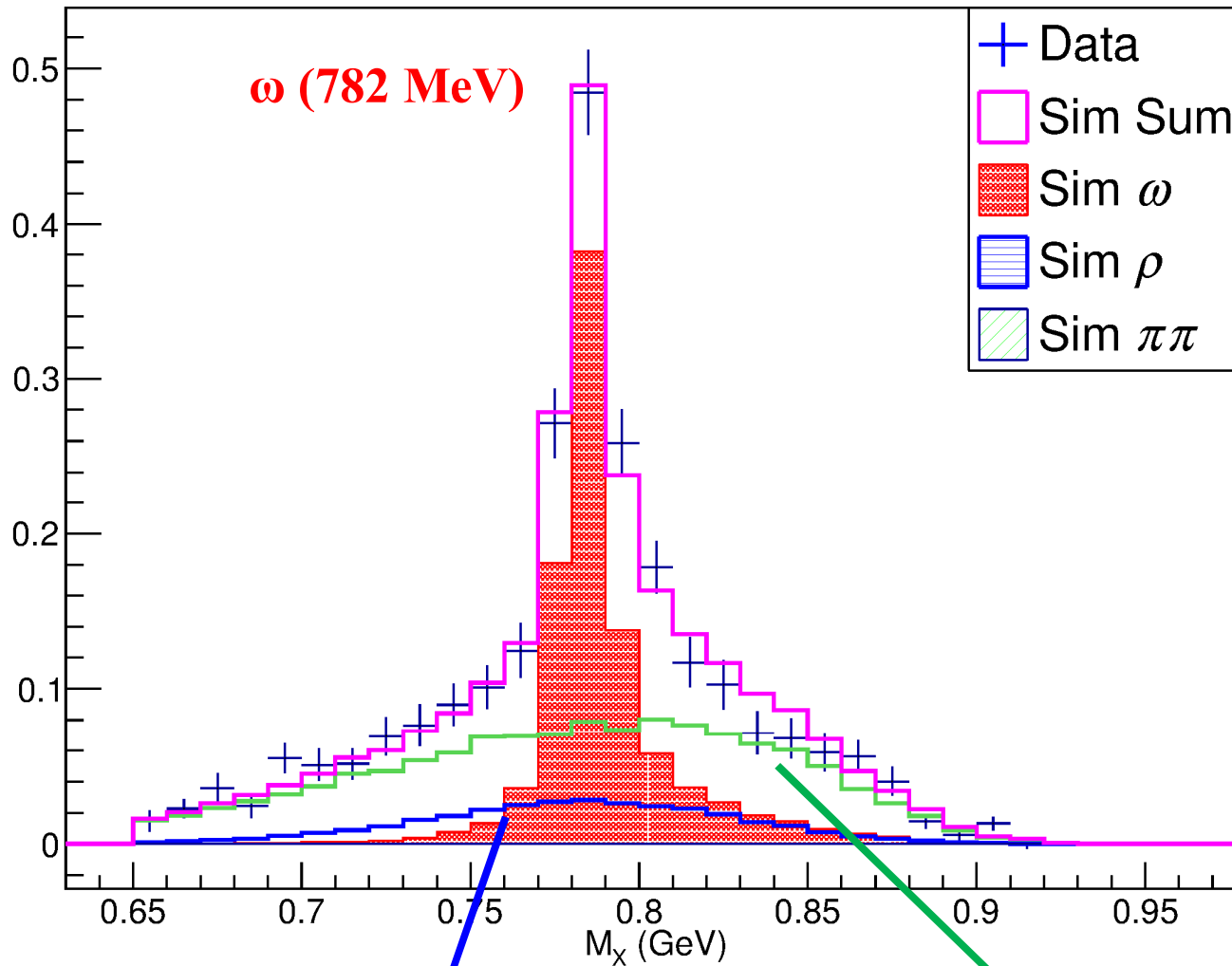


$E_e$ (GeV)	$\epsilon$	$-u$ (GeV <sup>2</sup> )	$-t$ (GeV <sup>2</sup> )	$\xi_u$	$\xi_t$
		$\langle Q^2 \rangle = 1.60 \text{ GeV}^2$		$\langle W \rangle = 2.21 \text{ GeV}$	
3.772	0.328	0.058 – 0.245	3.85	0.075 –	0.722 –
4.702	0.593		4.15	0.177	0.735
		$\langle Q^2 \rangle = 2.45 \text{ GeV}^2$		$\langle W \rangle = 2.21 \text{ GeV}$	
4.210	0.270	0.117 – 0.400	4.48	0.126 –	0.748 –
5.248	0.554		4.94	0.256	0.764

One of last analyses of Hall C 6 GeV era

# Physics Background Subtraction

$$M_x = \sqrt{(E_e + m_p - m_{e'} - E_p)^2 - (\vec{p}_e - \vec{p}_{e'} - \vec{p}_p)^2}$$



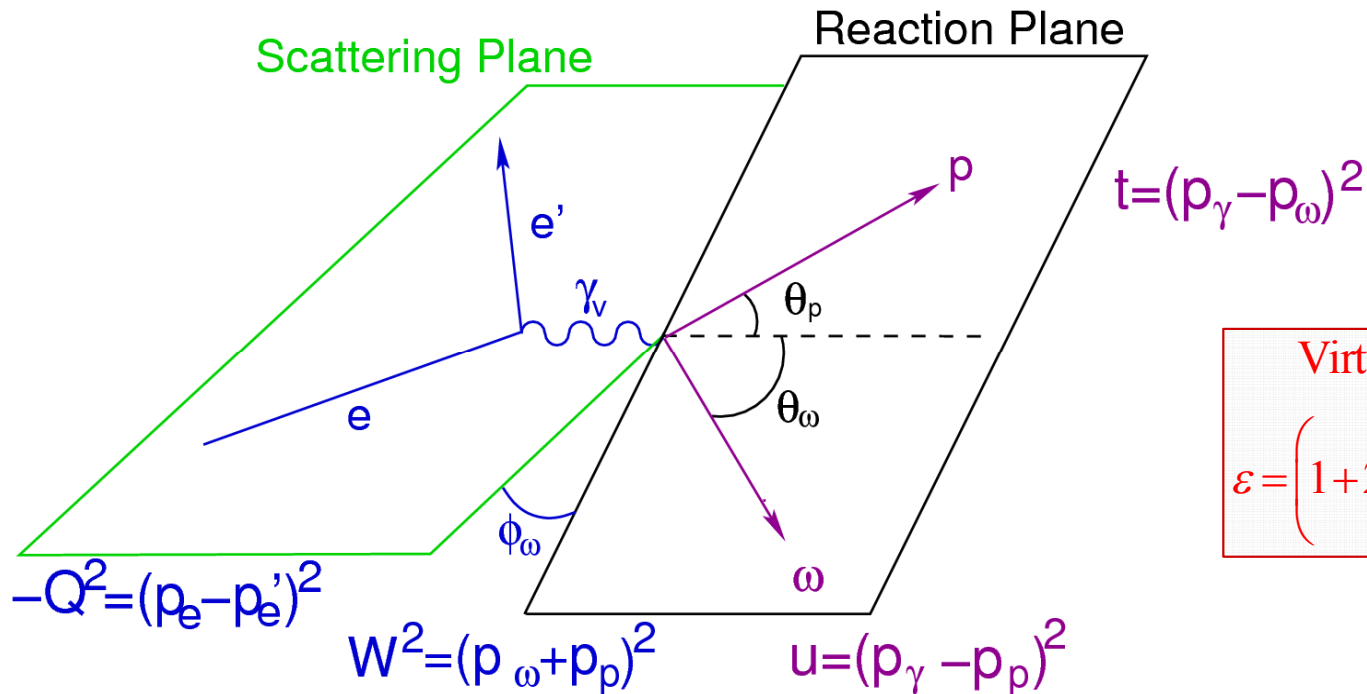
$\omega$  (782 MeV)

$\rho$  (770 MeV)

$2\pi$  production  
phase-space

HERMES Empirical parameterization  
with Soding skewness factor

# Rosenbluth (L/T/LT/TT) Separation



Virtual-photon polarization:

$$\varepsilon = \left( 1 + 2 \frac{(E_e - E_{e'})^2 + Q^2}{Q^2} \tan^2 \frac{\theta_{e'}}{2} \right)^{-1}$$



$$2\pi \frac{d^2\sigma}{dt d\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

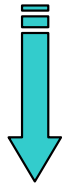
**Rosenbluth Separation requires:**

- Separate measurements at different  $\varepsilon$  (virtual photon polarization)
- All Lorentz invariant physics quantities:  $Q^2$ ,  $W$ ,  $t$ ,  $u$ , remain constant
- Beam energy, scattered  $e'$  angle and virtual photon angle will change as a result, event rates are dramatically different at high, low  $\varepsilon$

