

# Beam-Spin Asymmetry of Exclusive Pion Production

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July 15, 2024

University of Regina

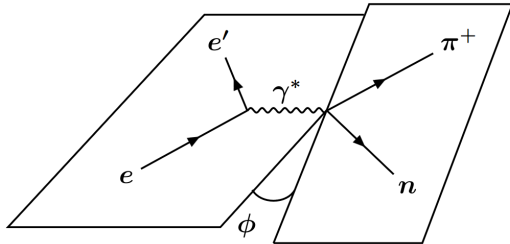
KaonLT Experiment, Jefferson Lab Hall C



University  
of Regina



- Measurement of beam spin asymmetry  $A_{LU}$  for two channels of exclusive  $\pi^+$  production:  $\rho(e, e'\pi^+)n/\Delta^0$
- Publication in preparation for  $\rho(e, e'\pi^+)n$
- New preliminary results for  $\rho(e, e'\pi^+)\Delta^0$
- Data from KaonLT experiment (E12-09-11)



$$Q^2 = -(p_e - p_{e'})^2$$
$$W = \sqrt{m_p^2 + 2m_p(E_e - E_{e'}) - Q^2}$$
$$t = (p_p - p_n)^2$$
$$x_B = Q^2 / 2m_p(E_e - E_{e'})$$



- Define the beam spin asymmetry  $A_{LU}$  as:

$$A_{LU} = \frac{1}{P} \left( \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} \right) = \frac{1}{P} \left( \frac{N^+ - N^-}{N^+ + N^-} \right)$$

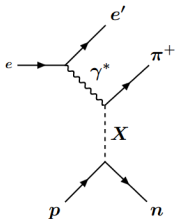
- Polarized cross-section in Rosenbluth equation:

$$2\pi \frac{d^2\sigma}{dtd\phi} = \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \sqrt{2\epsilon(1+\epsilon)} \frac{d\sigma_{LT}}{dt} \cos\phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi \\ + h \sqrt{2\epsilon(1-\epsilon)} \frac{d\sigma_{LT'}}{dt} \sin\phi$$

- Beam spin asymmetry provides much cleaner access to  $\sigma_{LT'}$ :

$$A_{LU} = \frac{\sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin\phi}{1 + \sqrt{2\epsilon(1+\epsilon)} \frac{\sigma_{LT}}{\sigma_0} \cos\phi + \epsilon \frac{\sigma_{TT}}{\sigma_0} \cos 2\phi}$$

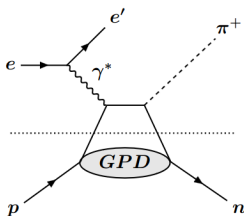
(a)



## Regge process:

$X$  represents the exchange of several particles along a **Regge trajectory**

(b)



## Factorization:

reaction split into a **hard** scattering part and a **soft** part described by a **GPD**

**This work:** Extract  $\sigma_{LT'}/\sigma_0$  over a range of kinematics and compare results to Regge and GPD predictions.



- Vrancx-Ryckebusch (**VR**): exchange of  $\pi(140)$ ,  $\rho(770)$ , and  $a_1(1260)$   
**Regge** trajectories
- Goloskokov-Kroll (**GK**): uses twist-2 longitudinal ( $\tilde{E}, \tilde{H}$ ) and twist-3 transverse ( $E_T, H_T$ ) **GPDs**, with pion pole contributions.  
**GK1**: default GK model  
**GK2**: modification  $H_T \rightarrow H_T * 2$ , as seen in [Diehl et al 2023]
- Yu-Choi-Kong (**YCK**): **Regge**-based, incorporates the exchange of tensor meson  $a_2(1320)$  and axial mesons  $a_1$  and  $b_1(1235)$ . *YCK are co-authors on this paper.*  
**YCK1**: nucleon EMFFs mediated by GPDs  
**YCK2**: nucleon EMFFs use dipole form

