



**Meson Structure at the EIC**

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University of Regina**

**Workshop on Hadron Structure at  
High-Energy, High-Luminosity Facilities  
26/10/21**

# Outline

- Meson Form Factors
- Measuring Form Factors
  - Pion Form Factor
  - Kaon Form Factor
- What can we achieve at the EIC?

Cover Image - Brookhaven National Lab, <https://www.flickr.com/photos/brookhavenlab/>

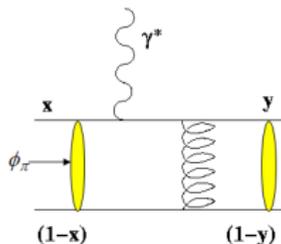
# Meson Form Factors

- Pion and Kaon form factors ( $F_\pi$ ,  $F_K$ ) are key QCD observables
  - Describe the spatial distribution of partons within a hadron
- $F_\pi$  and  $F_K$  of special interest in hadron structure studies
  - $\pi$  - Lightest QCD quark system, crucial in understanding dynamic mass generation
  - $K$  - Next simplest system, contains strangeness
- Clearest case for studying transition from perturbative to non-perturbative regime
- Existing data are good, but need to push  $Q^2$  reach further

# The Pion in pQCD 1/2

- At very large  $Q^2$ ,  $F_\pi$  can be calculated using pQCD via -

$$F_\pi(Q^2) = \frac{4_F \alpha_s(Q^2)}{Q^2} \left| \sum_{n=0}^{\infty} a_n \left( \log \left( \frac{Q^2}{\Lambda^2} \right) \right)^{-\gamma_n} \right|^2 \left[ 1 + O \left( \alpha_s(Q^2), \frac{m}{Q} \right) \right]$$



# The Pion in pQCD 2/2

- At asymptotically high  $Q^2$  ( $Q^2 \rightarrow \infty$ ), the pion distribution amplitude becomes -

$$\phi_\pi(x) \rightarrow \frac{3f_\pi}{\sqrt{n_c}} x(1-x)$$

- With  $f_\pi = 93 \text{ MeV}$ , the  $\pi^+ \rightarrow \mu^+ \nu$  decay constant
- $F_\pi$  takes the form -

$$Q^2 F_\pi \rightarrow 16\pi\alpha_s(Q^2) f_\pi^2$$

- This only relies on asymptotic freedom in QCD, i.e.  $(\partial\alpha_s/\partial\mu) < 0$  as  $\mu \rightarrow \infty$
- $Q^2 F_\pi$  should behave as  $\alpha_s(Q^2)$ , even for moderately large  $Q^2$
- Pion form factor seems to be the best tool for experimental study of the nature of the quark-gluon coupling constant renormalisation

Eqns - G.P. Lepage, S.J. Brodsky, PLB 87, p359, 1979 | Closing Statement - A.V. Efremov, A.V. Radyushkin PLB 94, p245, 1980

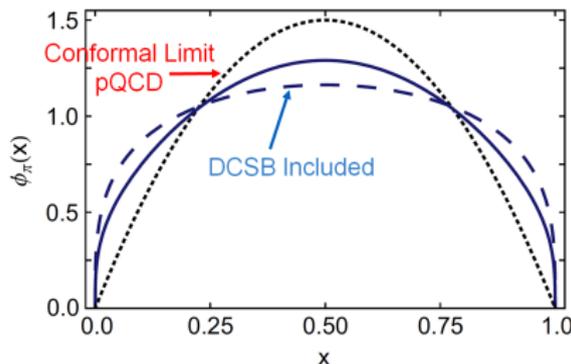
# Implications for Pion Structure 1/2

- Previous pQCD derivation used normalisation of  $F_\pi$  based on the conformal limit of the pion's twist 2-PDA -

$$\phi_\pi^{cl}(x) = 6x(1-x)$$

- Gives  $F_\pi$  that are “too small”
- Incorporating the DCSB effects yields Pion PDA -

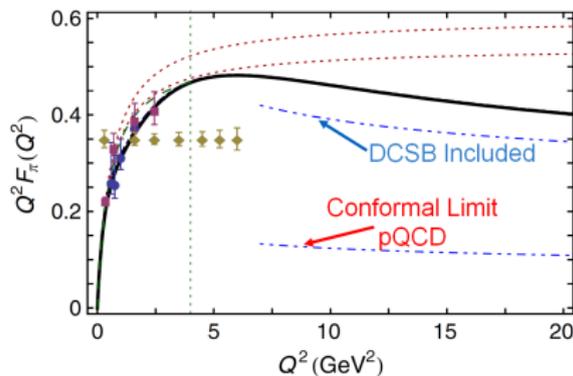
$$\phi_\pi(x) = \frac{8}{\pi} \sqrt{x(1-x)}$$