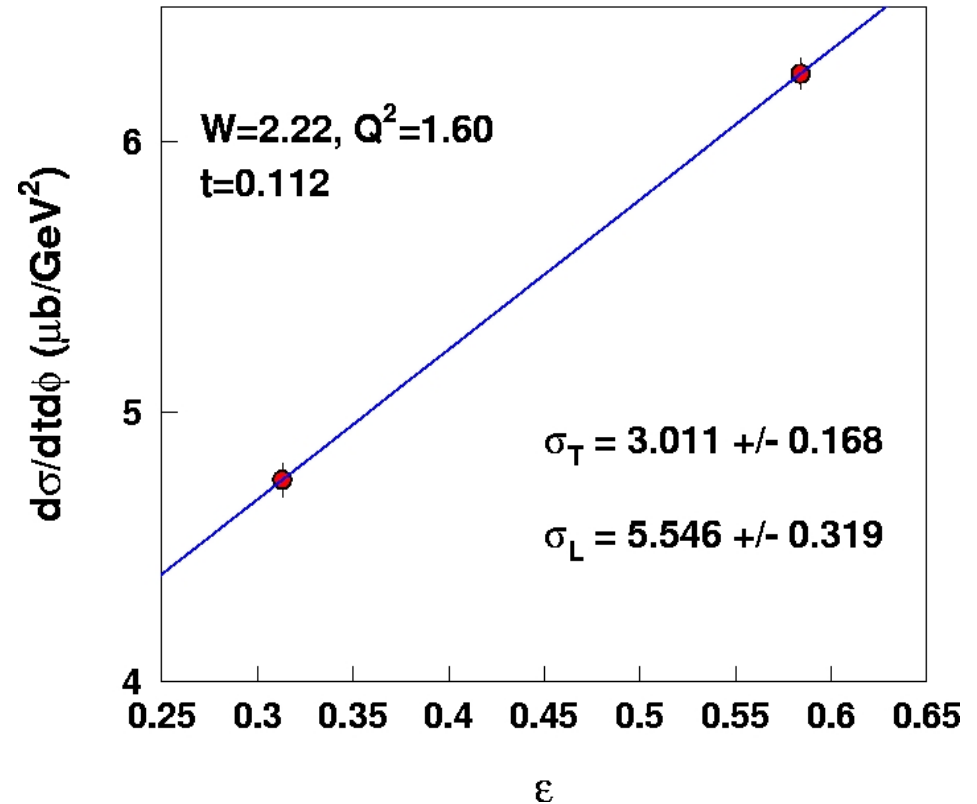
# “Simple” Longitudinal–Transverse Separation

- For **uniform**  $\phi$ -acceptance,  $\sigma_{TT}, \sigma_{LT} \rightarrow 0$  when integrated over  $\phi$
- Determine  $\sigma_T + \varepsilon \sigma_L$  for high and low  $\varepsilon$  in each  $u$ -bin for each  $Q^2$
- Isolate  $\sigma_L$ , by varying photon polarization,  $\varepsilon$

$$\varepsilon = [1 + 2(1 + \tau)\tan^2(\theta/2)]^{-1}$$

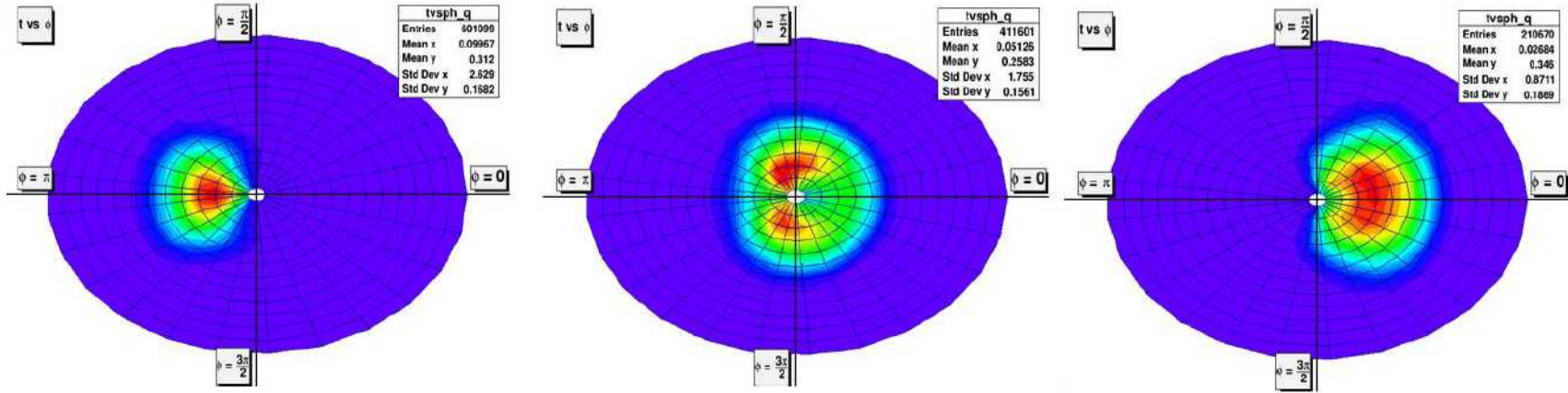


$$2\pi \frac{d\sigma}{dt d\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon + 1)} \frac{d\sigma_{LT}}{dt} \cos \phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$



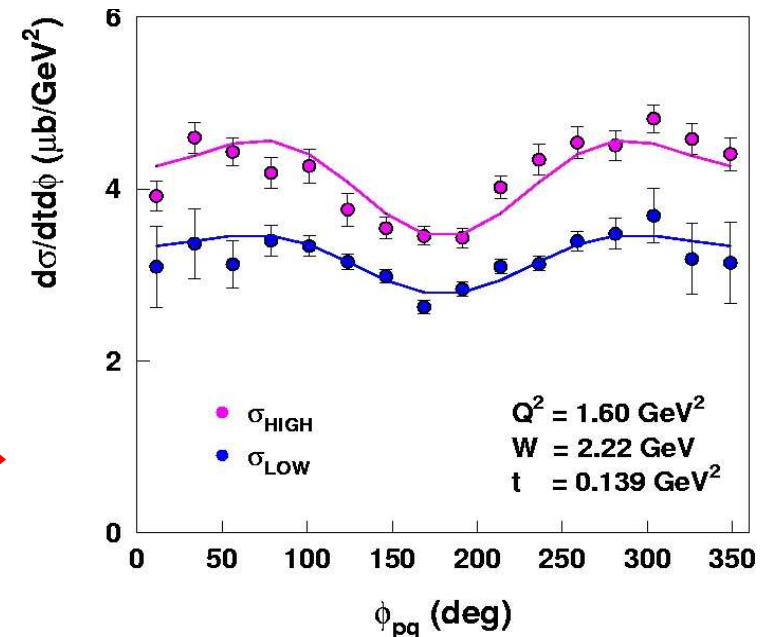
# “More Realistic” L/T Separation

$$2\pi \frac{d^2\sigma}{dtd\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$



## Cross-Section Determination:

- In reality,  $\phi$  acceptance not uniform
- Must measure  $\sigma_{LT}$  and  $\sigma_{TT}$
- Three hadron spectrometer angles needed for full azimuthal ( $\phi_p$ ) coverage to determine the interference terms
- Extract  $\sigma_L$  by simultaneous fit using measured azimuthal angle ( $\phi_p$ ) and knowledge of photon polarization ( $\varepsilon$ )