T. Vrancx, J. Ryckebusch & J. Nys, Phys. Rev C, **89** 065202 (2014). arXiv:1310.7715

S.V. Goloskokov, P. Kroll, Eur. Phys. J. C **65** 137 (2010). arXiv:1106.4897

T. K. Choi, K.-J. Kong & B.-G. Yu, J. Korean Phys. Soc. **67**, 1089-1094 (2015). arXiv:1508.00969



$$A_{LU} = \frac{1}{P} \left( \frac{N^+ - N^-}{N^+ + N^-} \right)$$

$$\delta_{\text{stat}} = \frac{2}{P} \sqrt{\frac{N^+ N^-}{(N^+ + N^-)^3}}$$

- No dedicated polarization measurements in Hall C
- **Mott polarimeter** at injector gives source polarization: **90±1%**
- **Spin precession** calculation shows Hall C receives **99%** of the source polarization
- Final value **P=89<sub>-3</sub><sup>+1</sup>%**  
Uncertainty from the **beam energy uncertainty** (3.6 MeV) and the range of possible **linac energy imbalance**

Thanks to Steve Wood and Dave Gaskell for polarization values and uncertainty.



- HMS detecting **electrons**
- SHMS detecting **positive hadrons**
- Data taken Autumn 2018
- Beam energy 10.585 GeV
- Beam helicity flipped at 30 Hz
- Target 10 cm unpolarized LH<sub>2</sub>

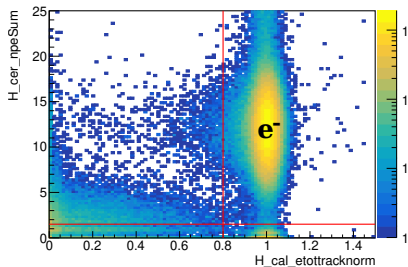
$Q^2$ (GeV)	$W$ (GeV)	$x_B$	$\epsilon$
2.115	2.95	0.21	0.79
3	3.14	0.25	0.67
3	2.32	0.40	0.88
4.4	2.74	0.40	0.71
5.5	3.02	0.40	0.53

$$\rho(e, e' \pi^+) n$$



# Particle Identification

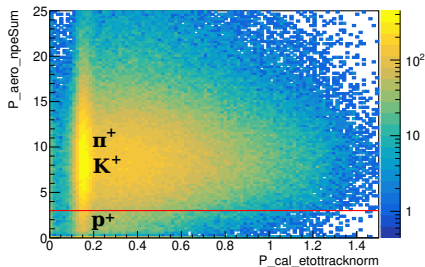
$p(e, e' \pi^+) n$



$e^-$  in HMS

$H_{cal\_etottracknorm} > 0.8$

$H_{cer\_npeSum} > 1.5$



$\pi^+$  in SHMS

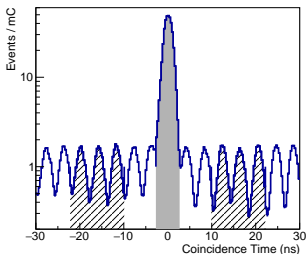
$P_{aero\_npeSum} > 3$

- Electrons identified with cut on gas Čerenkov ( $C_4F_{10}$  at 0.48 atm,  $n = 1.0008$ ) in combination with lead-glass calorimeter
- Pions identified with cut on an aerogel Čerenkov ( $n = 1.015$  or  $n = 1.011$ )

Plots:  $Q^2=3.0$ ,  $x_B=0.25$ , SHMS center.

# Event Selection

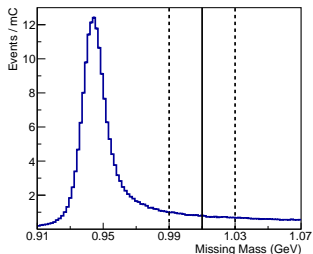
$p(e, e' \pi^+) n$



## Coincidence time:

$$t_{SHMS} - t_{HMS}$$

showing selected prompt  
and random windows



## Missing mass

$$m_X^2 = (p_e - p_{e'} - p_\pi)^2$$

showing cut used in analysis

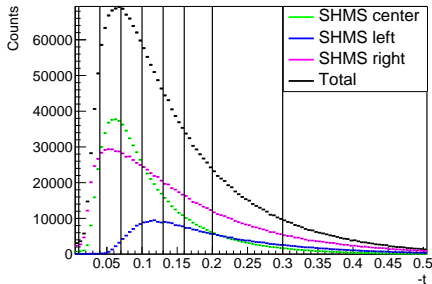
Plots:  $Q^2=3.0$ ,  $x_B=0.25$ , SHMS center.

