

The π^+ electromagnetic form factor at Jefferson Lab and future EIC



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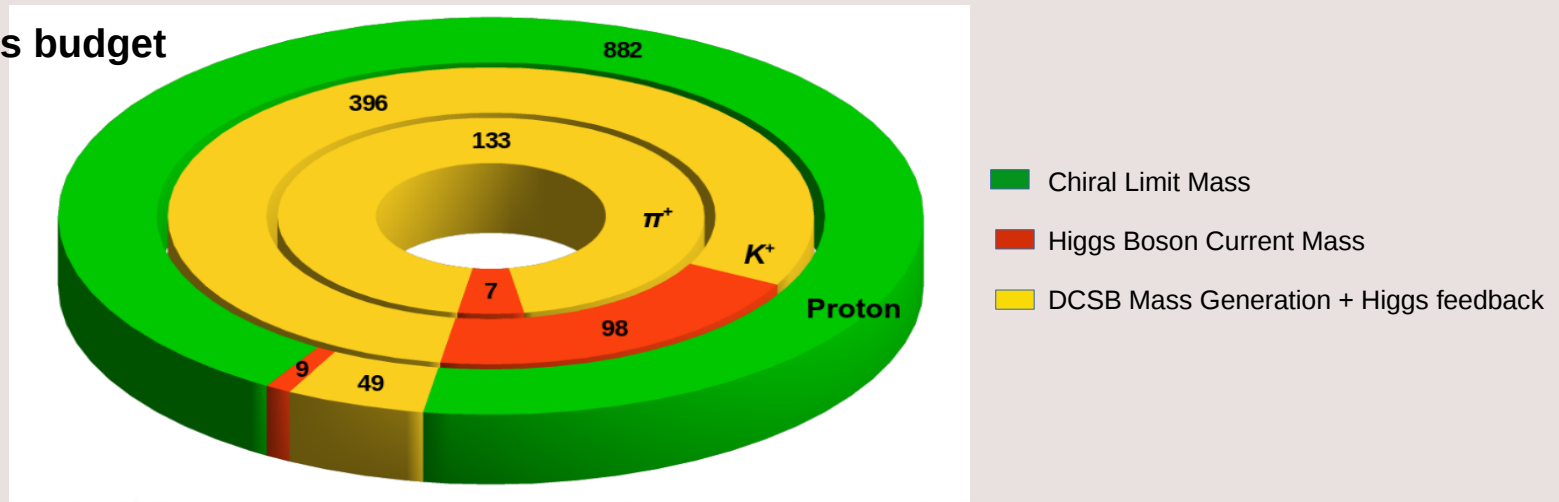
February 09, 2024

Dynamics of Gluons in QCD

- **How does the mass of nucleon arise?**
- **How does the spin of nucleon arise?**

Hope EIC answers

Hadron mass budget



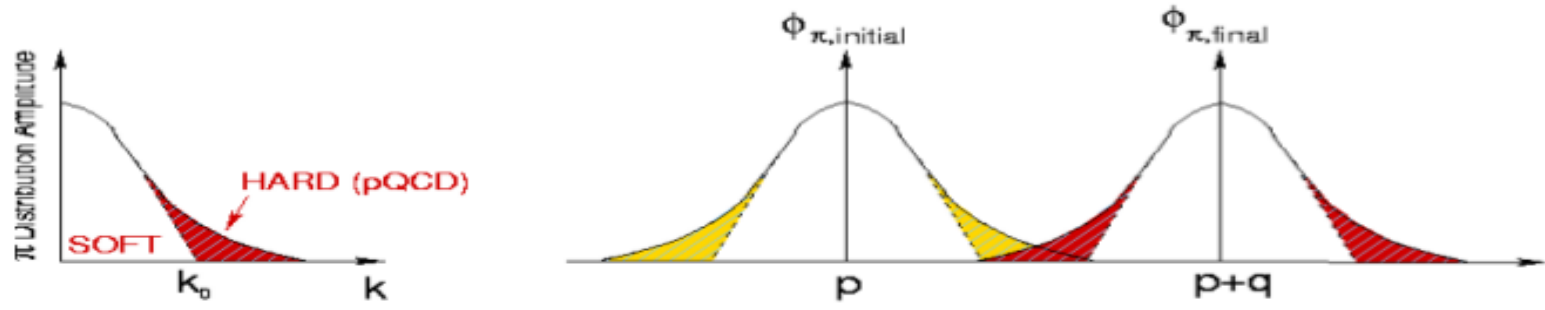
- **The Higgs mechanism is not sufficient to answer the questions!!!**
- **Dynamical Chiral Symmetry Breaking (DCSB)** is expected to provide most of the hadron mass.
- The π and K are pivotal to utilize in understanding **DCSB**.
 - π the lightest quark system, responsible for the long range character of the strong interaction.
 - K structure is involved with the strange quark.
 - π and K are connected to the Goldstone modes of **DCSB**.

Charged Meson Form Factors

Simple $q\bar{q}$ valence structure of mesons presents the ideal testing ground for our understanding of bound quark systems.

In quantum field theory, the form factor is the overlap integral:

$$F_\pi(Q^2) = \int \phi_\pi^*(p) \phi_\pi(p+q) dp$$



The meson wave function can be separated into φ_π^{soft} with only low momentum contributions ($k < k_0$) and a hard tail φ_π^{hard} .

While φ_π^{hard} can be treated in pQCD, φ_π^{soft} cannot.

From a theoretical standpoint, the study of the Q^2 -dependence of the form factor focuses on finding a description for the hard and soft contributions of the meson wave-function.

Slide's credit to Garth Huber

The Pion in Perturbative QCD

At very large Q^2 , pion form factor (F_π) can be calculated using pQCD

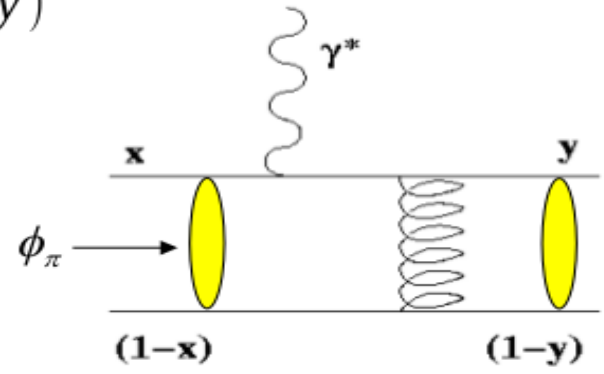
$$F_\pi(Q^2) = \frac{4}{3} \pi \alpha_s \int dx dy \frac{2}{3} \frac{1}{xyQ^2} \phi(x) \phi(y)$$

at asymptotically high Q^2 , the pion distribution amplitude becomes

$$\phi_\pi(x) \xrightarrow{Q^2 \rightarrow \infty} \frac{3f_\pi}{\sqrt{n_c}} x(1-x)$$

and F_π takes the very simple form

$$Q^2 F_\pi(Q^2) \xrightarrow{Q^2 \rightarrow \infty} 16\pi \alpha_s(Q^2) f_\pi^2$$



$f_\pi = 93$ MeV is the $\pi^+ \rightarrow \mu^+ \nu$ decay constant.

G.P. Lepage, S.J. Brodsky, Phys.Lett. 87B(1979)359.

This only relies on asymptotic freedom in QCD, *i.e.* $(\partial\alpha_s/\partial\mu) < 0$ as $\mu \rightarrow \infty$.

$Q^2 F_\pi$ should behave like $\alpha_s(Q^2)$ even for moderately large Q^2 .

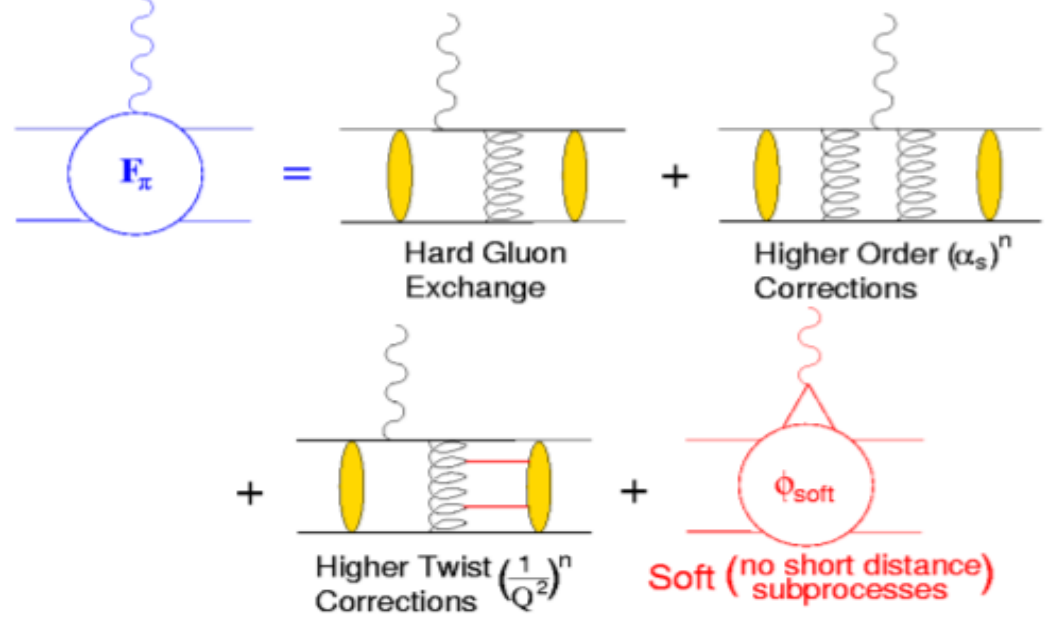
→ Pion form factor seems to be best tool for experimental study of nature of the quark–gluon coupling constant renormalization.

[A.V. Radyushkin, JINR 1977, arXiv:hep-ph/0410276]

Slide's credit to Garth Huber

The Pion Form Factor at Intermediate Q^2

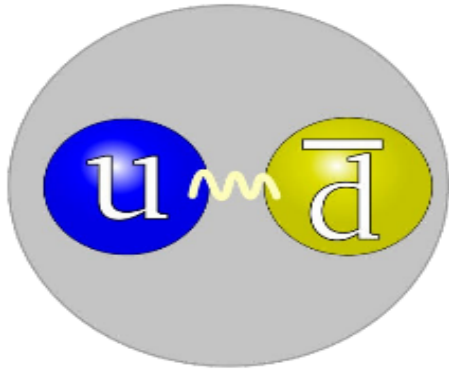
At experimentally-accessible Q^2 , both the “hard” and “soft” components (e.g. transverse momentum effects) contribute.