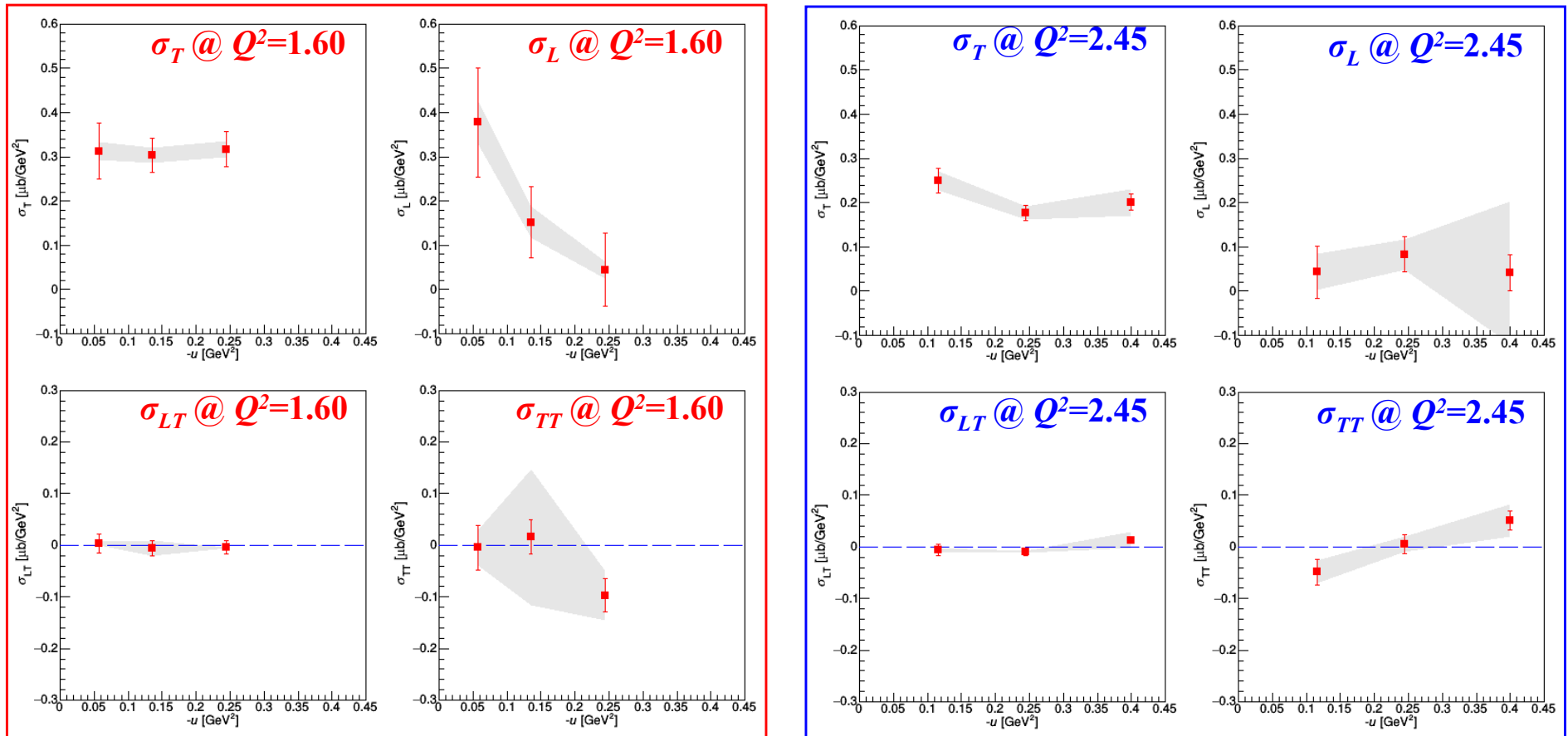




# Separated Cross Sections

$$\frac{d\sigma}{dt} \text{ VS } -u$$

## $p(e, e'p)\omega$



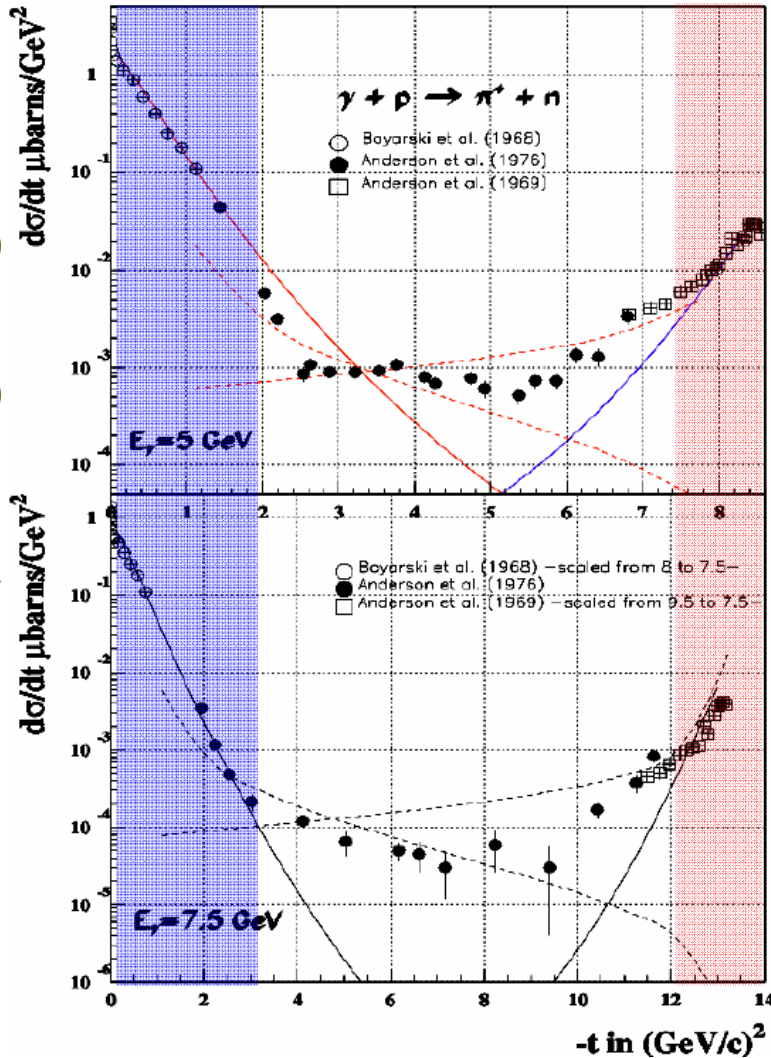
### Observations:

- $\sigma_T$  falls slowly with  $-u$ ;  $\sigma_L$  falls faster.
- $\sigma_{LT}$  is very small;  $\sigma_{TT}$  may sign flip for different  $Q^2$  values.

Error bars = statistical and uncorrelated syst. unc; Error bands = correlated syst. unc.

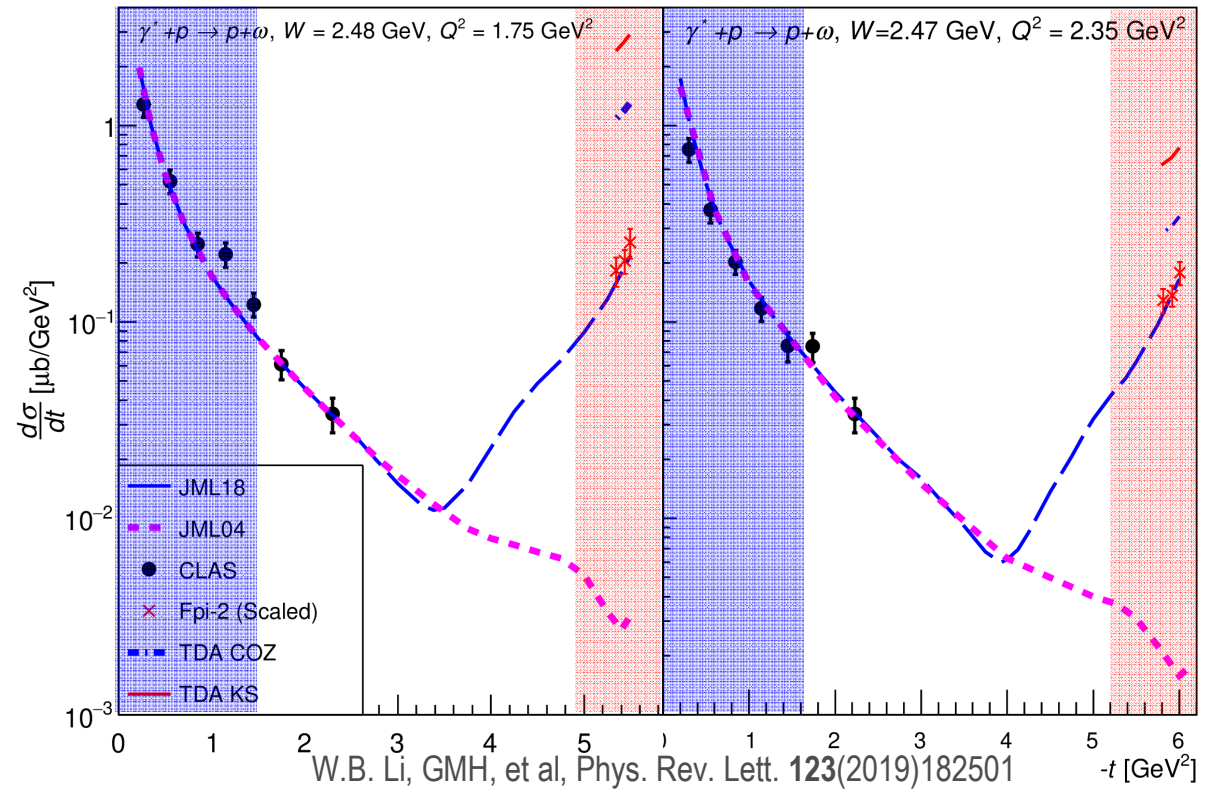
# Backward Angle Omega Electroproduction Peak

## Photoproduction



M. Guidal, J.-M. Laget, M. Vanderhaeghen, PLB 400(1997)6

## First observation of backward angle peak in electroproduction



Hall C data are scaled to match kinematics of Hall B data

	$W$ (GeV)	$x_B$	$Q^2$ (GeV <sup>2</sup> )	$-t$ (GeV <sup>2</sup> )	$-u$ (GeV <sup>2</sup> )
Hall B	1.8 – 2.8	0.16 – 0.64	1.6 – 5.1	< 2.7	> 1.68
Hall C	2.21	0.29	1.6	4.014	0.08 – 0.13
		0.38	2.45	4.724	0.17 – 0.24

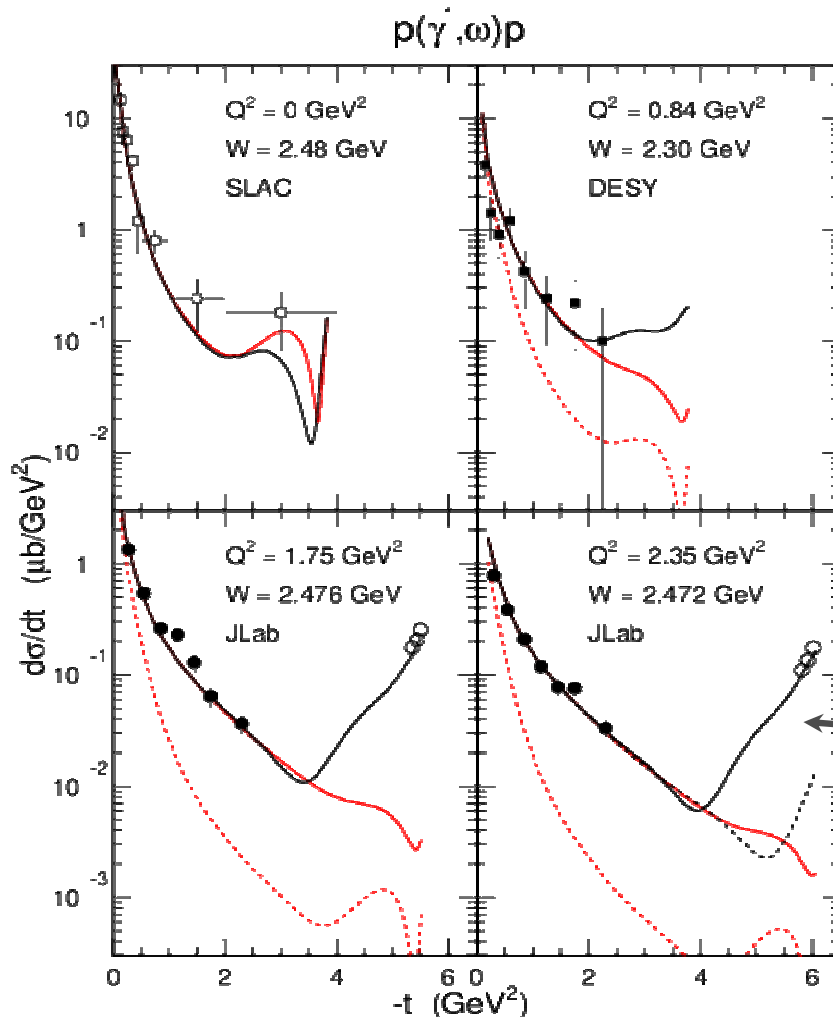
- In photoproduction, the ratio of the forward ( $t$ -channel) to backward ( $u$ -channel) peaks is  $\sim 100:1$
- The same was expected for electroproduction
  - It was thus a surprise when we observed the ratio of forward/backward peaks to be  $\sim 10:1$
- J.M. Laget (JML) has been able to provide a natural explanation for this surprisingly large ratio within the Regge model formalism
  - The L/T ratio for the backward peak can help distinguish various theoretical explanations, but JML model is not yet able to give such predictions
- Study of other exclusive channels over a broad kinematic range is needed to confirm whether strong backward peaks are ubiquitous or not