# -t Binning

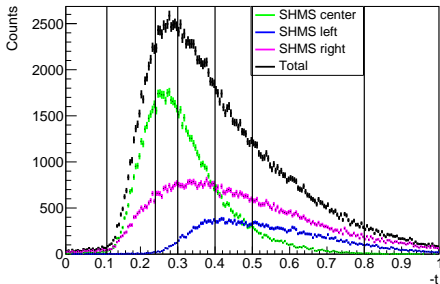
$p(e, e' \pi^+) n$



- Sum all events at one  $(Q^2, W)$  and separate into  $-t$  bins with similar numbers of events



$Q^2=2.1 \text{ GeV}^2$ ,  $x_B=0.25$   
 $\mathcal{O}(10^6)$  events, 8  $-t$ -bins



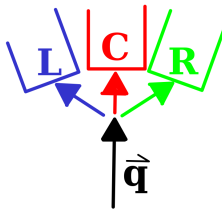
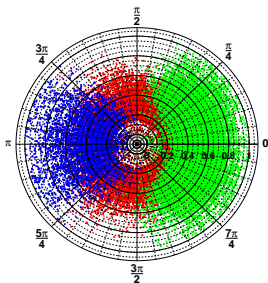
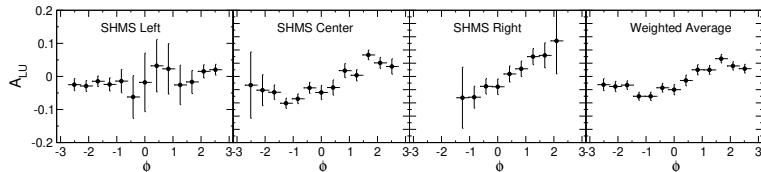
$Q^2=5.5 \text{ GeV}^2$ ,  $x_B=0.40$   
 $\mathcal{O}(10^5)$  events, 5  $-t$ -bins

# Combining SHMS Settings

$p(e, e'\pi^+)n$



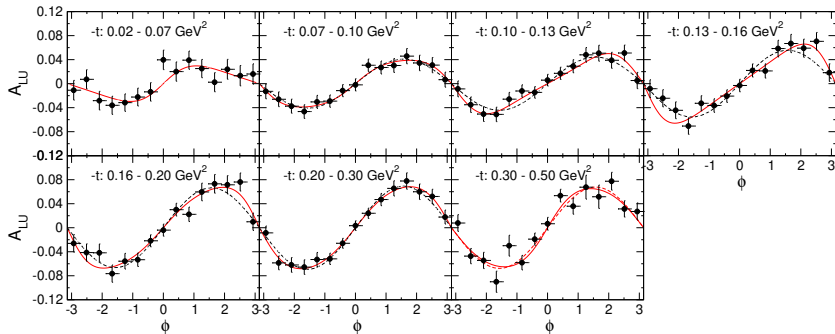
Asymmetry is calculated separately for three SHMS angles (**left**, **center**, **right**), then a weighted average is taken for full  $\phi$  coverage.



Plots:  $Q^2=3.0, x_B=0.40, 0.35 < -t < 0.40$  ( $A_{LU}$  vs  $\phi$ ) and  $Q^2=5.5, W=3.02$  ( $-t$  vs  $\phi$  polar plot).

# Asymmetry

$\rho(e, e' \pi^+) n$



- $A_{LU}$  as a function of  $\phi$  for each bin in  $-t$
- Solid line shows the **full fit** and the dashed line an **approximated fit**
- Error bars are statistical only

Plots:  $Q^2 = 3 \text{ GeV}^2$ ,  $x_B = 0.25$ .

# The Question of Fitting

$p(e, e' \pi^+) n$



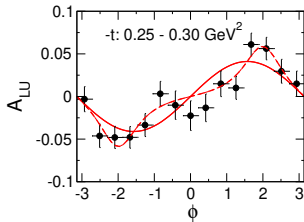
- Recall functional form of asymmetry:

$$A_{LU} = \frac{\sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi}{1 + \sqrt{2\epsilon(1+\epsilon)} \frac{\sigma_{LT}}{\sigma_0} \cos \phi + \epsilon \frac{\sigma_{TT}}{\sigma_0} \cos 2\phi}$$

- Previous work [Diehl et al 2023] has assumed  $\frac{\sigma_{LT}}{\sigma_0} \ll 1$ ,  $\frac{\sigma_{TT}}{\sigma_0} \ll 1$  such that

$$A_{LU} = \sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi$$

- This appears to be a low  $-t$  approximation, which is not sufficient to describe our data in all bins



- Extract  $A_{LU}$  using full functional form
- Use difference in  $A_{LU}$  from approximate fit as a systematic error

Plot:  $Q^2 = 3 \text{ GeV}^2$ ,  $x_B = 0.40$ .