L. Chang, et al., PRL110(2013) 132001

# Implications for Pion Structure 2/2

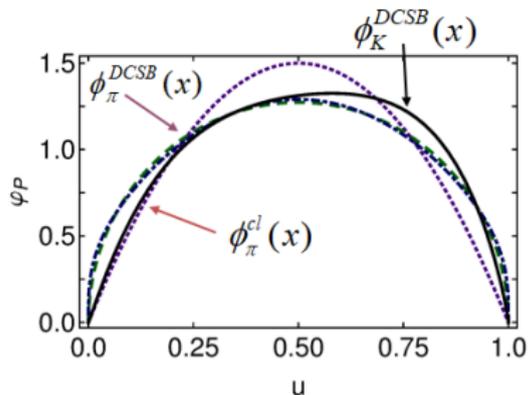
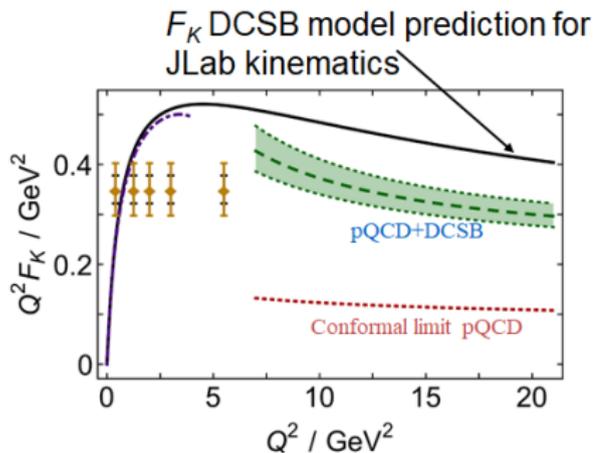
- Using this  $\phi_\pi(x)$  in the pQCD expression brings the  $F_\pi$  calculation much closer to the data
- Underestimates the full computation by  $\sim 15\%$  for  $Q^2 \geq 8 \text{ GeV}^2$



L. Chang, et al., PRL111(2013) 141802

# Effects of DCSB on $K^+$ Properties

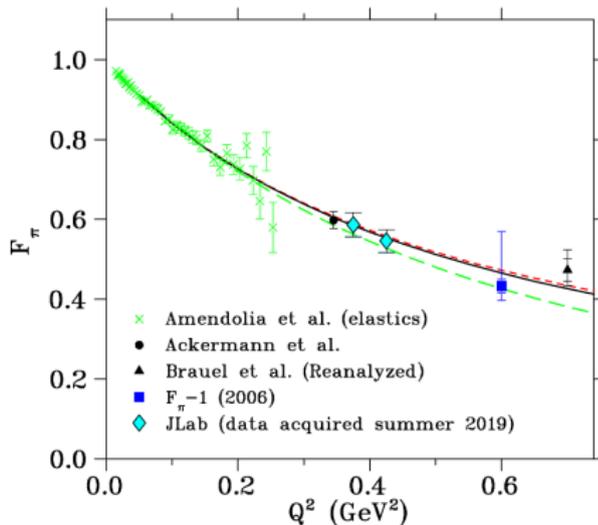
- $K^+$  PDA is also broad, concave and asymmetric
- Heavier  $s$  quark carries more bound state momentum than the  $u$  quark, shift is less than one might expect based on the difference in current quark masses.



C. Shi, et al., PRD 92 (2015) 014035, F. Guo, et al., PRD 96(2017) 034024 (Full calculation)

# Measurement of $F_\pi$ - Low $Q^2$

- At low  $Q^2$ ,  $F_\pi$  can be measured model independently
  - High energy elastic  $\pi^-$  scattering from atomic electrons in  $H$
- CERN SPS used 300 GeV pions to measure  $F_\pi$  up to  $Q^2 = 0.25 \text{ GeV}^2$
- Used data to extract pion charge radius -  $r_\pi = 0.657 \pm 0.012 \text{ fm}$
- Maximum accessible  $Q^2$  approximately proportional to pion beam energy
  - $Q^2 = 1 \text{ GeV}^2$  requires 1 TeV pion beam (!)