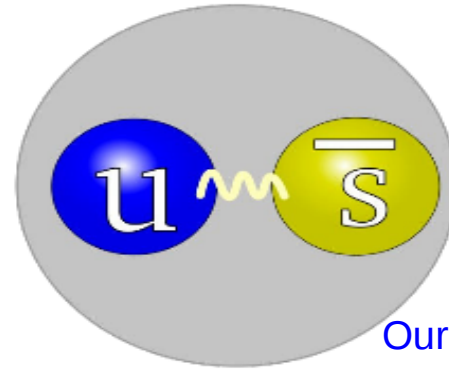
- **The interplay of hard and soft contributions is poorly understood.**
 - Different theoretical viewpoints on whether higher-twist mechanisms dominate until very large momentum transfer or not.
- **The pion elastic and transition form factors experimentally accessible over a wide kinematic range.**
 - A laboratory to study the **transition** from the soft to hard regime.

Slide's credit to Garth Huber

The Charged Kaon – a 2nd QCD Test Case



π^+



K^+

Our group has acquired experimental data for both π^+ and K^+ mesons. However, I will focus exclusively on the analysis of π^+ in this talk.

- In the hard scattering limit, pQCD predicts that the π^+ and K^+ form factors will behave similarly

$$\frac{F_K(Q^2)}{F_\pi(Q^2)} \xrightarrow{Q^2 \rightarrow \infty} \frac{f_K^2}{f_\pi^2}$$

- It is important to compare the magnitudes and Q^2 -dependences of both form factors.

Slide's credit to Garth Huber

Measurement of π^+ Form Factor – Low Q^2

At low Q^2 , F_π can be measured model-independently via high energy elastic π^- scattering from atomic electrons in Hydrogen

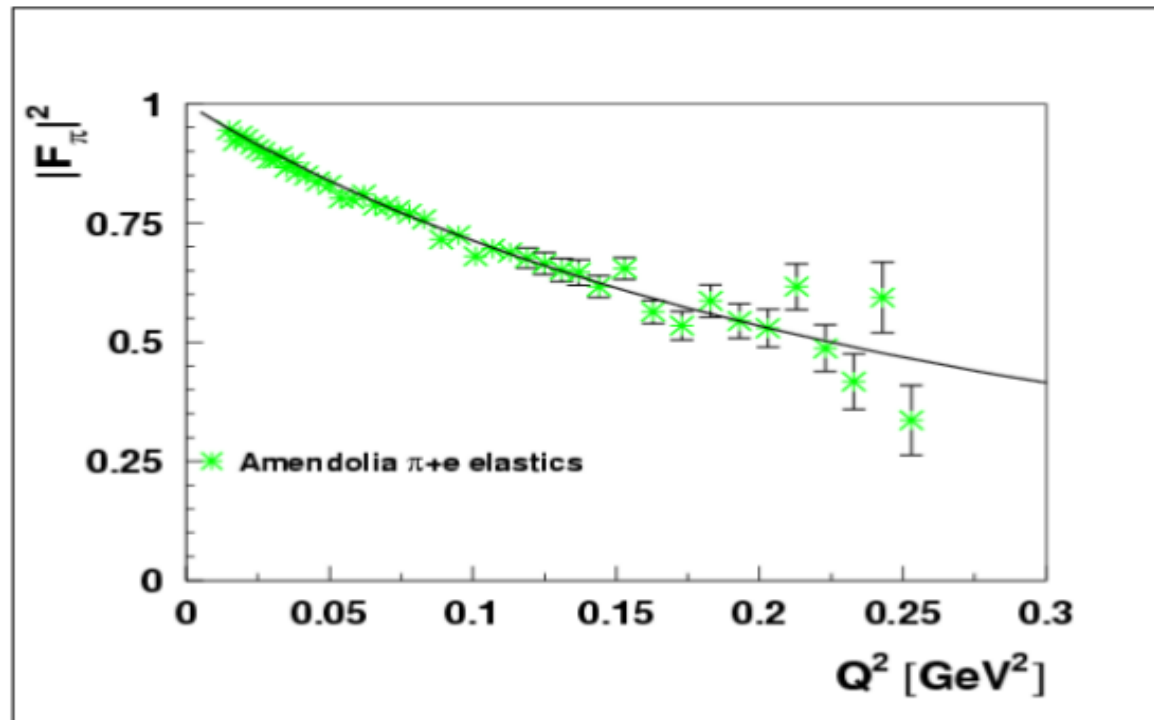
- CERN SPS used 300 GeV pions to measure form factor up to $Q^2 = 0.25 \text{ GeV}^2$ [*Amendolia, et al., NPB 277(1986)168*]

- Data used to extract pion charge radius

$$r_\pi = 0.657 \pm 0.012 \text{ fm}$$

Maximum accessible Q^2 roughly proportional to pion beam energy

$Q^2=1 \text{ GeV}^2$ requires 1 TeV pion beam



Slide's credit to Garth Huber

Measurement of F_π via Electroproduction (Indirect Technique)

Above $Q^2 > 0.3 \text{ GeV}^2$, F_π is measured indirectly using the “pion cloud” of the proton via pion electroproduction $p(e, e' \pi^+) n$

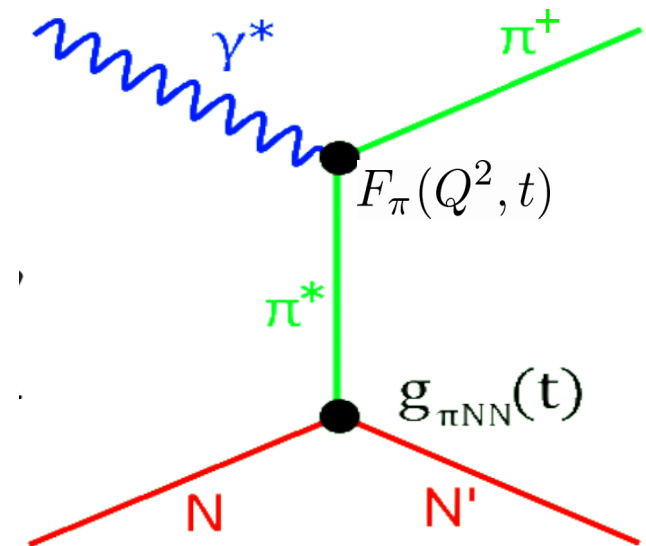
$$|p\rangle = |p\rangle_0 + |n\pi^+\rangle + \dots$$

- At small $-t$, the pion pole process dominates the longitudinal cross section, σ_L
- In Born term model, F_π^2 appears as

$$\frac{d\sigma_L}{dt} \propto \frac{-tQ^2}{(t - m_\pi^2)} g_{\pi NN}^2(t) F_\pi^2(Q^2, t)$$

Drawbacks of this technique:

1. Isolating σ_L experimentally challenging.
2. The F_π values are in principle dependent upon the model used, but this dependence is expected to be reduced at sufficiently small $-t$.



Slide's credit to Garth Huber

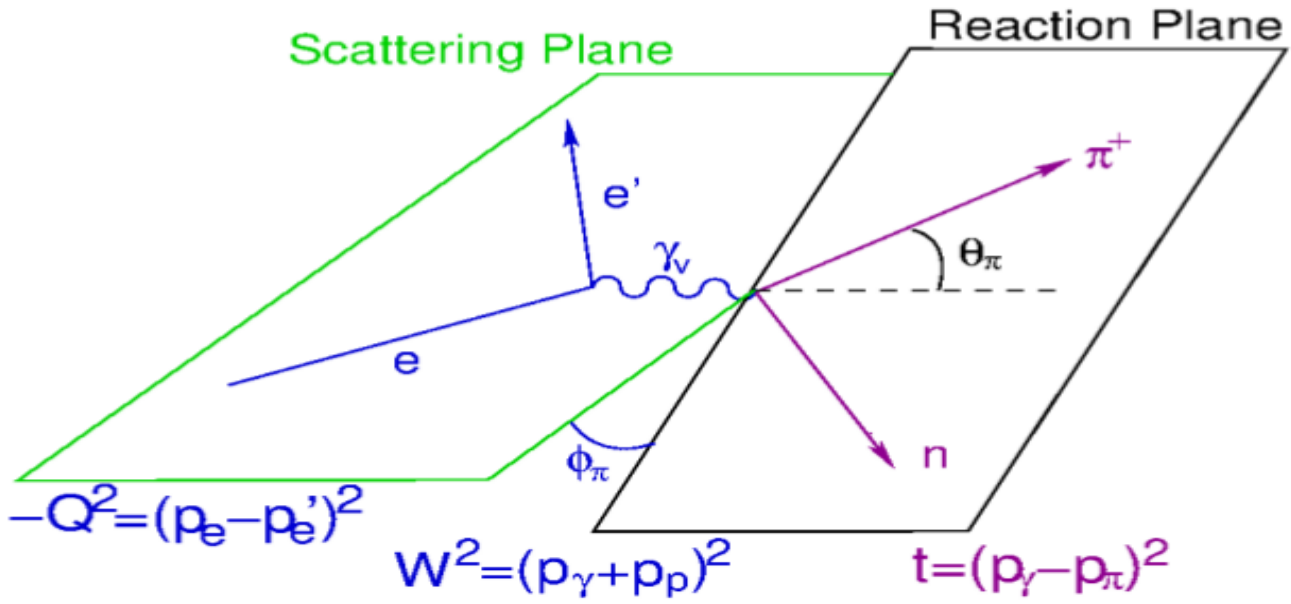
Rosenbluth (LT) Separation Technique

$$2\pi \frac{d^2\sigma}{dt d\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$



Virtual-photon polarization:

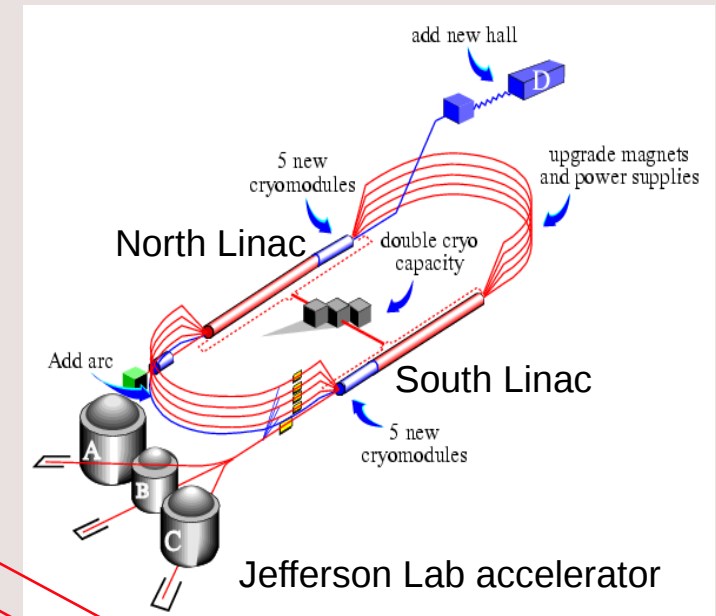
$$\varepsilon = \left(1 + 2 \frac{(E_e - E_{e'})^2 + Q^2}{Q^2} \tan^2 \frac{\theta_{e'}}{2} \right)^{-1}$$



- **L-T separation required to separate σ_L from σ_T**
- **Need to take data at smallest available $-t$, so σ_L has maximum contribution from the π^+ pole**
- **Need to measure t -dependence of σ_L at fixed Q^2, W**

Slide's credit to Garth Huber

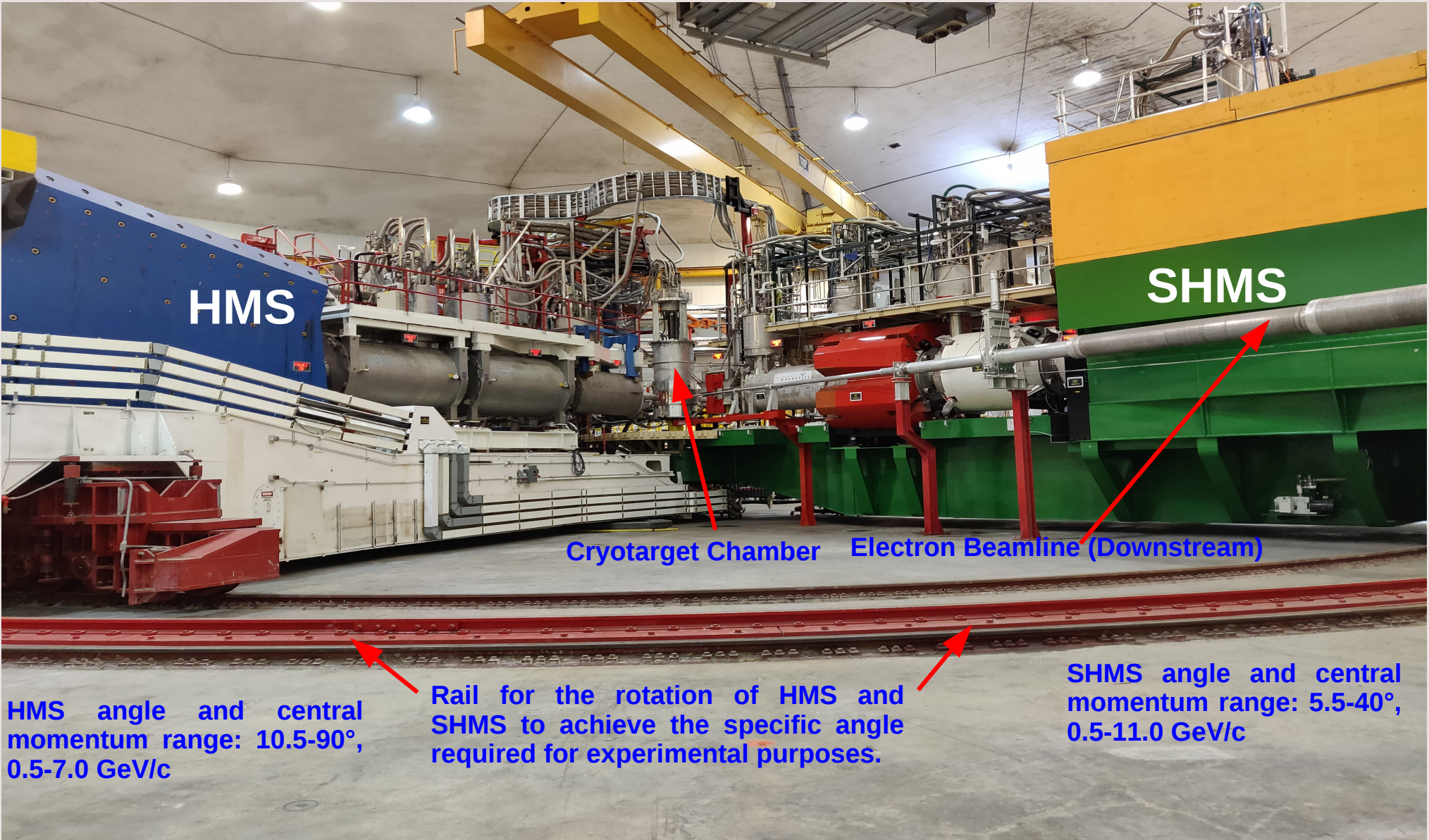
- Jefferson Lab has two 1.5 GHz Superconducting Linear Accelerators, which provide electron beam for Nucleon and Nuclear structure studies.



Four experimental Halls

- Beam energy up to ~ 12 GeV
- Beam current > 100 μA

- All halls can receive electron beam simultaneously.



HMS

SHMS

Cryotarget Chamber Electron Beamline (Downstream)

HMS angle and central momentum range: 10.5-90°, 0.5-7.0 GeV/c

Rail for the rotation of HMS and SHMS to achieve the specific angle required for experimental purposes.

SHMS angle and central momentum range: 5.5-40°, 0.5-11.0 GeV/c

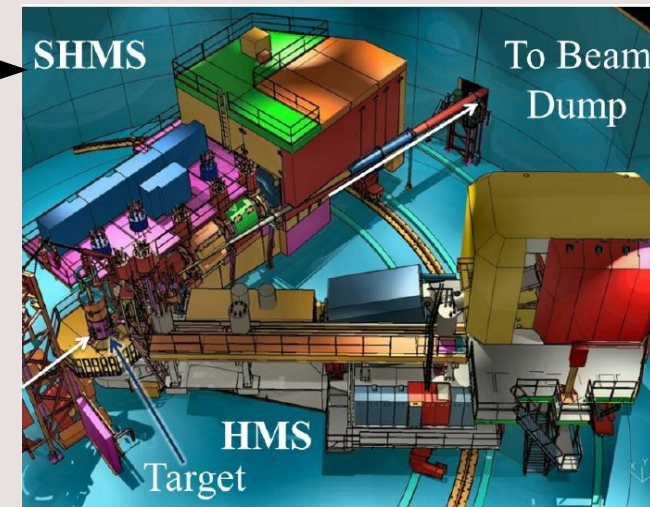
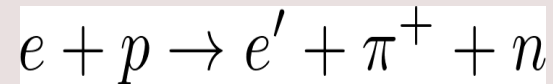
PionLT Exclusive Experiment (E12-19-006)



● The experiment conducted in Hall C in three phases. →

- **First run period:** ran in summer 2019
- **Second run period:** ran in fall 2021
- **Third run period:** ran in fall 2022

● The reaction system of the experiment



● The data acquired in first run period.

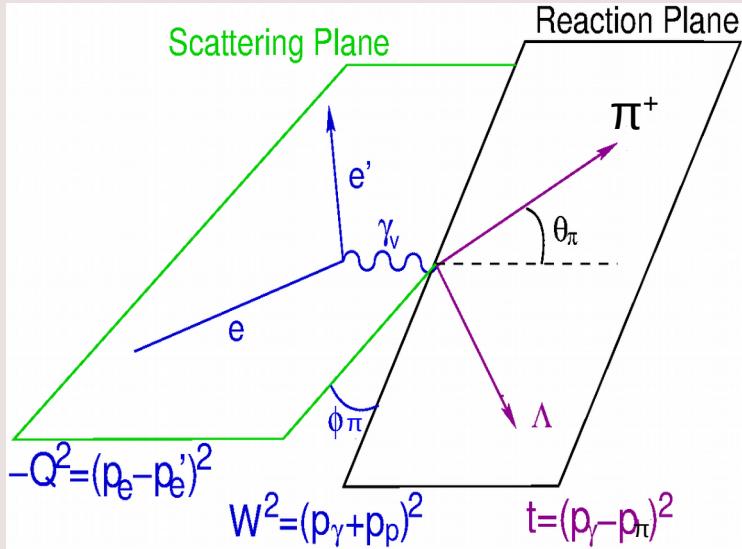
E_b (GeV)	Q^2 (GeV ²)	W (GeV)	x_B	ϵ
4.6/3.7/2.8	0.38	2.20	0.087	0.781/0.629/0.286
4.6/3.7/2.8	0.42	2.20	0.097	0.774/0.617/0.264

● Spokesperson of the experiment

- Garth Huber (UofR) , Tanja Horn (CUA), and Dave Gaskell (JLab)

E12-19-006 LT Separation (Parallel Kinematics Case)

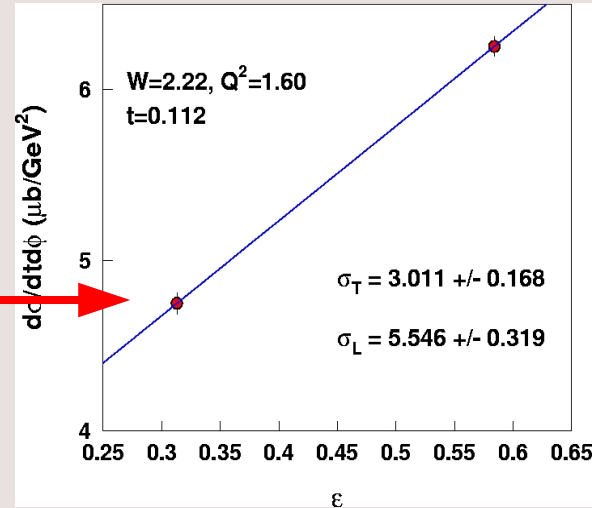
- The experimental data acquired for three ϵ at fixed Q^2 , W and $-t$.
 - This is the first time data acquired for 3 ϵ with multiple settings (left1, left2, center, right1, right2) to maximize the full Φ coverage for the LT separation.
 - The $-t$ range covers 0.001 - 0.07. Again, this is the first time data acquired to such lowest $-t$ to maximize the pion pole contribution.
 - In parallel kinematics, $\theta_\pi = 0$ (θ_π w.r.t \vec{q})
 - σ_L and σ_T can be separated out.
 - It requires uniform detector acceptance.