## 1. Fitting error

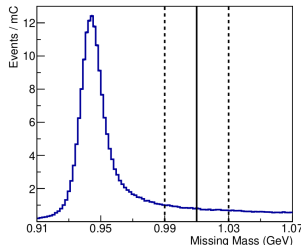
- Difference between  $A_{LU}$  extracted using **full or approximate fit**
- Unidirectional, leads to **asymmetric** total error
- Dominates point-to-point uncertainty: up to **70%** of  $A_{LU}$

## 2. Cut dependence

- RMS of differences in  $A_{LU}$  calculated using different values for **coincidence time** and **missing mass** cuts
- Contributes uncertainty of **1-7%**

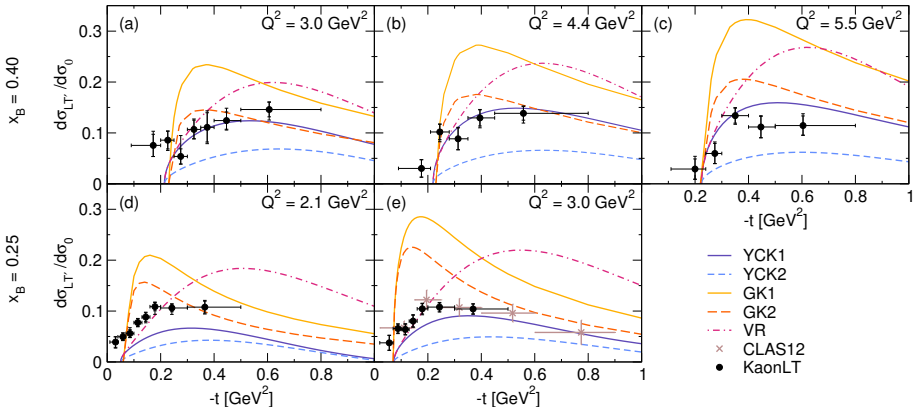
## 3. Beam polarization

- Uncertainty propagated using general formula
- Contributes  $\sim 3\%$  error



# Results

$\rho(e, e' \pi^+) n$



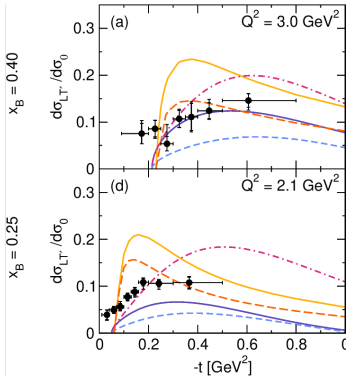
T. K. Choi, K.-J. Kong & B.-G. Yu, *J. Korean Phys. Soc.* **67**, 1089-1094 (2015).  
T. Vrancx, J. Ryckebusch & J. Nys, *Phys. Rev C*, **89** 065202 (2014).

S.V. Goloskokov, P. Kroll, *Eur. Phys. J. C* **65** 137 (2010).  
B. Berthou et al, *Eur. Phys. J. C* **78** 478 (2018).



# Comparison with Theory

$p(e, e' \pi^+) n$



**VR (Regge):** Good agreement at low  $-t$ , poor agreement for higher  $-t$

**GK1 (GPD):** Decent reproduction of  $-t$  dependence for  $x_B = 0.4$  but overestimates magnitude

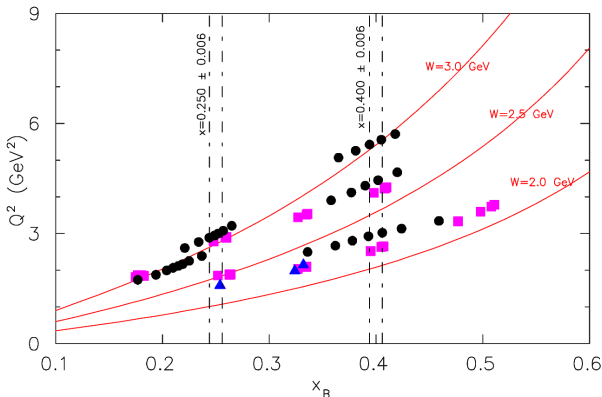
**GK2 (GPD):** Modification  $H_T \rightarrow H_T * 2$  improves agreement