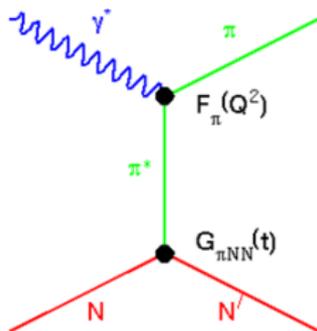
Amendolia, et al., NPB 277(1986) p168, P. Brauel, et al., ZPhysC (1979), p101, H. Ackermann, et al., NPB137 (1978), p294

# Measurement of $F_\pi$ at Higher $Q^2$

- To access  $F_\pi$  at high  $Q^2$ , must measure  $F_\pi$  indirectly
  - Use the “pion cloud” of the proton via pion electroproduction  $p(e, e'\pi^+)n$
  - At small  $-t$ , the pion pole process dominates the longitudinal cross section,  $\sigma_L$
- In the Born term model,  $F_\pi^2$  appears as -

$$\frac{d\sigma_L}{dt} \propto \frac{-tQ^2}{(t - m_\pi^2)} g^2(t) F_\pi^2(Q^2, t)$$

- Drawbacks of this technique -
  - Isolating  $\sigma_L$  experimentally challenging
  - Theoretical uncertainty in  $F_\pi$  extraction  
→ **Model dependent**  
(smaller dependency at low  $-t$ )

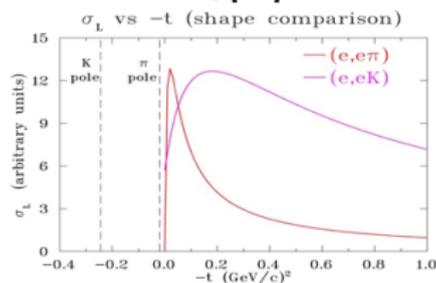
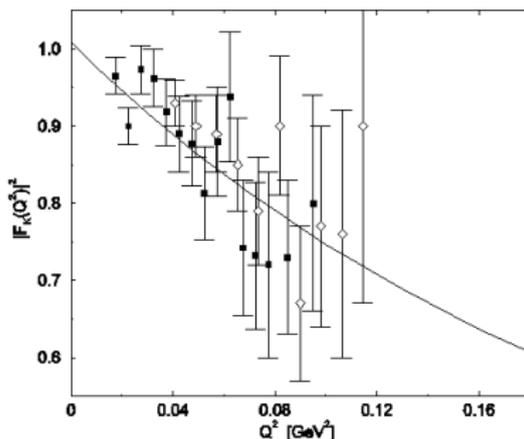


# Measurement of $F_K$

- Similar to  $F_\pi$ , elastic  $K^+$  scattering from  $e^-$  used to determine  $F_K$  at low  $Q^2$
- Can “kaon cloud” of the proton be used in the same way as the pion to extract  $F_K$  from electroproduction?
- Kaon pole further from kinematically allowed region

$$\frac{d\sigma_L}{dt} \propto \frac{-tQ^2}{(t - m_K^2)} g_K^2(T) F_K^2(Q^2, t)$$

- Issues are being explored and tested in JLab E12-09-011



Amendolia, et al., PLB178(1986)435

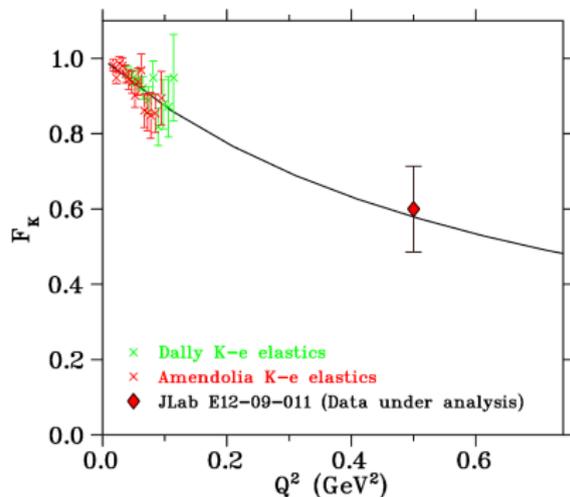
# $F_K$ Validation

- Low  $Q^2$  data is an important test
- Due to experimental setup, can simultaneously study  $\Lambda^0$  and  $\Sigma^0$  channels