$$2\pi \frac{d^2\sigma}{dt d\phi} = \epsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt}$$

Virtual-photon polarization:

$$\epsilon = \left(1 + 2 \frac{(E_e - E_{e'})^2 + Q^2}{Q^2} \tan^2 \frac{\theta_{e'}}{2} \right)^{-1}$$



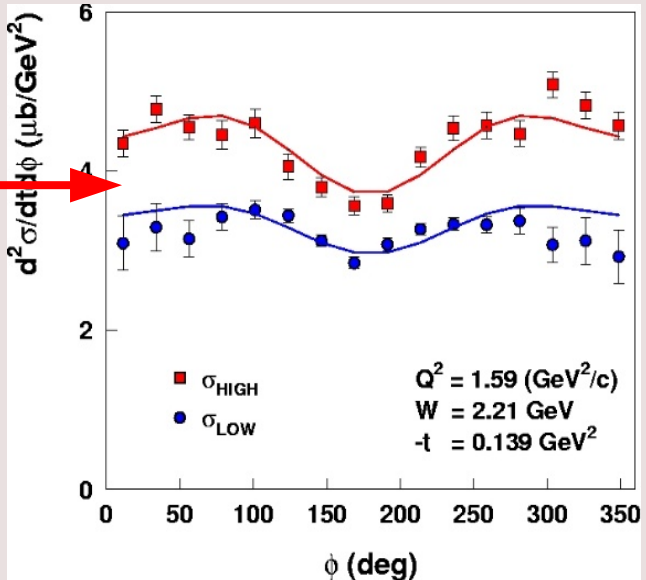
T. Horn, et al, PRL 97 (2006)192001

E12-19-006 Full LT Separation

- In non-parallel kinematics, $\theta_\pi \neq 0$ (θ_π w.r.t \vec{q})

$$2\pi \frac{d^2\sigma}{dt d\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

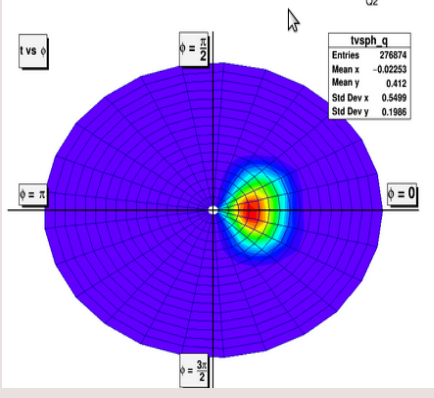
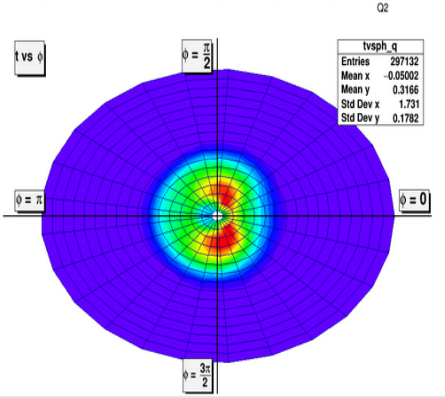
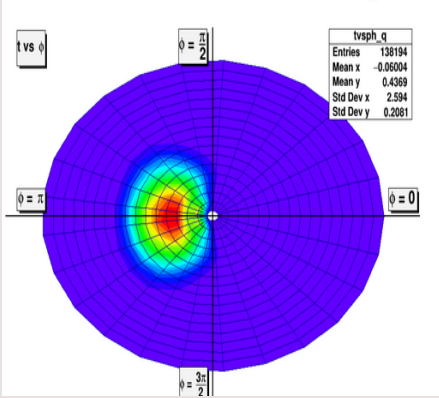
An example of experimental settings (left, center & right) for the full ϕ coverage.



(left)

(center)

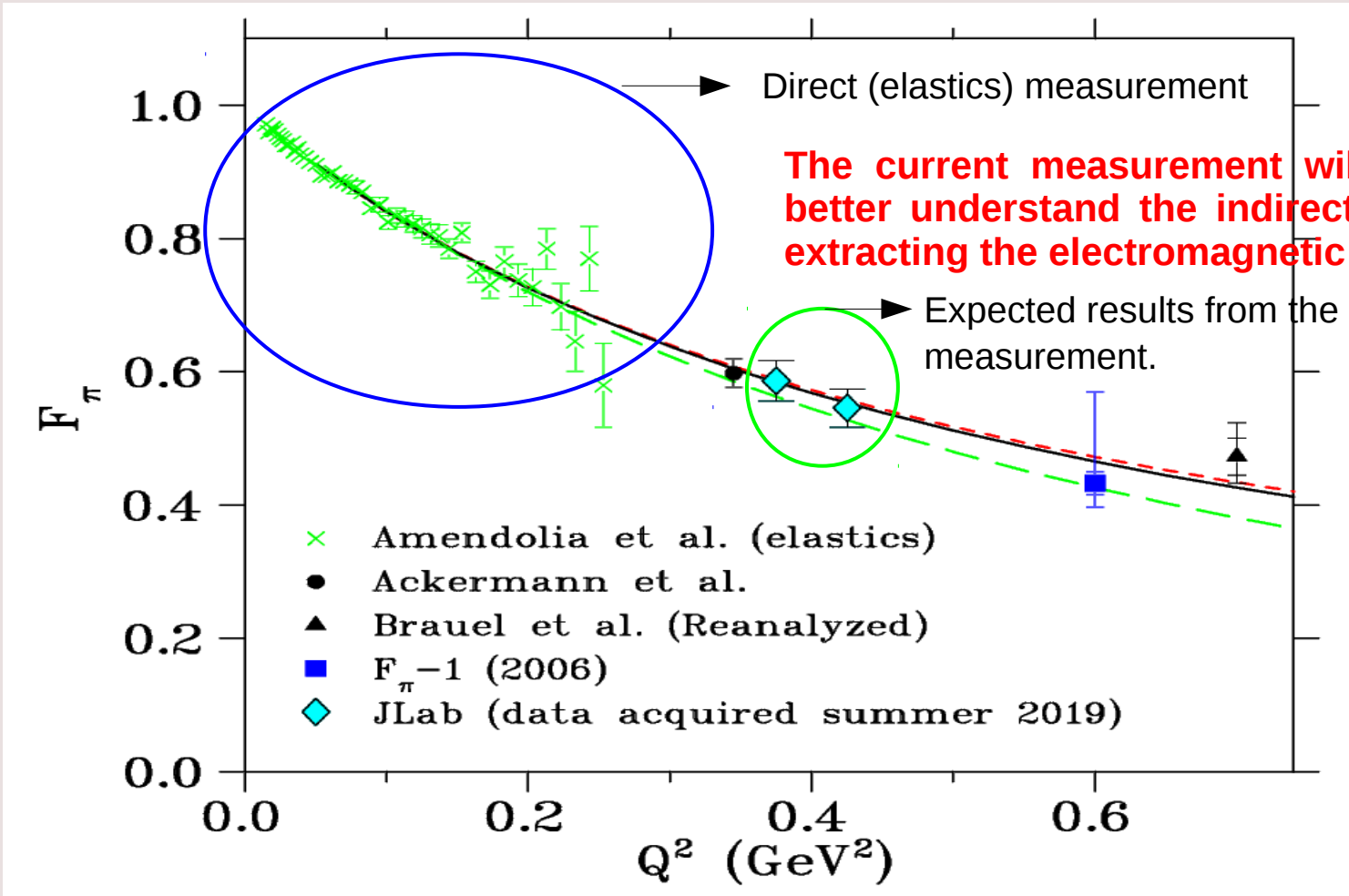
(right)



-t is radius

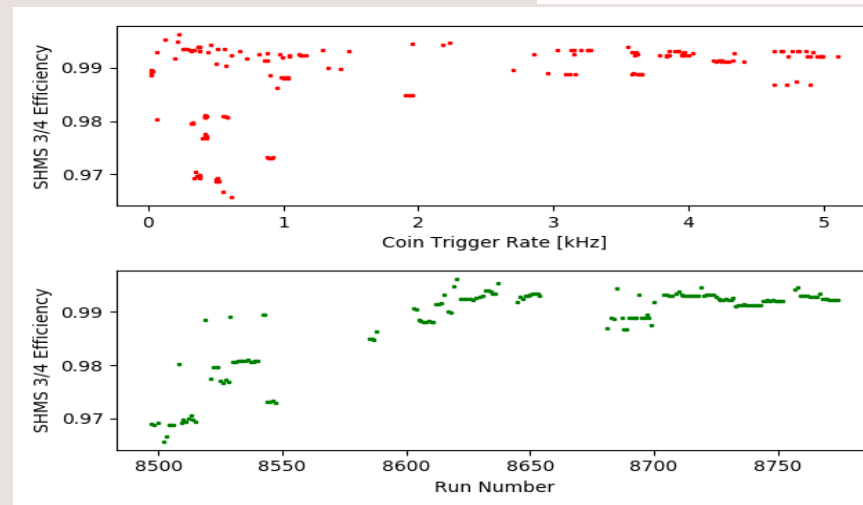
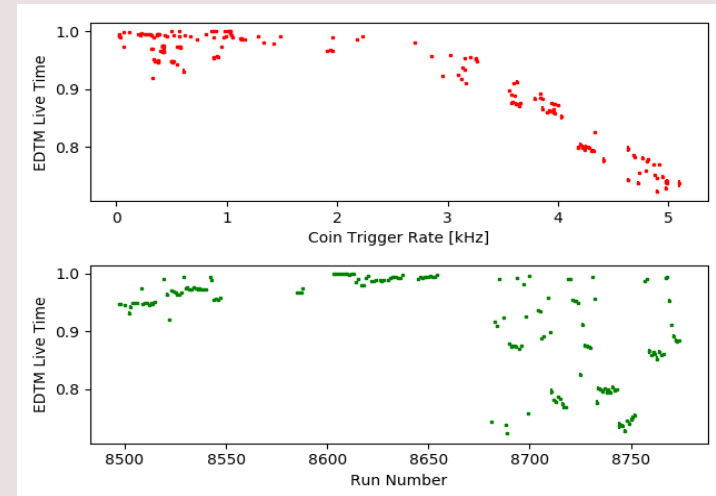
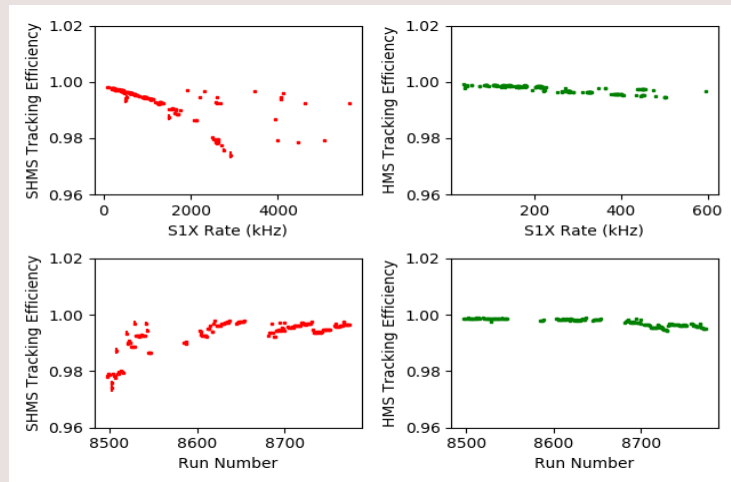
T. Horn, et al, PRL 97 (2006)192001