**YCK1 (Regge + GPD):** Best overall agreement

**YCK2 (Regge):** Underestimates magnitude

T. K. Choi, K.-J. Kong & B.-G. Yu, J. Korean Phys. Soc. **67**, 1089-1094 (2015).  
T. Vranckx, J. Ryckebusch & J. Nys, Phys. Rev. C, **89** 065202 (2014).

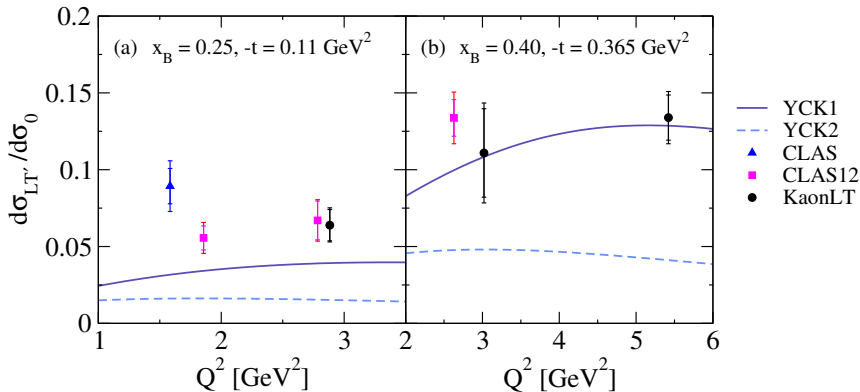
S.V. Goloskokov, P. Kroll, Eur. Phys. J. C **65** 137 (2010).  
B. Berthou et al, Eur. Phys. J. C **78** 478 (2018).



- Kinematics for measurements of  $\sigma_{LT'}/\sigma_0$  from **KaonLT** [This work], **CLAS**, and **CLAS12**
- Combine data sets to determine  $Q^2$  dependence at fixed  $(x_B, -t)$

# $Q^2$ Dependence

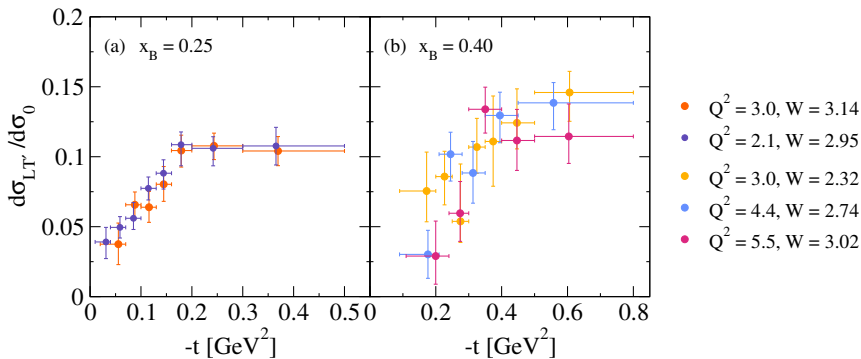
$\rho(e, e' \pi^+) n$



- $\sigma_{LT'}/\sigma_0$  from **KaonLT** [This work], **CLAS**, and **CLAS12** as a function of  $Q^2$
- Flat or weak  $Q^2$  dependence

# What If...

$\rho(e, e' \pi^+) n$



- No  $Q^2$  dependence → overlay curves at same  $x_B$
- Seems to show same  $-t$  dependence within uncertainties