# JML Regge Model description of $u$ -Peak

- Model provides natural description of JLab  $\pi$  electroproduction cross sections without destroying good agreement at  $Q^2=0$ .

[PLB 685(2010)146; PLB 695(2011)1999]

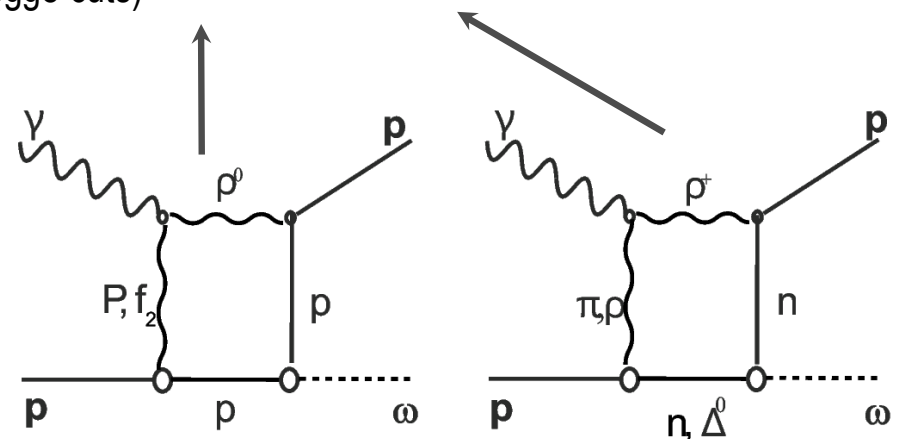
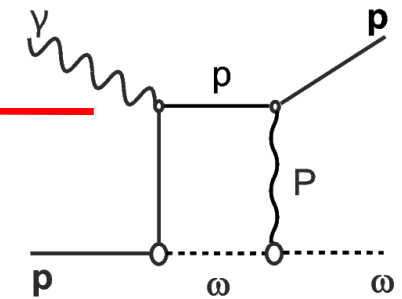
- Model also consistent with magnitude and slope of backward angle  $\omega$  peak.
- Would be interesting to examine L/T ratio predicted by model when full calc available.



J-M Laget, Private Communication (2018) and  
W.B. Li, GMH, et al., PRL 123(2019)182501

**Red line:** Non-degenerated Regge trajectory for  $N$ -exchange in  $u$ -channel w/  $t$ -dependent cutoff mass

**Black line:** Include  $\rho N$  and  $\rho \Delta$  rescattering inside nucleon (Regge cuts)



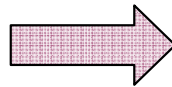
# $p(e, e'p)\omega$ $Q^2$ -Dependence

- To investigate  $Q^2$ -dependence, fit lowest  $-u$  bin values of  $\sigma_T$  and  $\sigma_L$  to  $Q^{-n}$  function

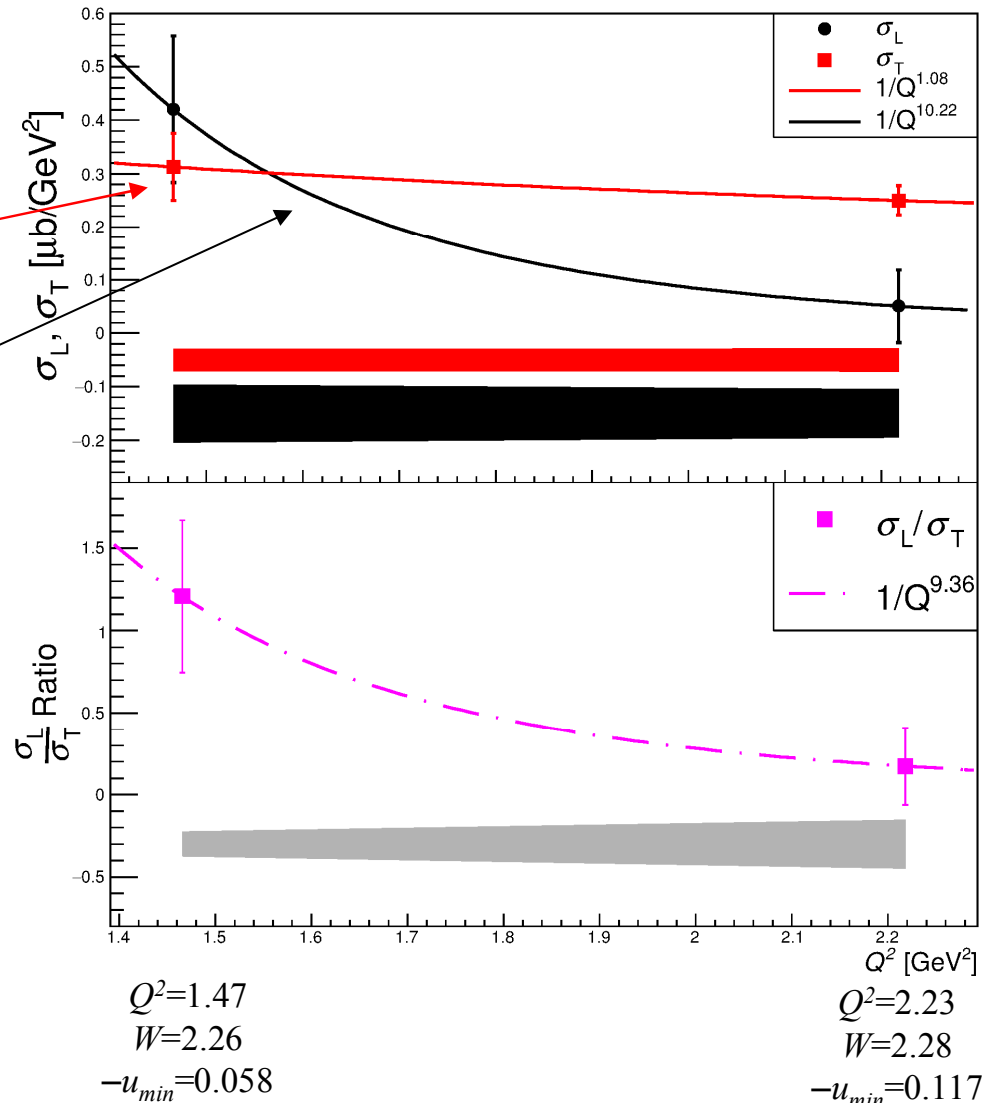
- $\sigma_T$  appears to have a flat  $Q^2$ -dependence within measured range
- $\sigma_L$  shows much stronger decrease

- **Decreasing L/T ratio indicates the gradual dominance of  $\sigma_T$  as  $Q^2$  increases.**

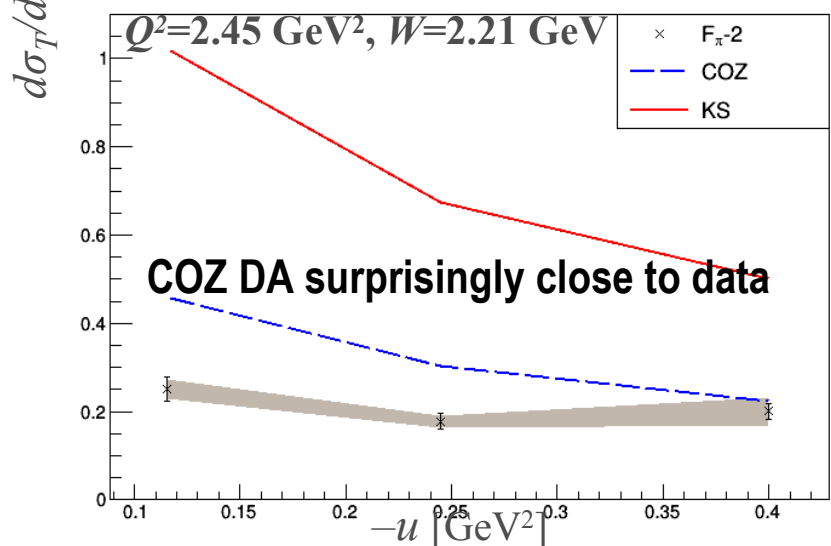
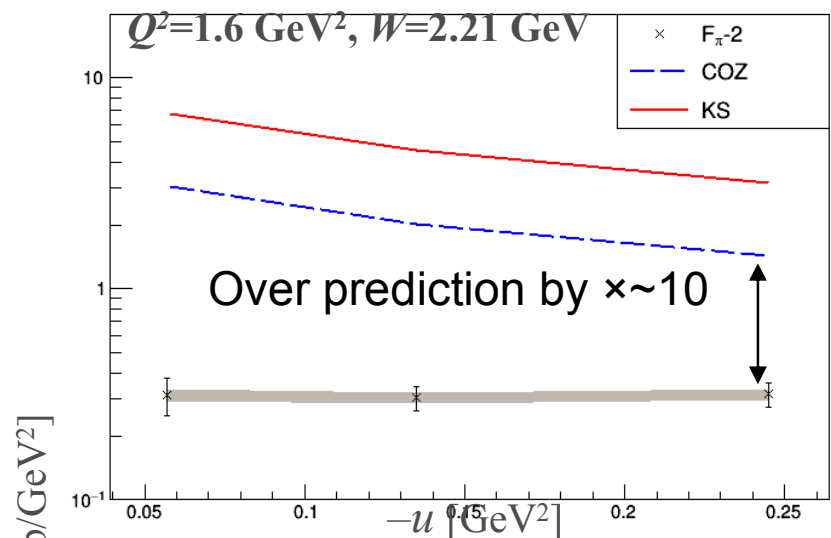
- Trend qualitatively consistent with prediction of TDA Collinear Factorization.