- Can conduct a pole dominance test through the ratio -

$$\frac{\sigma_L [p(e, e'K^+)\Sigma^0]}{\sigma_L [p(e, e'K^+)\Lambda^0]}$$

- Should be similar to ratio of  $g_{pK\Lambda}^2/g_{pK\Sigma}^2$  if t-channel exchange dominates



# Form Factors at the EIC

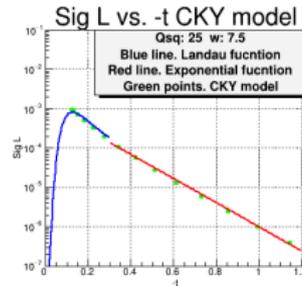
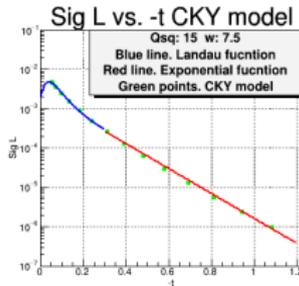
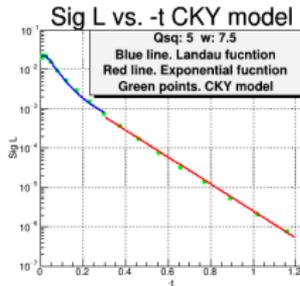
- JLab measurements push the  $Q^2$  reach of data considerably
- Still can't answer some key questions regarding the emergence of hadronic mass however
- Can we get quantitative guidance on the emergent pion mass mechanism?  
→ Need  $F_\pi$  data for  $Q^2 = 10 - 40 \text{ GeV}c^{-2}$
- What is the size and range of interference between emergent mass and the Higgs-mass mechanism?  
→ Need  $F_K$  data for  $Q^2 = 10 - 20 \text{ GeV}c^{-2}$
- Beyond what is possible at JLab in the 12 GeV era
  - Need a different machine → **The Electron-Ion Collider (EIC)**

# DEMP Studies at the EIC

- Measurements of the  $p(e, e'\pi^+n)$  reaction at the EIC have the potential to extend the  $Q^2$  reach of  $F_\pi$  measurements even further
- A challenging measurement however
  - Need good identification of  $p(e, e'\pi^+n)$  triple coincidences
  - Conventional L-T separation not possible  $\rightarrow$  would need lower than feasible proton energies to access low  $\epsilon$
  - Need to use a model to isolate  $d\sigma_L/dt$  from  $d\sigma_{uns}/dt$
- Utilise new EIC software framework to assess the feasibility of the study with updated design parameters
  - Feed in events generated from a DEMF event generator
  - Multiple detector concepts to evaluate
- Event generator being modified to generate kaon events

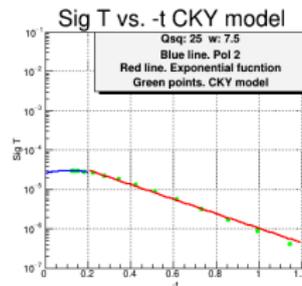
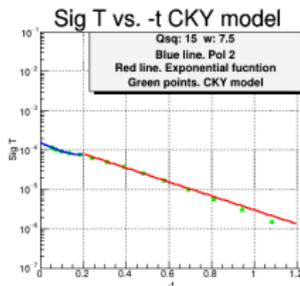
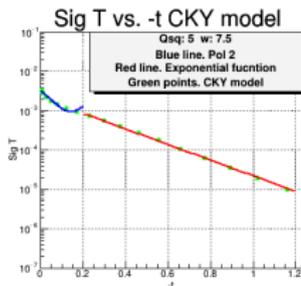
# DEMP Event Generator

- Want to examine **exclusive** reactions
  - $p(e, e'\pi^+n)$  **exclusive reaction** is reaction of interest
    - $\rightarrow p(e, e'\pi^+)X$  SIDIS events are background
- Generator uses Regge-based  $p(e, e'\pi^+)n$  model from T.K. Choi, K.J. Kong and B.G. Yu (CKY) - arXiv 1508.00969
  - MC event generator created by parametrising CKY  $\sigma_L, \sigma_T$  for  $5 < Q^2 < 35, 2 < W < 10, 0 < -t < 1.2$