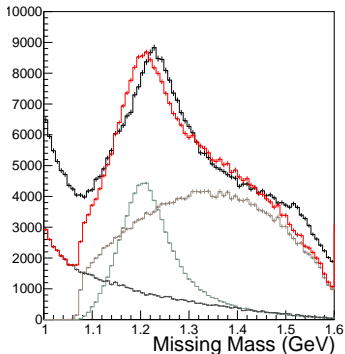
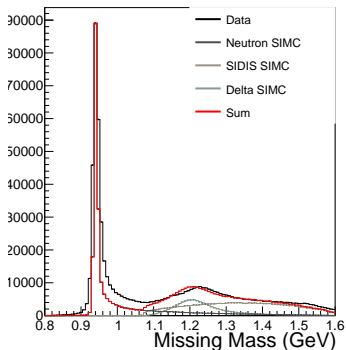
- $\sigma_{LT'}/\sigma_0$  extracted from KaonLT data over a wide range of kinematics
- Magnitude and  $-t$  dependence closest to **YCK1**
- Combined Regge/GPD description likely most accurate
- Flat  $Q^2$  dependence predicted by **YCK2**

For submission to Physical Review Letters **this week**  
→ Comments from co-authors requested by **tomorrow** to  
**acp548@uregina.ca**

*Manuscript can be found **HERE***

$$\rho(e, e' \pi^+) \Delta^0$$

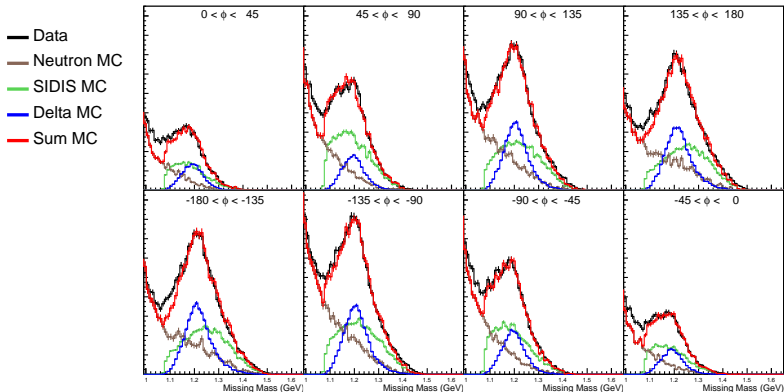
- Missing mass much more complicated than  $\rho(e, e'\pi^+)n$  due to overlapping channels



Plot by Ali Usman. Kinematics  $Q^2=2.115$ ,  $W=2.95$ , SHMS center.

# Shape Study

$$\rho(e, e' \pi^+) \Delta^0$$



- Fit missing mass with sum of **delta**, **neutron**, and **SIDIS** MC
- Yield is integral of **delta** MC

Plots by Ali Usman, based on initial work by Portia Switzer. Kinematics  $Q^2=2.115, x_B=0.25$ , SHMS center,  $0.10 < -t < 0.27$ .



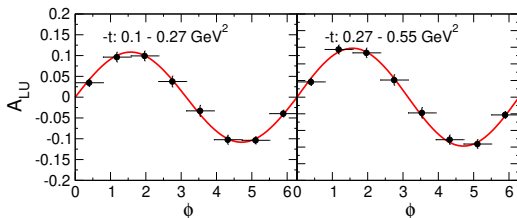
# Asymmetry

$\rho(e, e' \pi^+) \Delta^0$



- Due to lower statistics, we have 1-2 bins in  $-t$  and 9 in  $\phi$  for  $\rho(e, e' \pi^+) \Delta^0$
- Errors are purely statistical

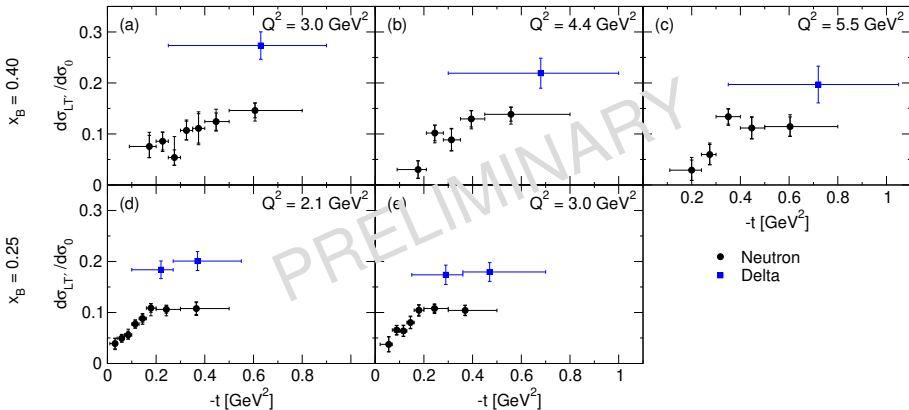
$$A_{LU} = \frac{1}{P} \left( \frac{N^+ - N^-}{N^+ + N^-} \right), \quad \delta_{\text{stat}} = \frac{2}{P} \sqrt{\frac{N^+ N^-}{(N^+ + N^-)^3}}$$



Plots:  $Q^2=2.115$ ,  $W=2.95$ .