$e + p \rightarrow e' + \pi^+ + n$, Projected Results at $Q^2 = 0.38$ & 0.42 GeV^2



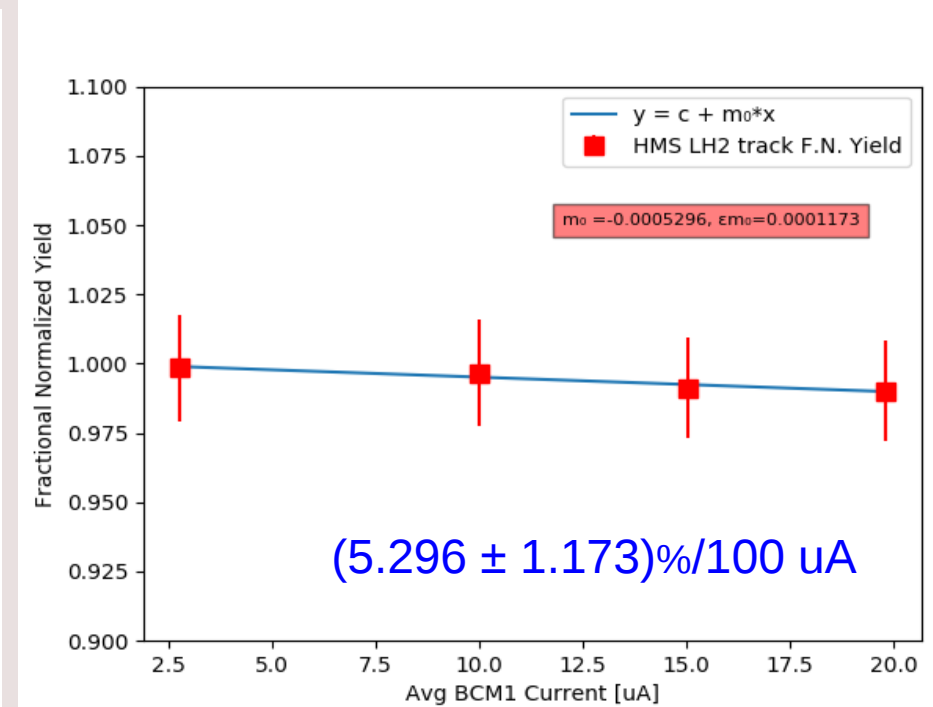
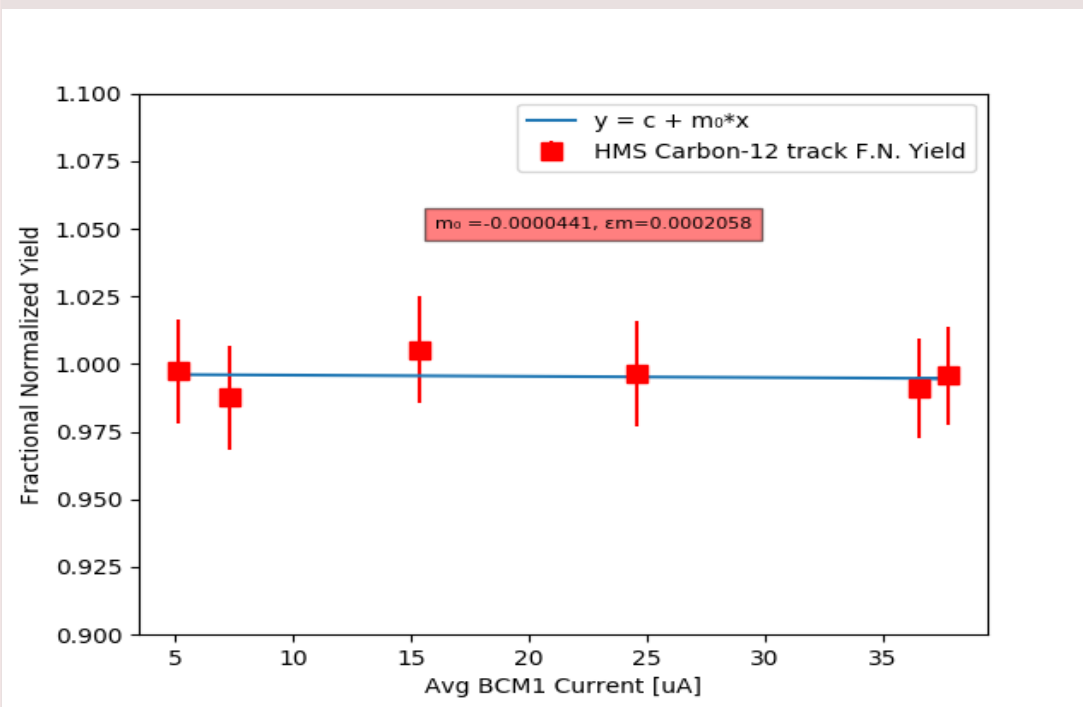
The Data Analysis (Various Efficiency)

- The rate dependence study for all settings is of utmost importance to have correct experimental yield for the LT separation.
 - The experimental settings (left1, left2, center, right1 & right2) are acquired at different experimental rates.



The Data Analysis (Luminosity Analysis)

- To check the rate dependence study and determine the LH_2 boiling correction factor the luminosity analysis is required.
 - Carbon does not boil at the Hall C experiments. Its yield at different currents (μA) should show no slope.
 - LH_2 could boil, and is required to determine the boiling correction factor for the LT separation.

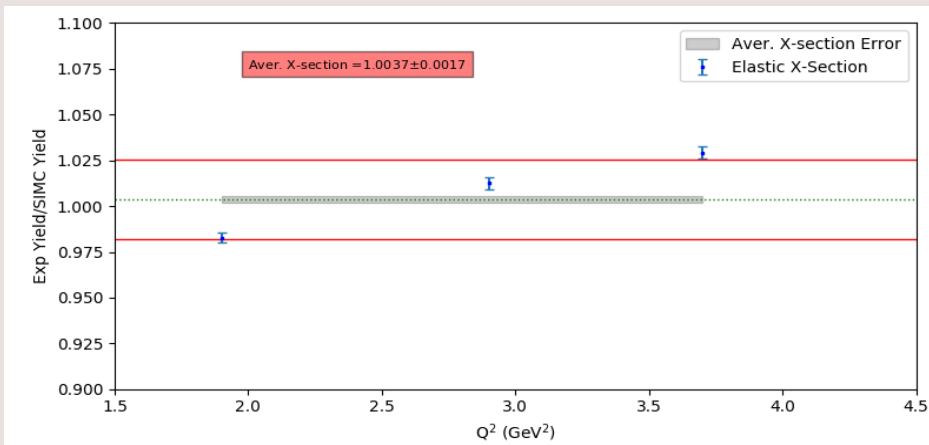
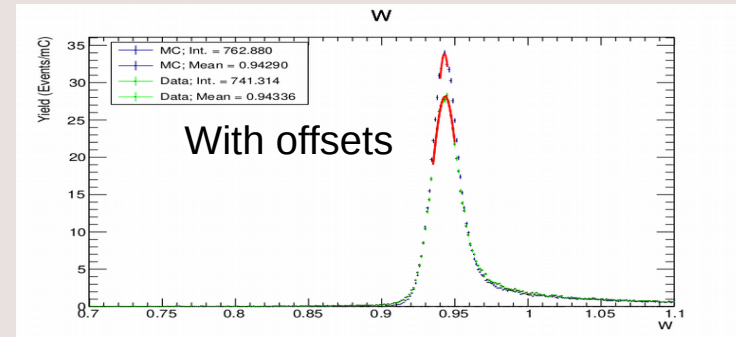
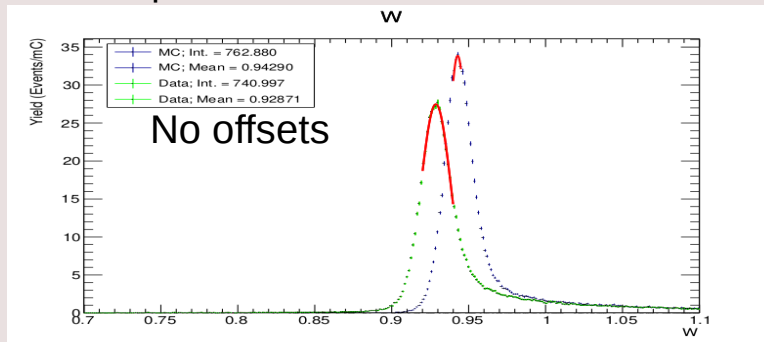


Error bars are statistical only.

'Heep', $e + p \rightarrow e' + p$, Analysis

High quality L-T separation requires that we know the beam energy, spectrometer angles and momenta more accurately than what we know from the power supply calibrations and floor angle markings.

- Heep reaction kinematically over-determined (detected both the e' and p).
- Missing energy, missing momentum and components of missing momentum must work out to zero.
- W should ideally be equal to the proton mass.
- We use the deviations between observed and physically-required values to determine the experimental offsets.