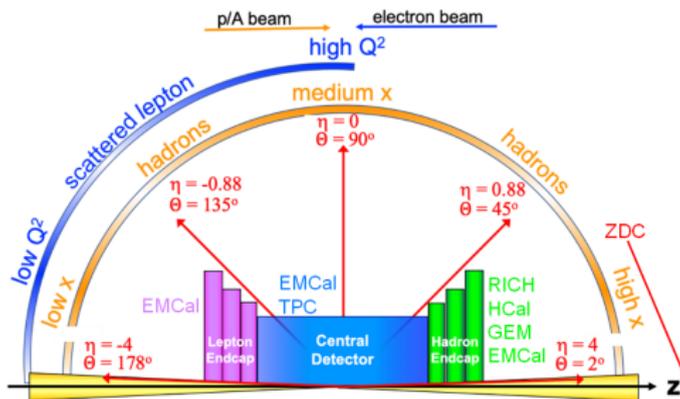


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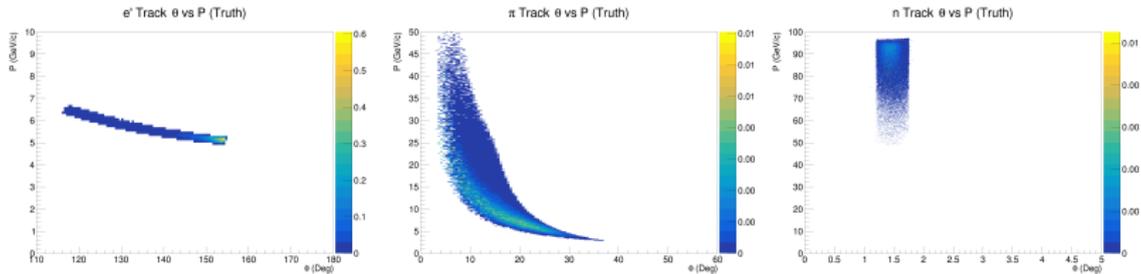


# EIC Detector Overview



- Feed generator output into detector simulations
- Various detector concepts
- All share common elements
- Current simulation effort has been focused on the EIC Comprehensive Chromodynamics Experiment (ECCE)
  - <https://www.ecce-eic.org/>

# $p(e, e'\pi^+n)$ - Particle Distributions



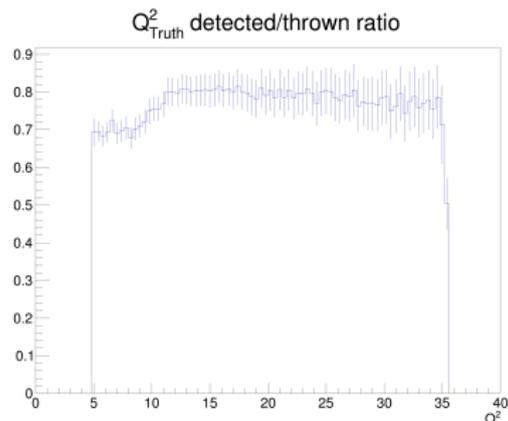
- Truth level particle distributions for  $p(e, e'\pi^+n)$  events
- Neutrons take most of the momentum, forward focused
- Electrons and pions spread over wider range of angles

# Selecting Good Simulated Events

- Pass through a full Geant4 simulation (ECCE)
  - More realistic estimates of detector acceptance/performance than earlier studies
- Identify  $e'\pi^+n$  triple coincidences in the simulation output
- For a good triple coincidence event, require -
  - Exactly two tracks
    - One positively charged track going in the  $+z$  direction ( $\pi^+$ )
    - One negatively charged track going in the  $-z$  direction ( $e'$ )
  - At least hit in the zero degree calorimeter (ZDC)
    - For 5 ( $e'$ , GeV) on 100 ( $p$ , GeV) events, require that the hit has an energy deposit over 40 GeV
- Both conditions must be satisfied
- Determine kinematic quantities for remaining events