$$-u = -u_{min}$$



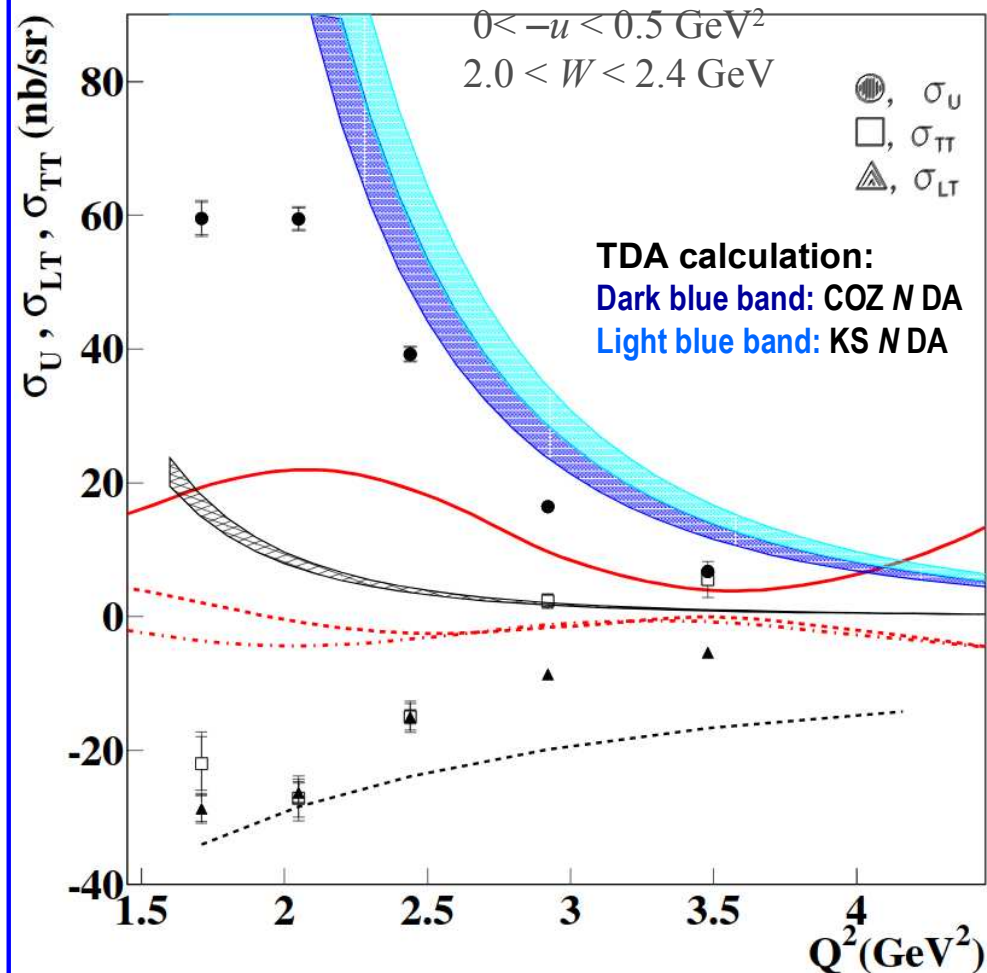
# TDA model Comparison to Data



TDA calculation by B. Pire, K. Semenov, L. Szymanowski  
W.B. Li, GMH, et al., PRL **123** (2019) 182501

Hall C  $\omega$  electroproduction

Both data sets suggestive of early  
TDA scaling  $Q^2 \approx 2.5 \text{ GeV}^2$  !?



Hall B  $\pi^+$  Electroproduction  
K. Park et al., PLB **780** (2017) 340

1. Determine if backward angle peak observed in exclusive  $\omega$  electroproduction occurs also in other channels, over a broad kinematic range.
2. Measure  $u$ -dependence of L/T-separated cross sections, to determine the relevance of Regge-rescattering and TDA mechanisms in JLab kinematics.
3. Assuming the backward angle peak is present, as expected, measure the  $\sigma_T/\sigma_L$  ratio over a wide  $Q^2$  range for  $W > 2$  GeV.
  - Where does  $\sigma_T \gg \sigma_L$ , as predicted by TDA formalism?
4. Determine the  $Q^2$ -dependence of  $\sigma_T$  at fixed  $x_B$ .
  - Where does  $\sigma_T \sim Q^{-8}$  as predicted by TDA formalism?

# JLab Hall C – 12 GeV Upgrade

## SHMS:

- 11 GeV/c Spectrometer
- Partner of existing 7 GeV/c HMS

## MAGNETIC OPTICS:

- Point-to Point QQD for easy calibration and wide acceptance.
- Horizontal bend magnet allows acceptance at forward angles ( $5.5^\circ$ )

## Detector Package:

- Drift Chambers
- Hodoscopes
- Cerenkovs
- Calorimeter

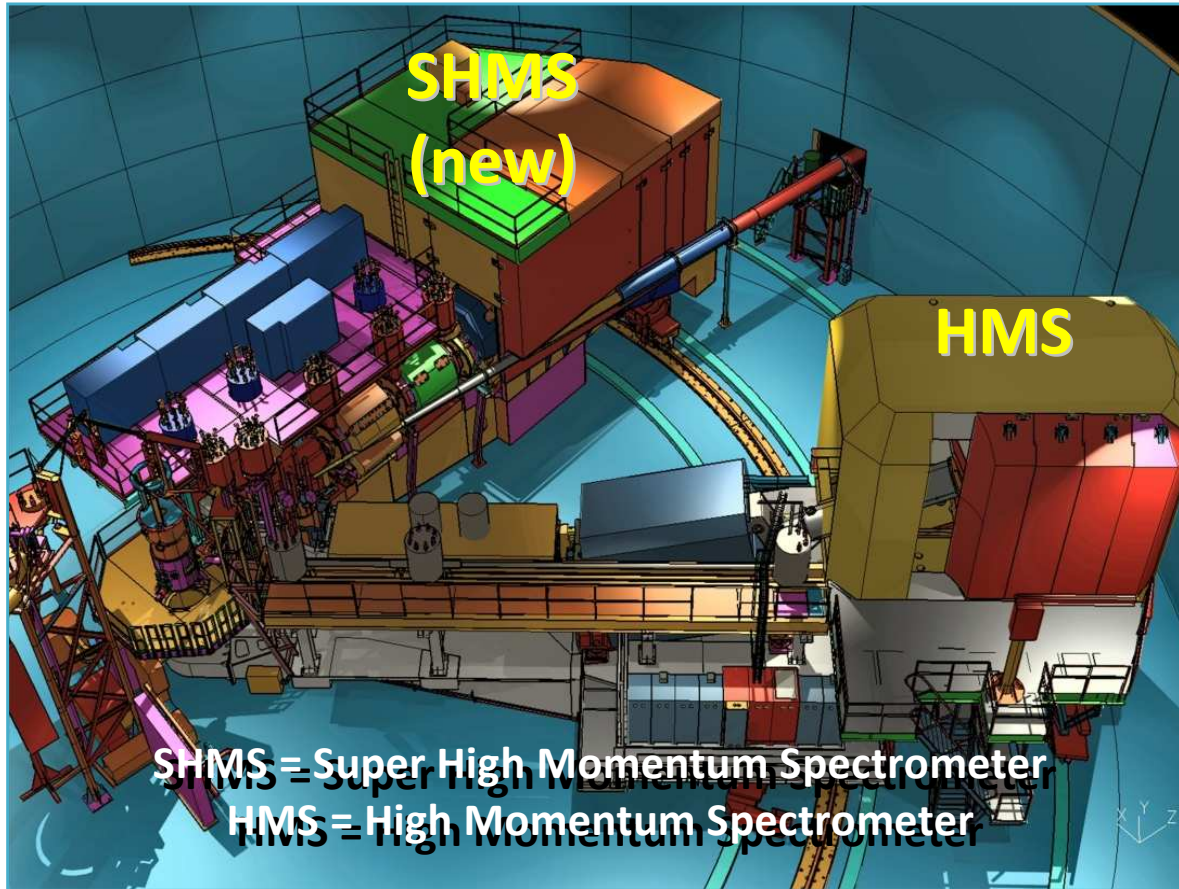
## Well-Shielded Detector Enclosure

## Rigid Support Structure

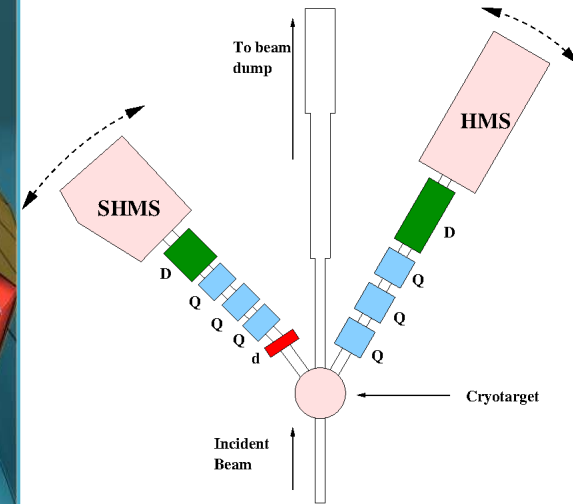
- Rapid & Remote Rotation
- Provides Pointing Accuracy & Reproducibility demonstrated in HMS

## Luminosity

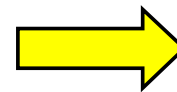
- $\sim 4 \times 10^{38} \text{ cm}^{-2} \text{ s}^{-1}$



SHMS = Super High Momentum Spectrometer  
 HMS = High Momentum Spectrometer



Upgraded Hall C has some similarity to SLAC End Station A, where the quark substructure of proton was discovered in 1968.