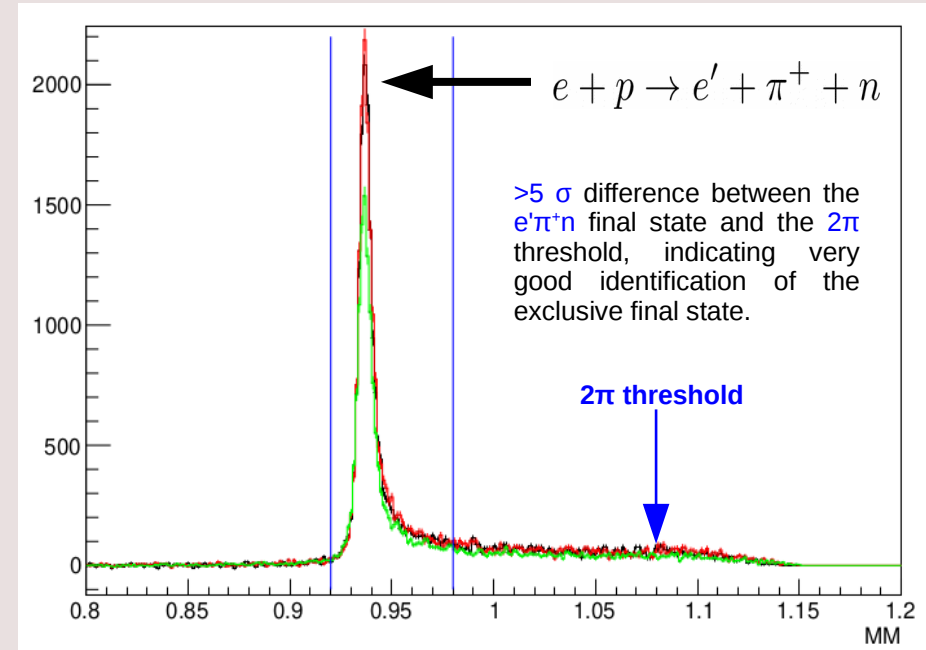
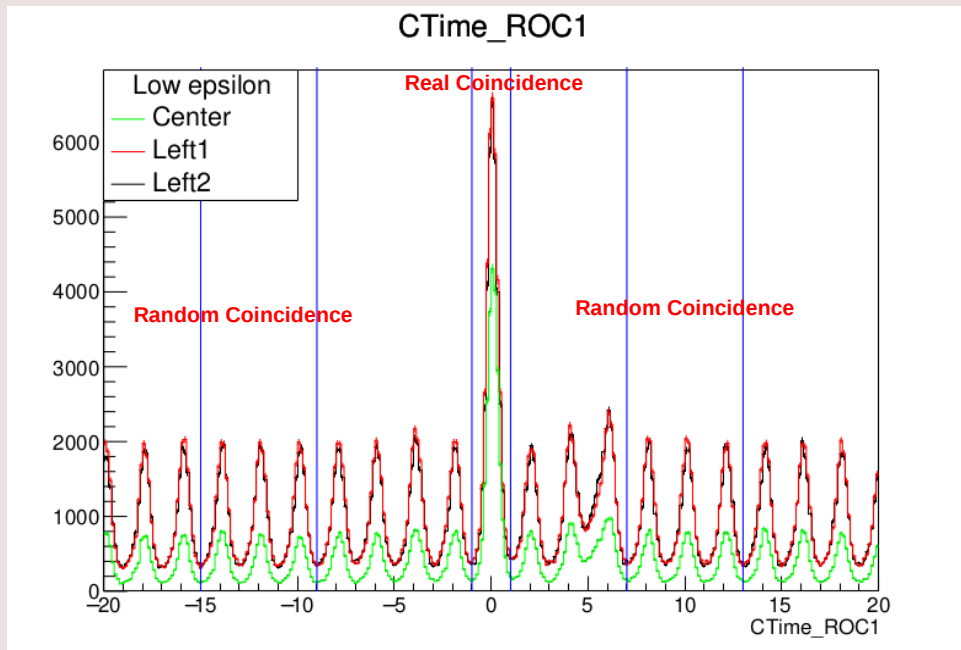


Quantity	SHMS	HMS
In-plane angle	2.8 mrad	1.2 mrad
Out-of-plane angle	0.0	0.99 mrad
Central Momentum	0.0	0.15%
Beam Energy	0.01% to 0.07%	

$e + p \rightarrow e' + \pi^+ + n$ Event Selection

■ The experimental data acquired in the coincidence mode of DAQ.

- The coincidence time is defined as, $t_{\text{coin}} = t_{\text{HMS}} - t_{\text{SHMS}}$.
- Random coincidences: due to the RF structure of the electron beam, giving rise to accidental coincidences between a scattered electron from one beam burst and a pion from another.
- Random coincidences are measured and subtracted from the real coincidences to give the real coincidences. The time spacing of bunches is 2 ns.
- Also, we uniquely identify the exclusive final state with the missing mass technique.

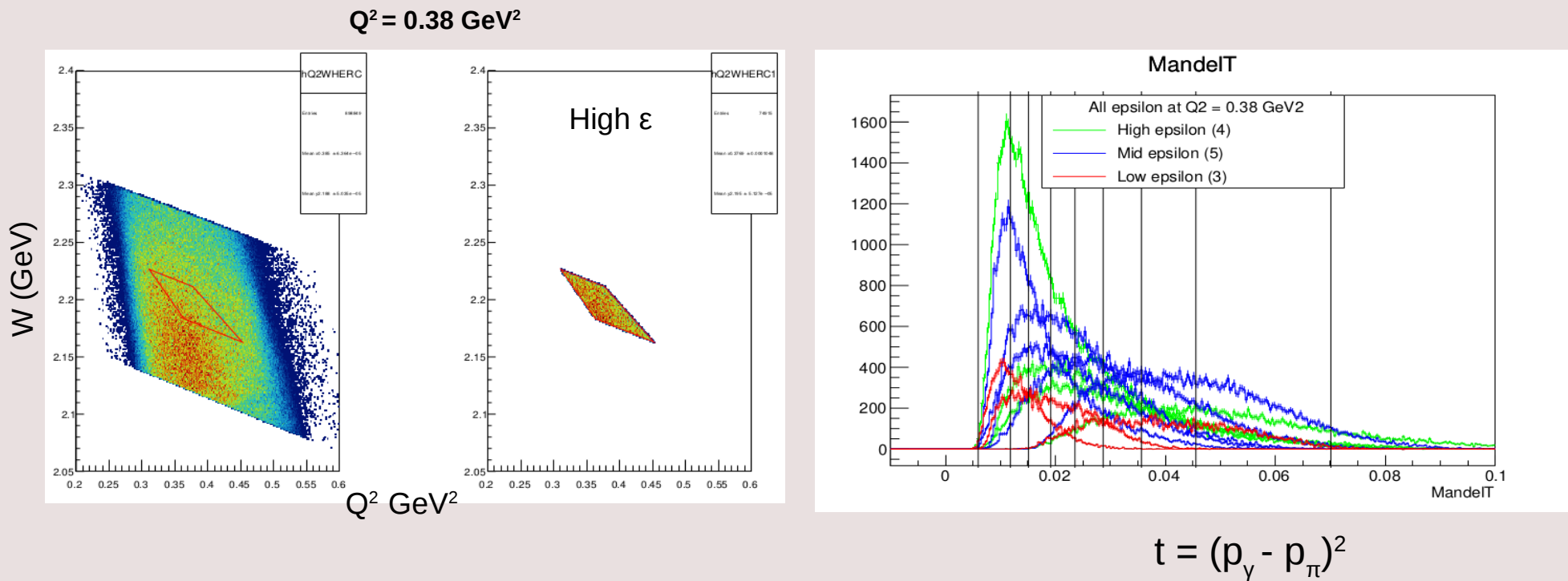


$$MM = \sqrt{((E_b + m_p - E'_e - E_{\pi^+})^2 - (\vec{P}_e - \vec{P}'_e - \vec{P}_{\pi^+})^2)}$$

$e + p \rightarrow e' + \pi^+ + n$ Diamond Cut, -t binning & Φ binning

📌 To separate the individual cross-section terms through the Rosenbluth separation technique.

- A diamond cut is required to match the phase space for all three ϵ data.
- Diamond cut decides from the low ϵ data and applies the same cut to all three ϵ data.
- **-t and Φ binning**: extract the cross section in **-t** and **ϕ** bins. In this study, **8 t** bins and **16 Φ** bins decided for a better converge the Rosenbluth separation equation.



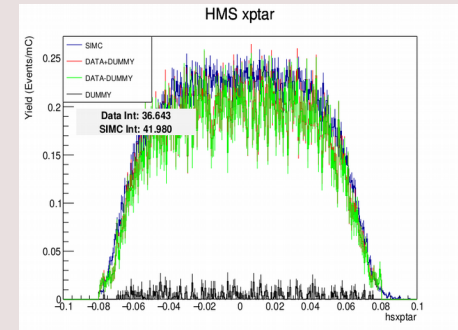
$e + p \rightarrow e' + \pi^+ + n$ Cross-Section

Monte Carlo (SIMC) is used to account for effects on the experimental acceptance, such as finite target length and beam spot, magnet field map and detector geometry.

- It includes an empirical model, to compare the simulated event distributions with the observed distributions, for various experimental variables.

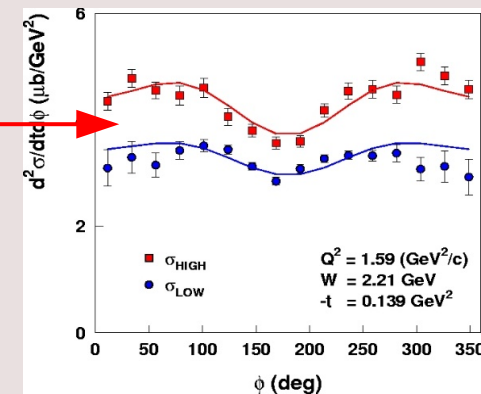
The unseparated cross-section is calculated as,

$$\sigma_{exp}(\bar{W}, \bar{Q}^2, t, \phi; \bar{\theta}, \bar{\epsilon}) = \frac{Y_{exp}}{Y_{MC}} \sigma_{MC}(\bar{W}, \bar{Q}^2, t, \phi; \bar{\theta}, \bar{\epsilon}).$$



The simultaneous fitting gives the individual cross-section terms.

$$2\pi \frac{d^2\sigma}{dt d\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$



The model input cross-section is then iterated to achieve the best agreement between the data and SIMC. The iteration process is continued until the experimental cross-section changes by less than **1 %**.