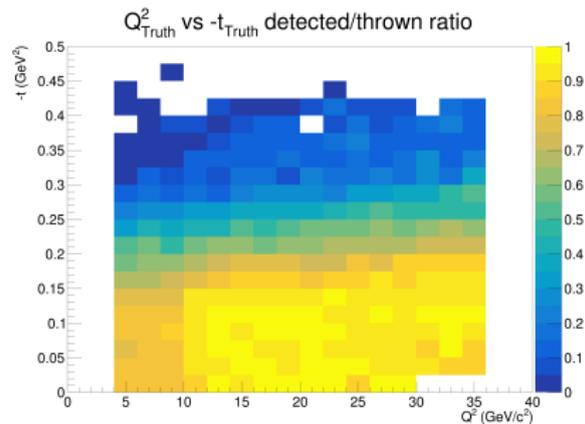
# Simulation Results - Detection Efficiency

- Can examine truth quantities too, quick check of detection efficiency
- $\text{Efficiency} = \frac{\text{Accepted}}{\text{Thrown}}$
- Detection efficiency fairly high,  $\sim 80\%$
- Nearly independent of  $Q^2$
- Detection efficiency highest for low  $-t$ 
  - Falls off rapidly with increasing  $-t$
  - Dictated by size of ZDC



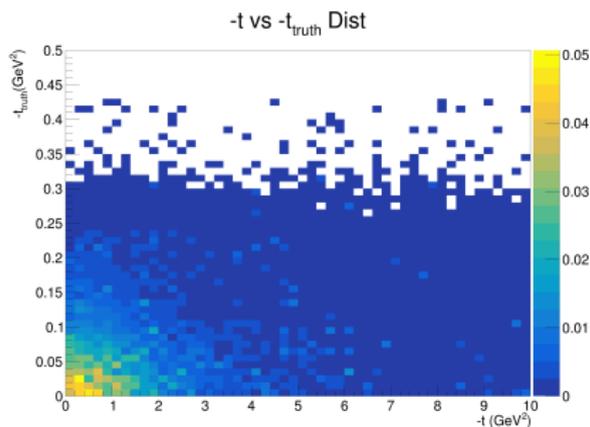
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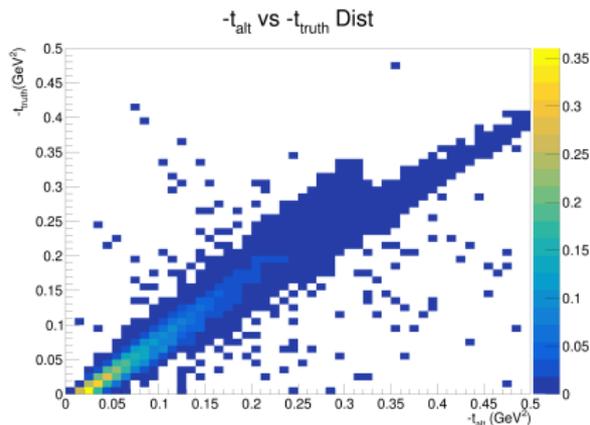
# Simulation Results - $t$ Reconstruction

- Reconstruction of  $-t$  from detected  $e'$  and  $\pi^+$  tracks proved highly unreliable
  - $-t = -(p_e - p_{e'} - p_\pi)^2$
- Calculation of  $-t$  from detected neutron track matched "truth" value very closely
  - $-t_{alt} = -(p_p - p_n)^2$
- Only possible due to the excellent position accuracy provided by a good ZDC

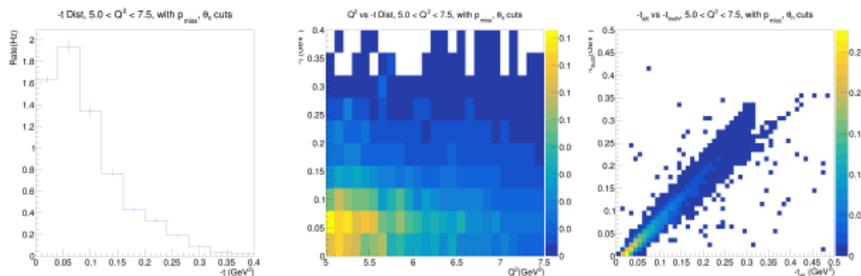


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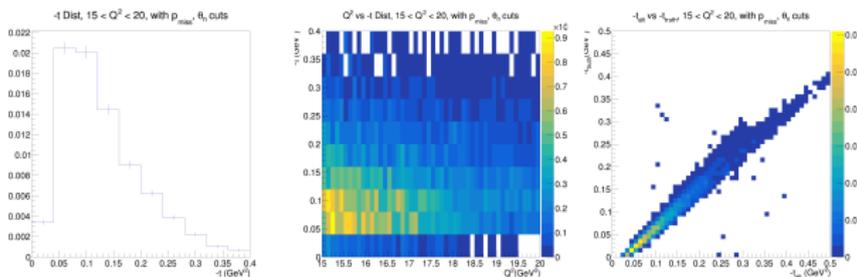