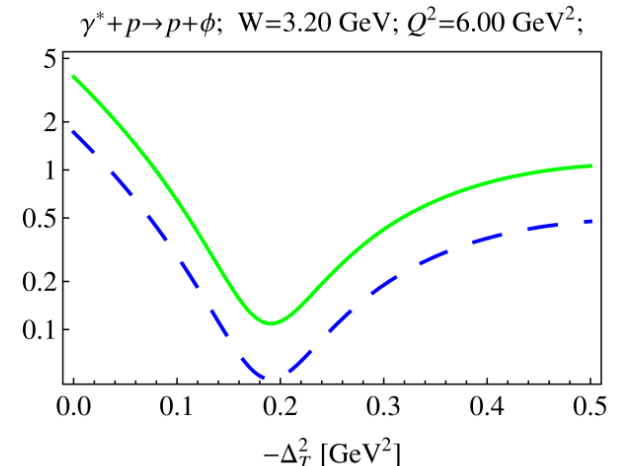
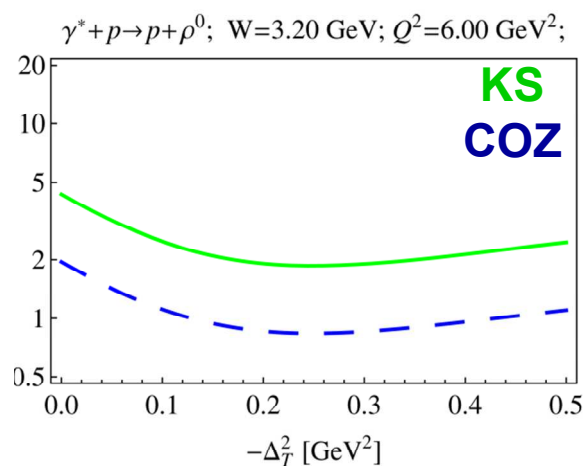
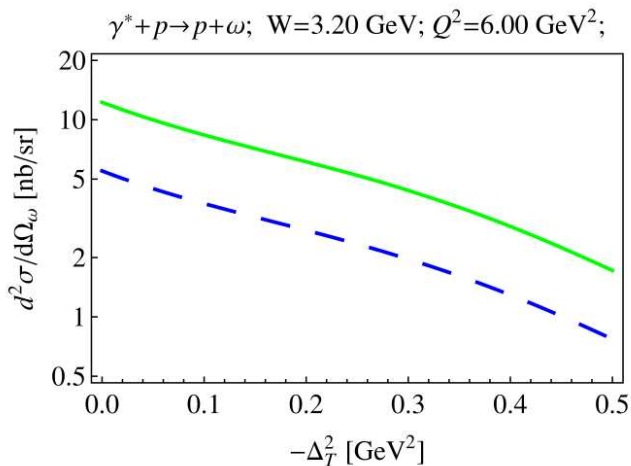




PionLT experiment (E12-19-006) L/T separations up to  $Q^2=8.5 \text{ GeV}^2$

Spokespersons: D. Gaskell, G.M. Huber, T. Horn

- Data acquired 2021-22
- L/T-Separations over wide kinematic range will allow  $\sigma_T \gg \sigma_L$  and  $1/Q^8$  scaling predictions to be checked with greater authority
- u-channel  $\phi$ -electroproduction particularly interesting
  - Sensitive to Strangeness content of nucleon
- Combined analysis of  $\rho$ ,  $\omega$  production allows one to disentangle isotopic structure of  $VN$  TDAs in non-strange sector

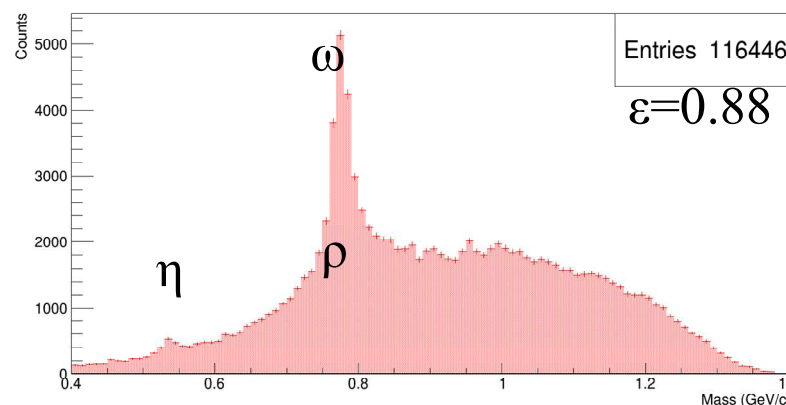
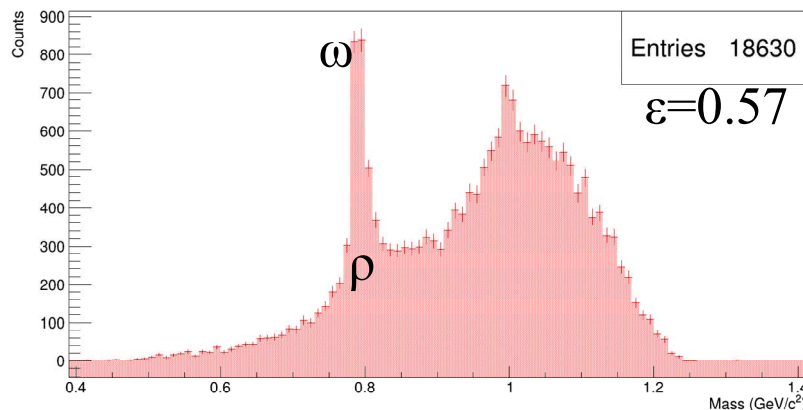


At  $Q^2=6.0 \text{ GeV}^2$ ,  $\omega$  predicted to remain dominant (unlike  $t$ -channel),  $\phi$  to drop rapidly with  $-u$ .

# Example “12 GeV” data already acquired

## $p(e,e'p)X$ Online Data Analysis

$$Q^2=3.00 \quad W=2.32 \quad \theta_{pq}=+3.0^\circ \quad -u=0.15 \quad \xi_u=0.15$$