Extract $F_\pi(Q^2)$ from JLab σ_L data

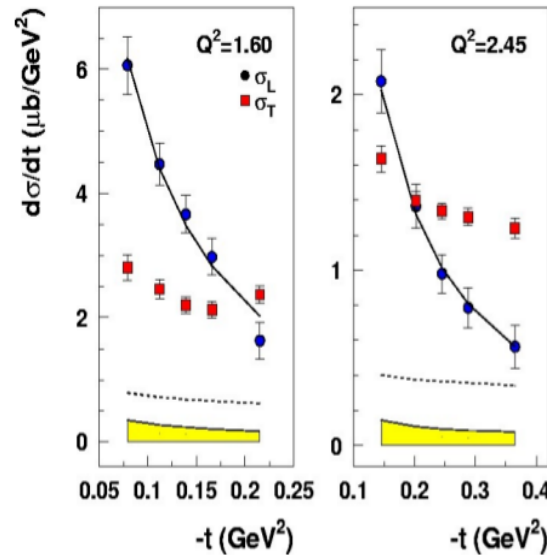
Model incorporates π^+ production mechanism and spectator neutron effects:

VGL Regge Model:

- Feynman propagator $\left(\frac{1}{t - m_\pi^2}\right)$ replaced by π and ρ Regge propagators.
 - Represents the exchange of a series of particles, compared to a single particle.
- Free parameters: $\Lambda_\pi, \Lambda_\rho$ (trajectory cutoff).
[Vanderhaeghen, Guidal, Laget, PRC 57(1998)1454]
- At small $-t$, σ_L only sensitive to F_π

$$F_\pi = \frac{1}{1 + Q^2 / \Lambda_\pi^2}$$

Fit to σ_L to model gives F_π at each Q^2

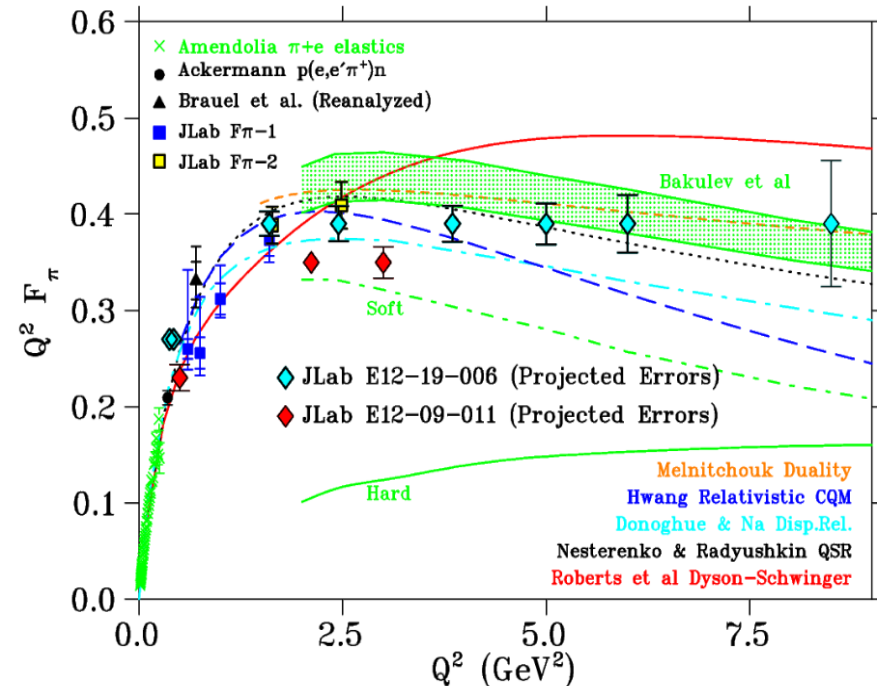


Error bars indicate statistical and random (pt-pt) systematic uncertainties in quadrature. Yellow band indicates the correlated (scale) and partly correlated (t-corr) systematic uncertainties.

$$\Lambda_\pi^2 = 0.513, 0.491 \text{ GeV}^2, \Lambda_\rho^2 = 1.7 \text{ GeV}^2.$$

F π -2 data: T. Horn et al., PRL 97(2006)192001.

Previous measurements and projected results for the whole E12-19-006 experiment.



- Garth Huber (UofR), Tanja Horn (CUA) and Dave Gaskell (JLab).
- Proposal of the experiment: [E12-19-006](#)

We now also have CKY model.

If anyone is working on developing cross-section models (σ_L & σ_T), please let me know. I would love to talk to you.

Slide's credit to Garth Huber

The study at EIC

Extension of the Studies to EIC

● Physics Motivation:

- JLab measurements have shown the importance of π^+ and K^+ structure studies for understanding QCD's transition from “weak” and “strong” domains, and understanding DCSB's role in generating hadron properties.
- Definite answers to these questions require high Q^2 data well beyond JLab's reach.
- The Electron–Ion Collider (EIC) may provide this reach.

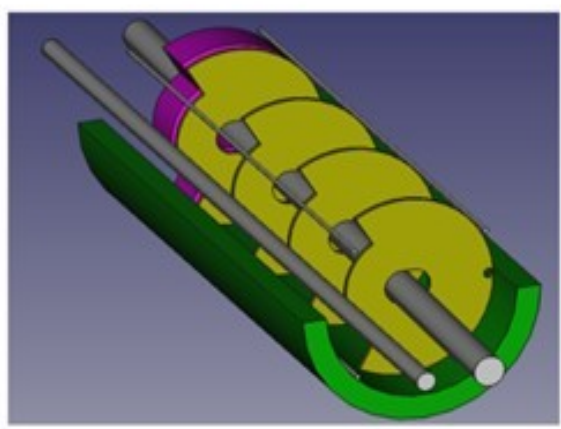
● Experimental Issues:

- The cross section for the exclusive $p(e, e'\pi^+n)$ channel is small, can it be cleanly identified at EIC?
- Is the detector resolution sufficient to reliably reconstruct (Q^2, W, t) ? (*work is being done*)
- How to measure the longitudinal cross section, $d\sigma_L/dt$, (LT separation is not possible at the EIC) needed for form factor extraction?

Extension of the Studies to EIC

Far-Forward Detectors:

We will acquire data at triple coincidence to measure all three particles (e' , π^+ & n) in the reaction.



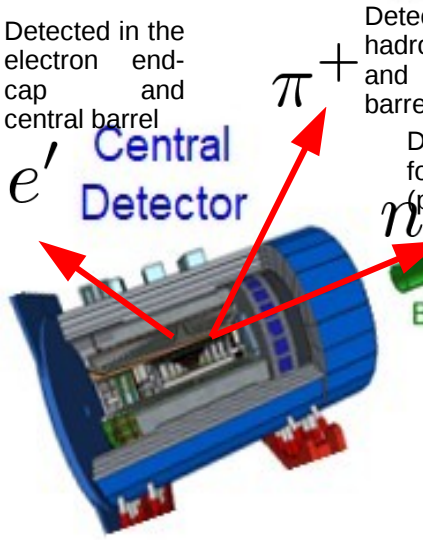
Roman Pots

Hadron Beam after IP

ZDC

Off Momentum ZDC

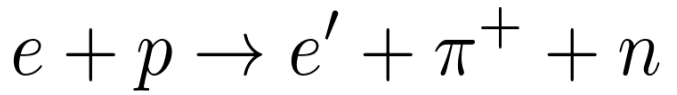
B0 Trackers + Calorimeter



π^+
Detected in the hadron end-cap and central barrel

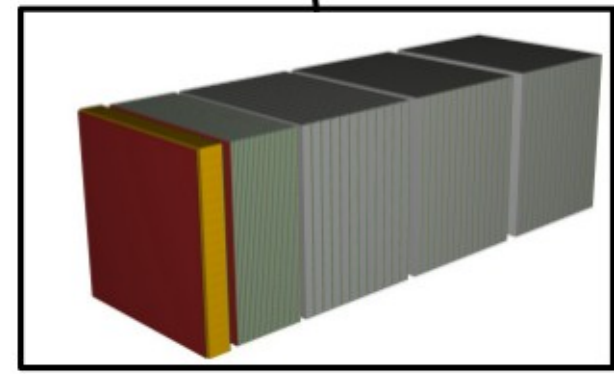
n
Detected in the far-forward detectors (primarily ZDC)

B0apf Diople
B0pf Diople



Q2bpf quadrupole
Q1pf quadrupole
Q1apf quadrupole

B1apf Dipole
B1pf Dipole



$e + p \rightarrow e' + \pi^+ + n$ at EIC

■ The weighted spatial distribution study of $p(e, e'\pi^+, n)$ reaction.

- Used Deep Exclusive Meson Production (DEMP) event generator.

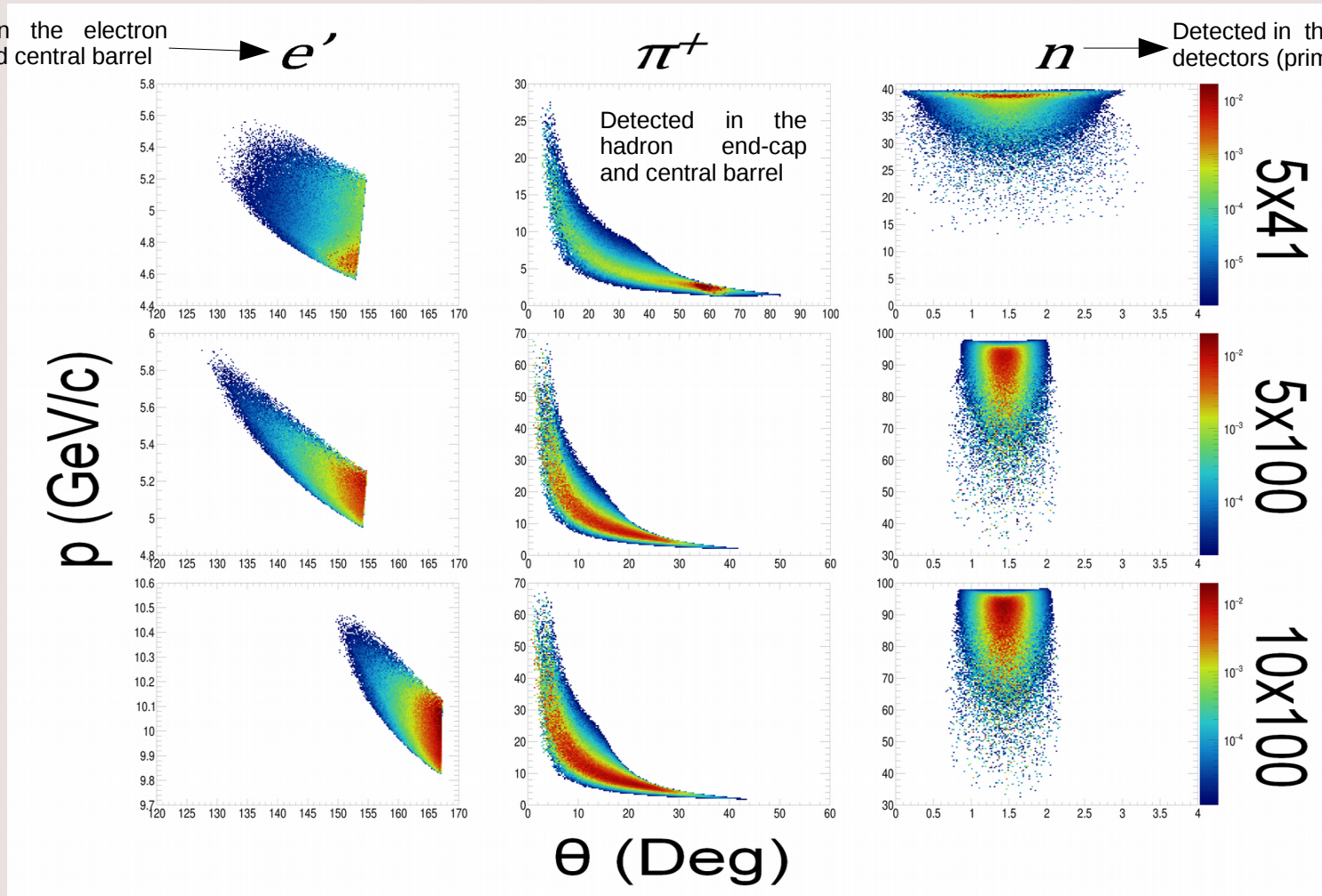
Detected in the electron end-cap and central barrel