# Simulation Results



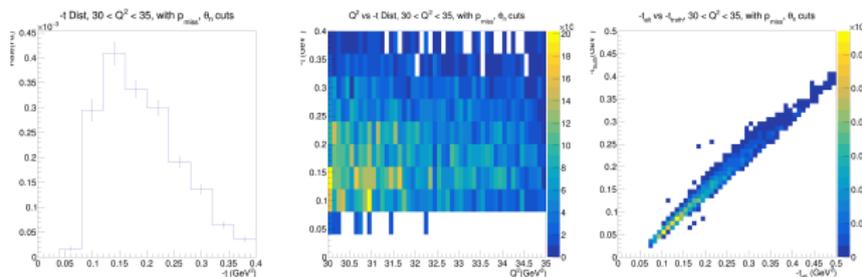
- Predicted  $e'\pi^+n$  triple coincidence rate, binned in  $Q^2$  and  $-t$ 
  - 5 ( $e'$ , GeV) on 100 ( $p$ , GeV) events
  - $\mathcal{L} = 10^{34} \text{cm}^{-2} \text{s}^{-1}$  assumed
  - $-t$  bins are 0.04 GeV<sup>2</sup> wide
  - Cut on  $\theta_n$  ( $\theta_n = 1.45 \pm 0.5^\circ$ ) and  $\vec{p}_{miss} = \vec{p}_e + \vec{p}_p - \vec{p}_{e'} - \vec{p}_{\pi^+}$  (varies by  $Q^2$  bin) to simulate removal of SIDIS background
- $-t_{min}$  migrates with  $Q^2$  as expected

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# Isolating $\sigma_L$ from $\sigma_T$ in an e-p Collider

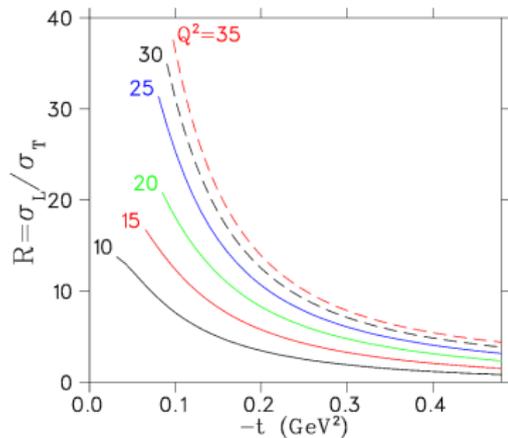
- For a collider -

$$\epsilon = \frac{2(1-y)}{1+(1-y)^2} \quad \text{with} \quad y = \frac{Q^2}{x(s_{tot} - M_N^2)}$$

- $y$  is the fractional energy loss
- Systematic uncertainties in  $\sigma_L$  magnified by  $1/\Delta\epsilon$ 
  - Ideally,  $\Delta\epsilon > 0.2$
- To access  $\epsilon < 0.8$  with a collider, need  $y > 0.5$ 
  - Only accessible at small  $s_{tot}$
  - Requires low proton energies ( $\sim 10$  GeV), luminosity too low
- Conventional L-T separation not practical, need another way to determine  $\sigma_L$

# $\sigma_L$ Isolation with a Model at the EIC

- QCD scaling predicts  $\sigma_L \propto Q^{-6}$   
and  $\sigma_T \propto Q^{-8}$
- At the high  $Q^2$  and  $W$  accessible at the EIC, phenomenological models predict  $\sigma_L \gg \sigma_T$  at small  $-t$
- Can attempt to extract  $\sigma_L$  by using a model to isolate dominant  $d\sigma_L/dt$  from measured  $d\sigma_{UNS}/dt$
- Critical to confirm the validity of the model used!