Plots by Stephen Kay

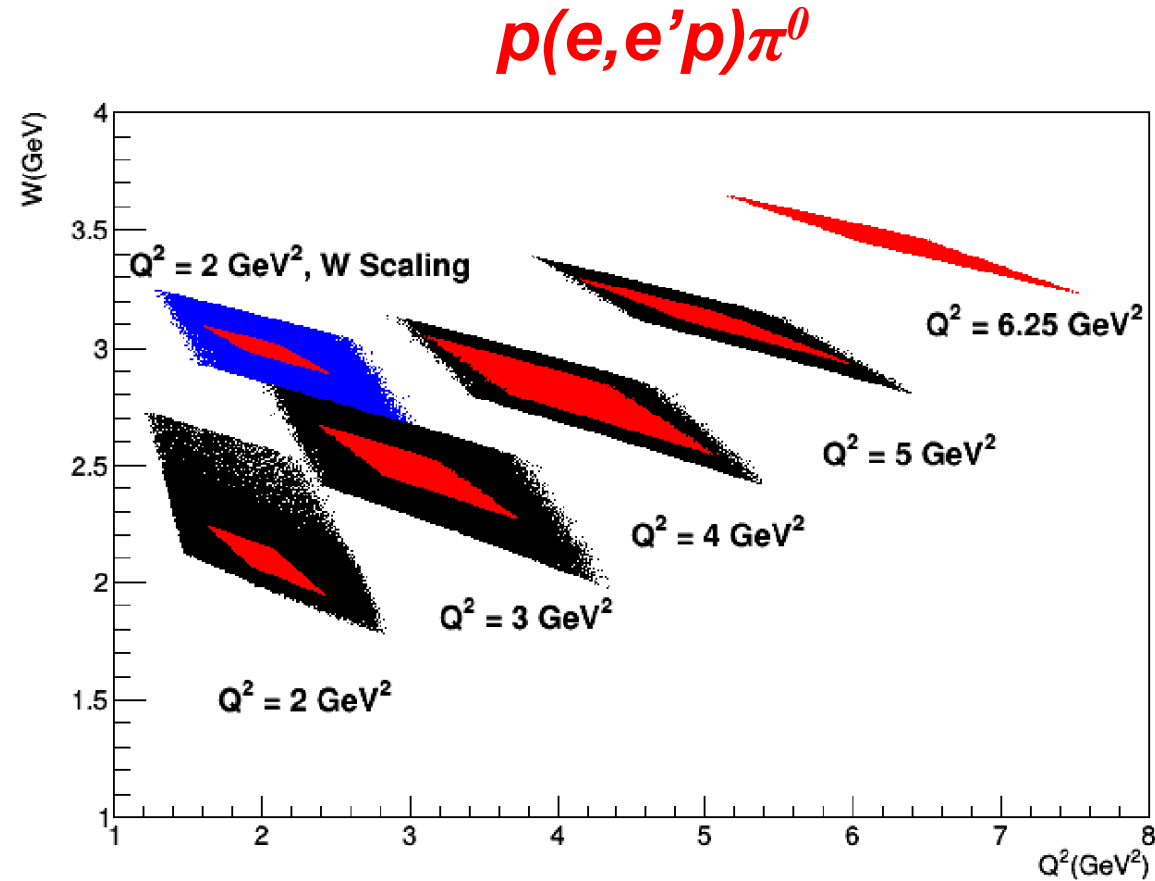
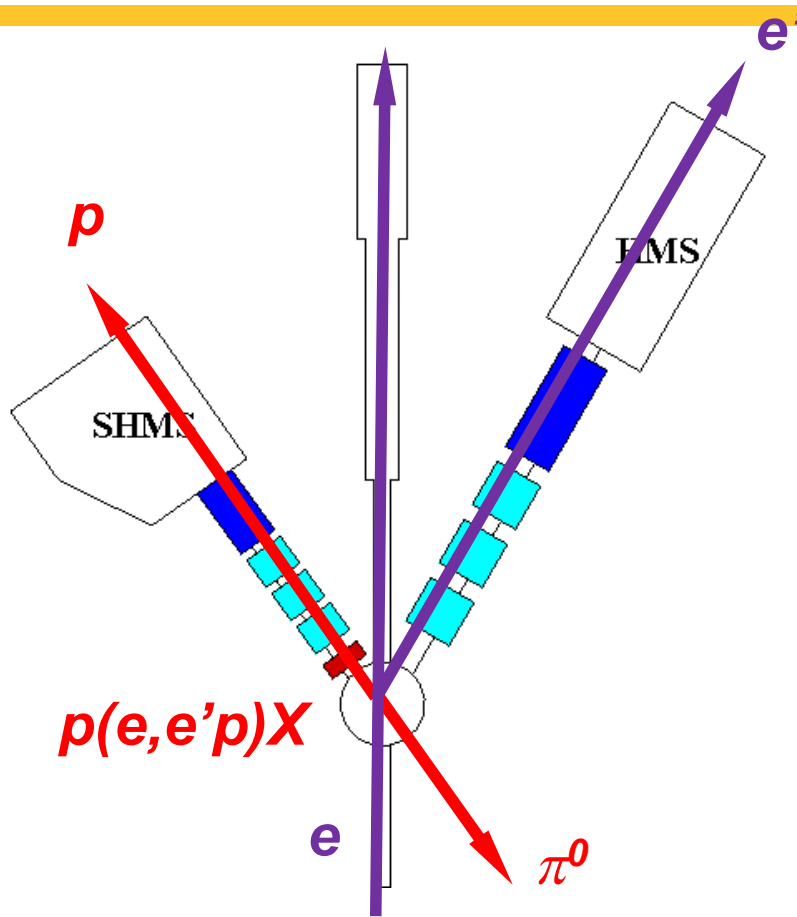
## $K^+$ L/T–experiment (E12–09–011)

Spokespersons: T. Horn, G.M. Huber, P. Markowitz

- Data acquired 2018–19
- Abundant  $u$ –channel  $p(e,e'p)X$  data acquired will allow backward angle studies over a wide kinematic range
- Planned first extraction of Beam Spin Asymmetry for  $u$ –channel reactions (PhD student: Alicia Postuma)

Setting	Low $\epsilon$ data	High $\epsilon$ data
$Q^2=0.50$ $W=2.40$	✓	✓
$Q^2=2.1$ $W=2.95$	✓	✓
$Q^2=3.0$ $W=2.32$	✓	✓
$Q^2=3.0$ $W=3.14$	✓	✓
$Q^2=4.4$ $W=2.74$	✓	✓
$Q^2=5.5$ $W=3.02$	✓	✓

# Backward Exclusive $\pi^0$ Production



## E12-20-007: $u \approx 0$ $\pi^0$ production in Hall C

Spokespersons: W.B. Li, G.M. Huber, J. Stevens

**Purpose:** test applicability of TDA formalism for  $\pi^0$  production

- Is  $\sigma_T$  dominant over  $\sigma_L$ ?
- Does the  $\sigma_T$  cross section at constant  $x_B$  scale as  $1/Q^8$ ?
- Kinematics overlap forward angle  $p(e, e'\pi^0)p$  experiment with NPS+HMS
- Beam time possible for 2025-26

- Backward angle kinematics match forward angle experiment using NPS currently running in Hall C
  - **DVCS/ $\pi^0$  E12-13-010** (Spokespersons: *T. Horn, C. Hyde, C. Munoz-Camacho, R. Paremuzyan, J. Roche*)
- Combination of both experiments will allow forward/backward peak ratio to be measured for  $\pi^0$  electroproduction for first time

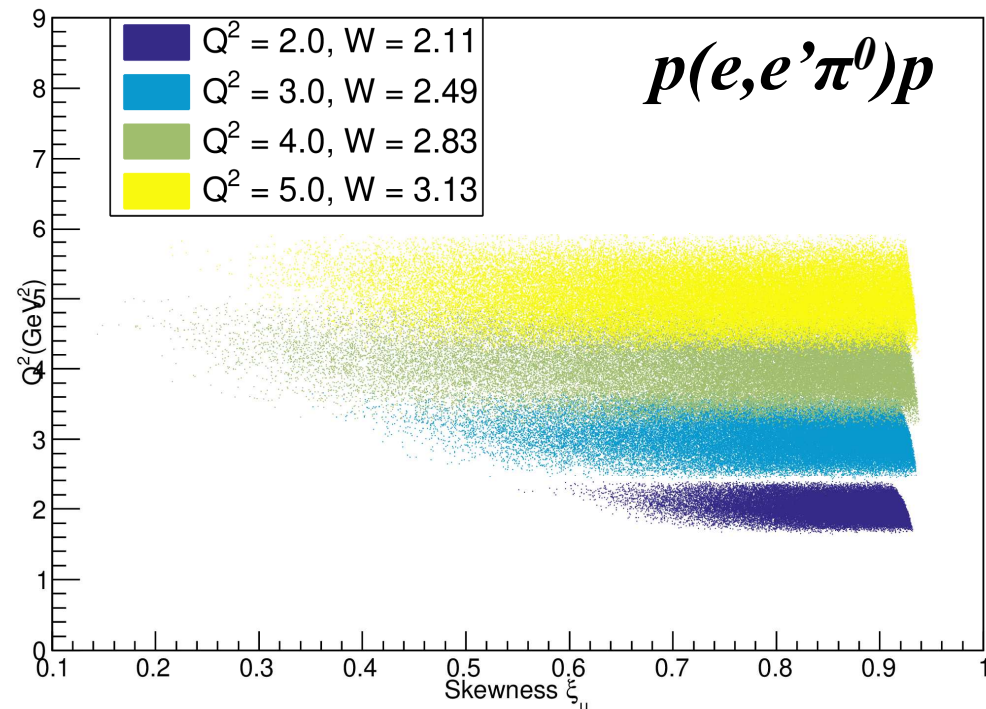
E12-20-007 covers a broad range in skewness, approaching  $\xi_u \rightarrow 1$ , which is ERBL dominated



L/T-separations planned for fixed  $x_B=0.36$  at:

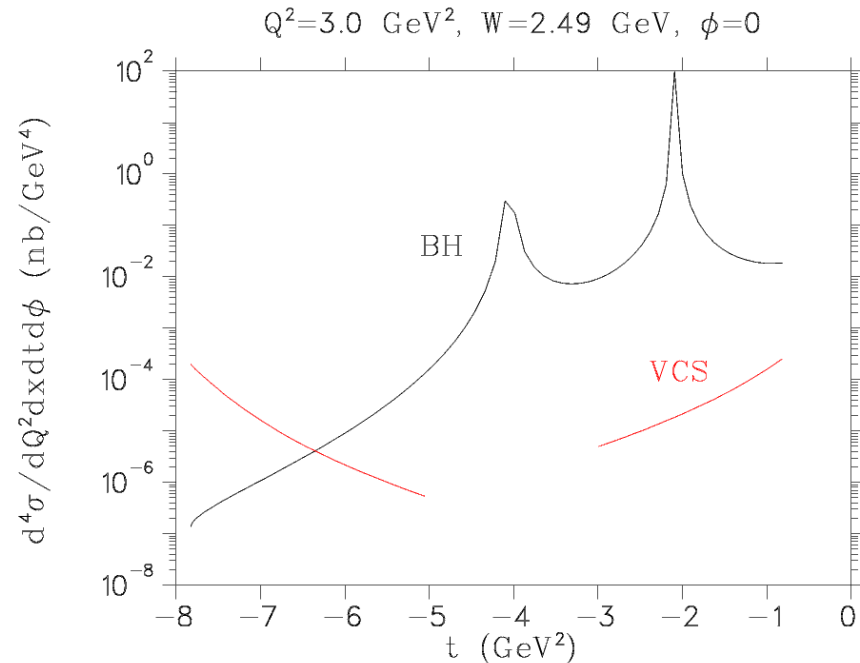
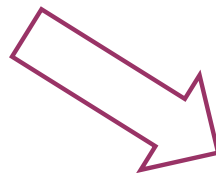
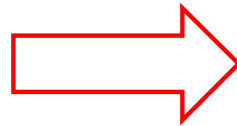
$Q^2$	2.0	3.0	4.0	5.5*
$W$	2.11	2.49	2.83	3.26*