e'

π^+

n

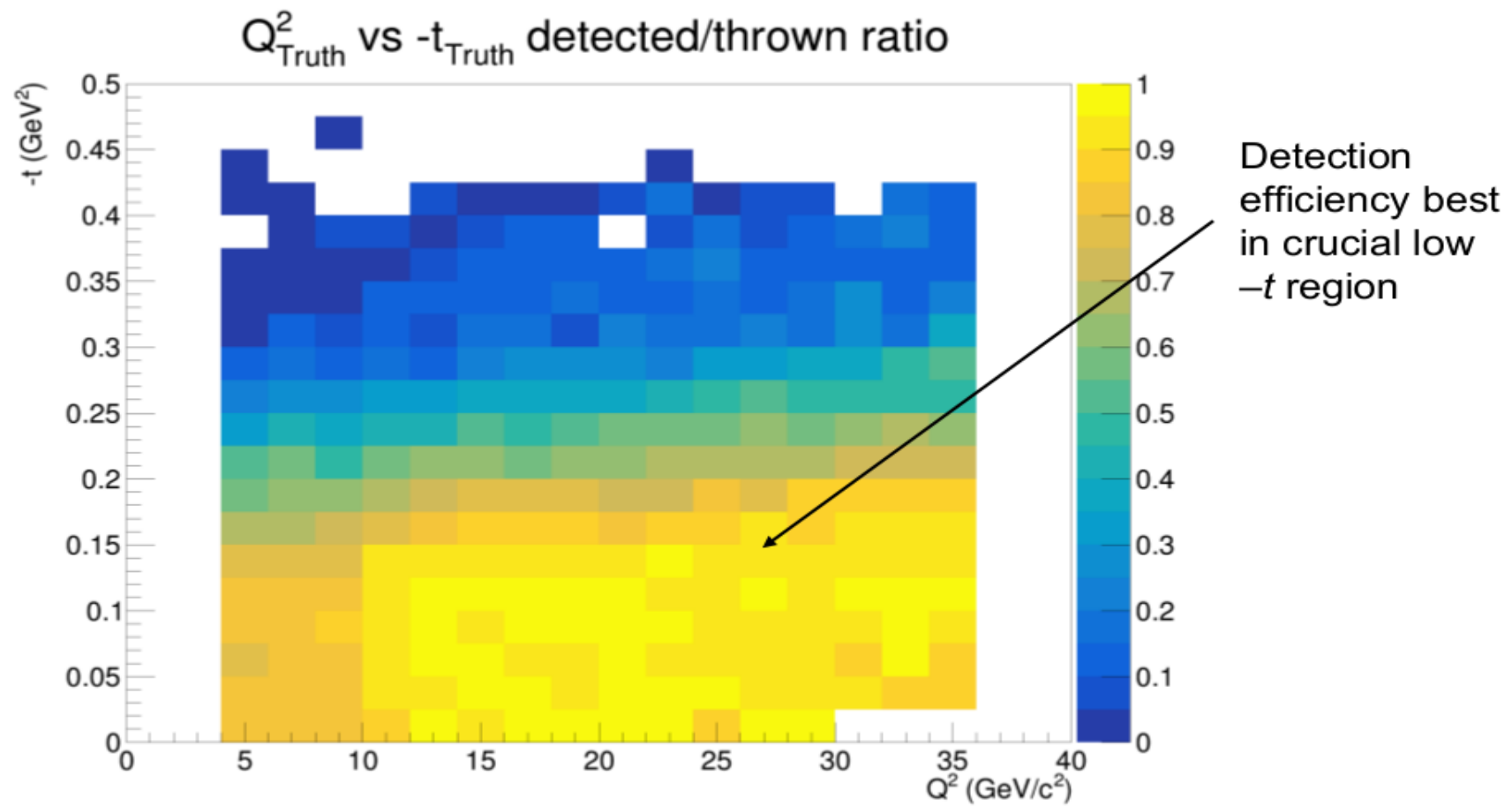
Detected in the far-forward detectors (primarily ZDC)



More details about simulation are in the [ECCE NIM paper](#).

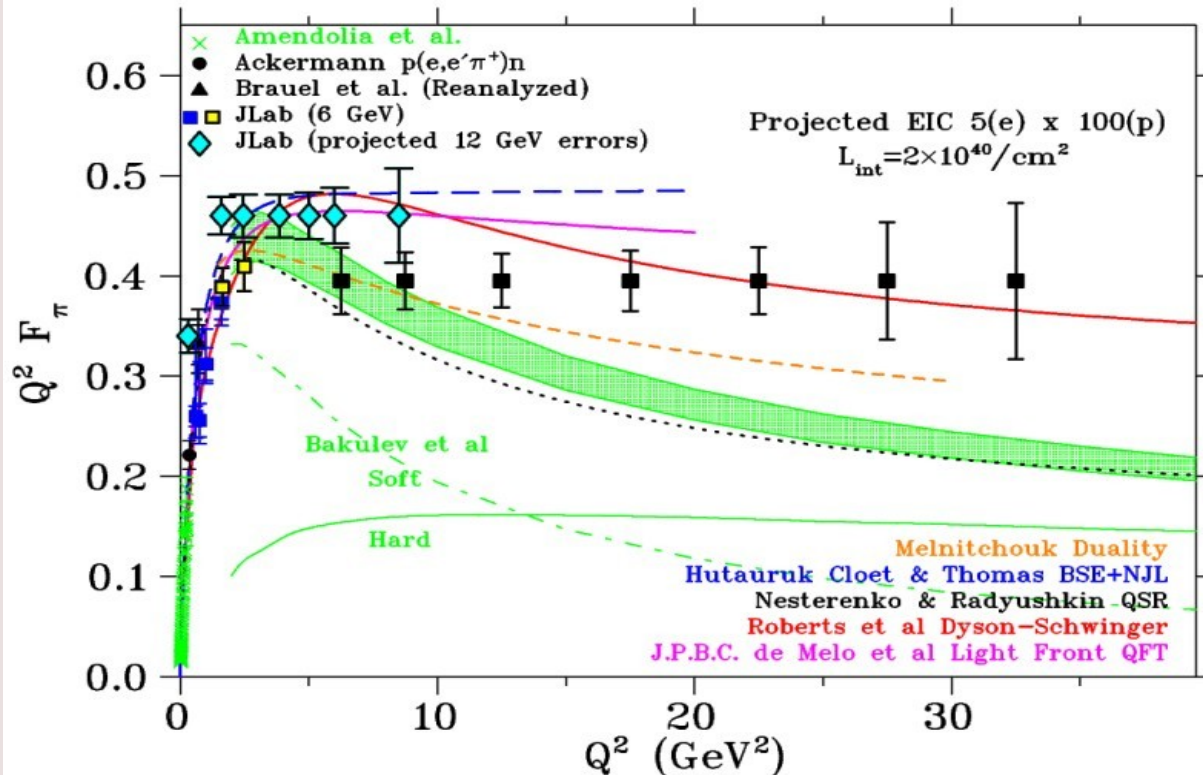
Plot's credit to Love Preet

Detection efficiency per (Q^2, t) bin



Plot by Stephen Kay

The Projected $F_\pi(Q^2)$ at EIC (5(e) x 100(p))



Assumptions:

- 5(e^-) x 100(p)
- Integrated $L = 20 \text{ fb}^{-1}/\text{yr}$
- Clean identification of exclusive $p(e, e' \pi^+ n)$ events
- t reconstruction resolution based on ECCE detector design
- Syst. Unc: 2.5% pt-pt and 12% scale
- $R = \sigma_L / \sigma_T = 0.013 - 0.14$ at lowest $-t$ from VR model, and $\delta R = R$ syst. unc. in model subtraction to isolate σ_L .
- π pole dominance at small $-t$ confirmed in ${}^2\text{H} \pi^- / \pi^+$ ratios.

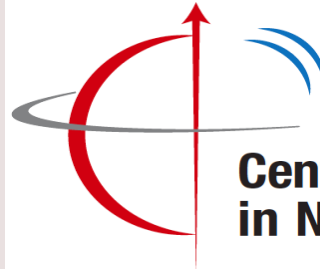
Plot's credit to Garth Huber

Summary

- Our research focuses on advancing our comprehension of the electro-production reaction mechanism for pions and kaons, along with the investigation of their electromagnetic form factors. Jefferson Lab is the only facility for the LT separation.
- The pion data analysis at low Q^2 (0.38 & 0.42) would be the first measurement at the lowest $-t$, and the multiple experimental settings (left1, left2, center, right1 & right2).
- Unlike the pion pole, the dominance of the kaon pole at the lowest $-t$ has not been previously tested. For the first time, our group is trying to understand the dominance of the kaon pole at the lowest $-t$.
- We are delving into understanding the validity of factorization, specifically how longitudinal and transverse cross-sections scale with Q^2 .
- Our group is actively engaged in extending the study of pion and kaon structures at the Electron-Ion Collider.



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Thank You!

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