# Results

$\rho(e, e' \pi^+) \Delta^0$

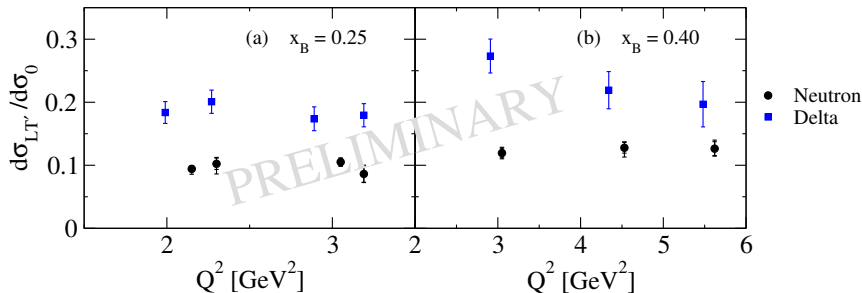


■ Extracted values of  $\sigma_{LT'}/\sigma_0$  in exclusive  $\pi^+$  production

■ Errors on  $\Delta^0$  are only statistical

# $Q^2$ Dependence

$p(e, e' \pi^+) \Delta^0$



- $Q^2$  dependence of  $\sigma_{LT'}/\sigma_0$  in exclusive  $\pi^+$  production
- Neutron channel **re-analyzed** using bins optimized for  $\Delta^0$
- No systematic errors  $\rightarrow$  trend in (b)  $\Delta^0$  likely not significant

# Summary

$\rho(e, e' \pi^+) \Delta^0$



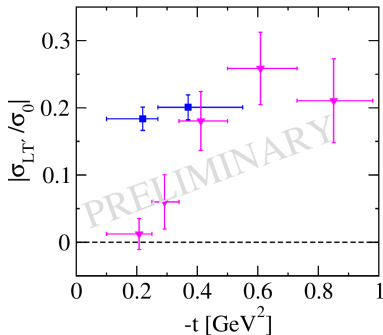
- This data is the first ever measurement of  $A_{LU}$  in  $\rho(e, e' \pi^+) \Delta^0$
- No known theoretical predictions to use for comparison
- Systematic errors must be calculated

Compare with previous results in  
 $e + p \rightarrow e' + \pi^- + \Delta^{++}$  from CLAS12

$\pi^+ \Delta^0$  **KaonLT**:  $Q^2=2.1$ ,  $x_B=0.25$

$\pi^- \Delta^{++}$  **CLAS12**:  $Q^2=1.95$ ,  $x_B=0.19$

→ Note  $\sigma_{LT'}/\sigma_0$  has **opposite sign**  
between these channels





- Submitting  $\rho(e, e'\pi^+)n$  results to PRL (A. Postuma)
- Writing a manuscript for PRL on  $\rho(e, e'\pi^+)\Delta^0$  (A. Usman)
- Next study:  $u$ -channel BSA (A. Postuma)
- Possible projects: BSA for  $K^+$  production in KaonLT, numerous channels in **PionLT** data (unclaimed)  
*suitable for undergraduate summer student projects*

## ■ KaonLT working group and shift takers

*We thank the staff of the Accelerator and the Physics Divisions at Jefferson Lab for the excellent efforts during the experimental data taking. This work is supported by the Natural Sciences and Engineering Research Council of Canada (NSERC) SAPIN-2021-00026 and a Canadian Institute of Nuclear Physics Graduate Fellowship. Additional support from the University of Regina is gratefully acknowledged. This material is based upon work supported by the U.S. Department of Energy, Office of Science, Office of Nuclear Physics under contract DE-AC05-06OR23177. Support is also acknowledged from NSF grants PHY 2309976, 2012430 and 1714133 at the Catholic University of America, NSF grant PHY 2209199 at Ohio University, and by the National Research Foundation of Korea Grant No. NRF-2022R1A2B5B01002307.*



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