\* Low  $\varepsilon$  only possible for  $\theta_{pq}=+1.64^\circ$

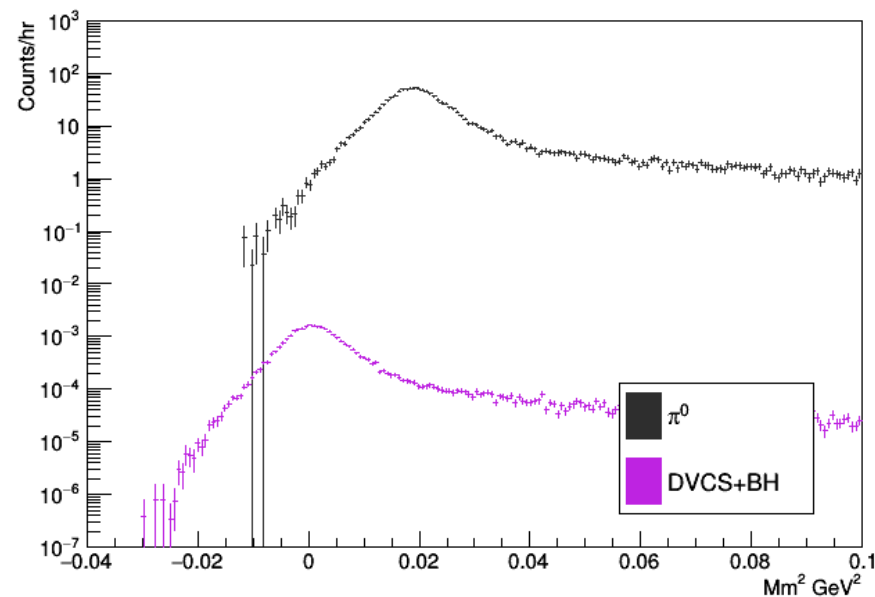


# $\pi^0$ Channel Expected to be Clean

- In comparison to backward-angle  $\omega$  electroproduction, there is little physics background in  $\pi^0$  production.
- Bethe-Heitler process has no backward-angle peak, and will be negligible.
- Virtual Compton Scattering (VCS) should dominate backward-angle  $\gamma$  production, but is expected to be much smaller than  $\pi^0$  production.



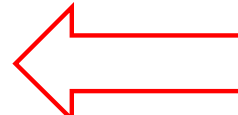
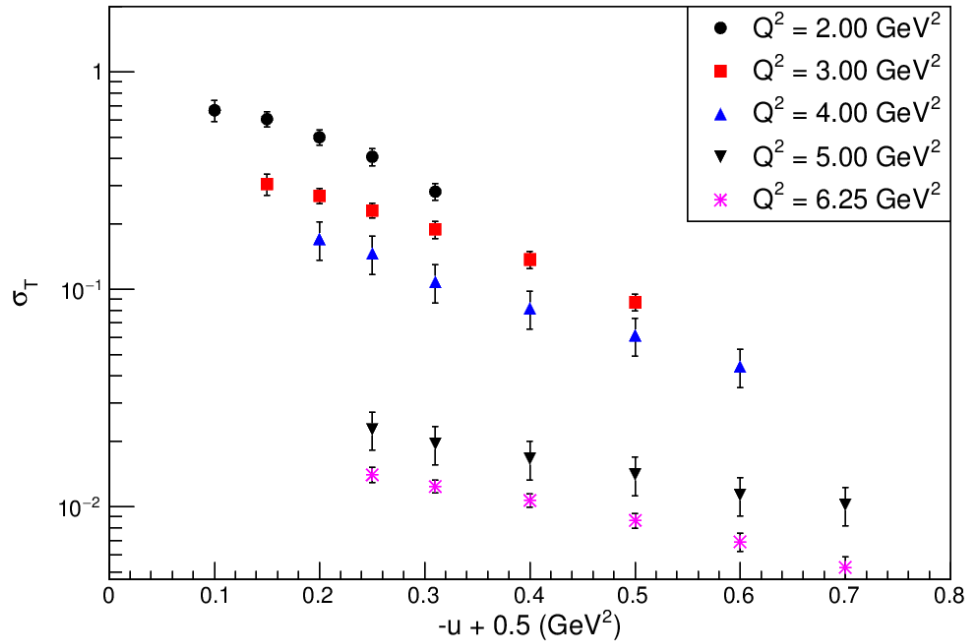
SHMS+HMS  $Q^2=3.0$  Simulation



BH+VCS simulations based on code by P. Guichon and M. Vanderhaeghen.

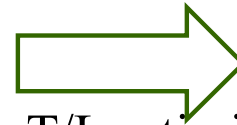
- BH calculation is exact.
- VCS calculation makes use of ad-hoc ansatz based on  $u$ -channel  $\omega$  data.

# E12-20-007 Projected Data Quality

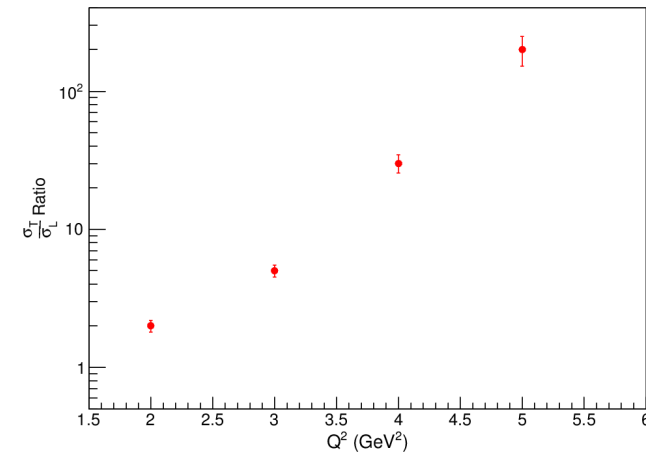


**Projected SHMS+HMS  $u$ -coverage and uncertainties at each  $Q^2$ .**

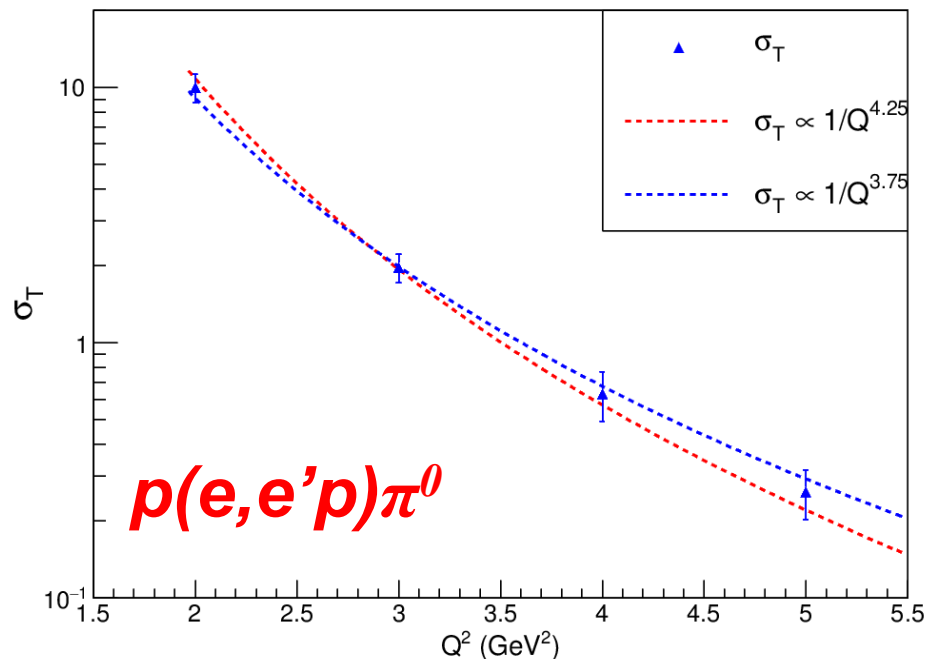
- L/T separations for comparison with Regge and TDA model calculations.
- $\sigma_T$  units are arbitrary.



T/L ratio is expected to be large.



**Projected uncertainty in  $Q^{-n}$ , which could be used to test TDA prediction:  $\sigma_T \sim Q^{-8}$ .**



- **New experimental technique pioneered at JLab Hall C has opened up a unique kinematic regime for study:**
  - Extreme backward angle ( $u \approx 0$ ) scattering
  - Detect forward-going proton in parallel kinematics, leaving “recoil” meson nearly-at-rest in target
- Possible access to **Transition Distribution Amplitudes**
  - Universal perturbative objects in  $u$ -channel, analogous to Generalized Parton Distributions (GPDs)
  - Access to 3-quark plus sea component  $\psi_{(3q+q\bar{q})}$  of nucleon
- **J.-M. Laget Regge Model** provides natural explanation of magnitude and  $u$ -slope of observed backward angle peak
  - $\sigma_L/\sigma_T$  separations will be essential to distinguish between alternate theoretical descriptions
- **Color Transparency (CT) also is a signal of factorization** and can be used to distinguish Regge and TDA explanations (see our LOI12-23-009)
  - Does Baryon Junction predict absence of  $u$ -channel CT? If so, the comparison would be interesting