Predictions are assuming  $\epsilon > 0.9995$  with the kinematic ranges seen earlier

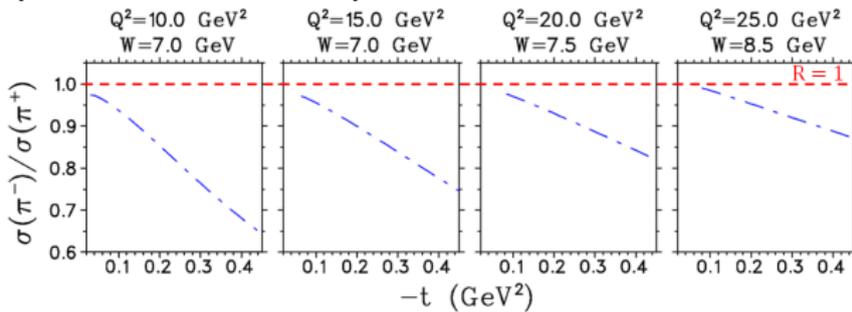
T.Vrancx, J. Ryckebusch, PRC 89(2014)025203

# Model Validation via $\pi^-/\pi^+$ ratios

- Measure exclusive  ${}^2H(e, e'\pi^+n)n$  and  ${}^2H(e, e'\pi^-p)p$  in same kinematics as  $p(e, e'\pi^+n)$
- $\pi$   $t$ -channel diagram is purely isovector  $\rightarrow$  G-Parity conserved

$$R = \frac{\sigma [n(e, e'\pi^-p)]}{\sigma [p(e, e'\pi^+n)]} = \frac{|A_V - A_S|^2}{|A_V + A_S|^2}$$

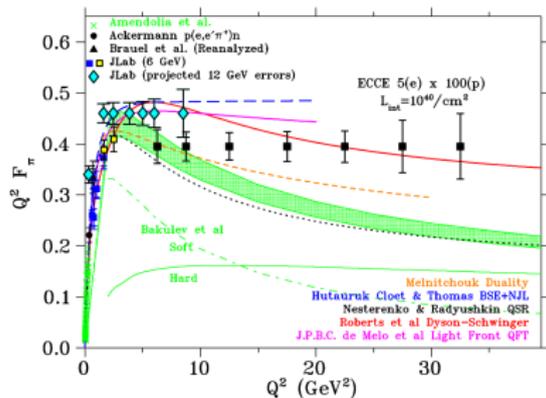
- $R$  will be diluted if  $\sigma_T$  not small or if there are significant non-pole contributions to  $\sigma_L$
- Compare  $R$  to model expectations



T.Vrancx, J. Ryckebusch, PRC 89(2014)025203

# EIC Kinematic Reach for $F_\pi$

- ECCE appears to be capable of measuring  $F_\pi$  to  $Q^2 \sim 32.5 \text{ GeV}^2$
- Error bars represent real projected error bars
  - 2.5% point-to-point
  - 12% scale
  - $\delta R = R$ ,  $R = \sigma_L / \sigma_T$
  - $R = 0.013 - 0.014$  at lowest  $-t$  from VR model
- Uncertainties dominated by  $R$  at low  $Q^2$
- Statistical uncertainties dominate at high  $Q^2$



- Results look promising, need to test other detector concepts
- More details in upcoming ECCE analysis note

# Summary and Outlook

- EIC has the potential to push the  $Q^2$  reach of  $F_\pi$  measurements
- **Work already featured in the EIC yellow report**
- Now working closely with detector proto-collaborations
  - **Carrying out feasibility studies**
  - Existing DEMP event generator utilised
  - **Kaon event generator and simulations in progress**
  - **Activities are a priority for the ECCE Diffractive and Tagging group**
- Results from simulation have been written up in an ECCE analysis note
  - **Expect to see this soon!**

R. Abdul Khalek et al. EIC Yellow Report. 2021. arXiv:2103.05419, Sections 7.2.1 and 8.5.1

Thanks for listening, any questions?



University  
of Regina



**S.J.D. Kay**, G.M. Huber, Z. Ahmed, Ali Usman, Daniele Binosi, Huey-Wen Lin, Timothy Hobbs, Arun Tadepalli, Rachel Montgomery, Paul Reimer, David Richards, Rik Yoshida, Craig Roberts, Thia Keppel, John Arrington, Lei Chang, Ian L. Pegg, Jorge Segovia, Carlos Ayerbe Gayoso, Wenliang Li, Yulia Furletova, Dmitry Romanov, Markus Diefenthaler, Richard Trotta, Tanja Horn, Rolf Ent, Tobias Frederico

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